

```

> restart;
with(plots):
with(StringTools):
with(LinearAlgebra):
with(DEtools):

#####

Region:='SPB'; url:="https://gogov.ru/covid-19/spb#data";

#valp := [11.3603305375848, 14475.0879688793, 0.0765869162260003, 0.135376422146201,
0.209261126269982, 0.153145171332402, #0.106398829547104, 0.106093197464564, 0.159923251386689,
0.200585027191738, 0.0222217255445156, 0.0124207218170124, #0.0000954521220352052];

valp:=readdata(cat(Region,`3c.txt`));

#####

fdisplay:=proc(f,p)
  print(cat(f,`.jpg`)); #print(cat(f,`.eps`));
  plotsetup(jpeg,plotoutput=cat(f,`.jpg`),plotoptions=`noborder`); print(display(p));
  plotsetup(ps,plotoutput=cat(f,`.eps`),plotoptions=`noborder`); print(display(p));
  plotsetup(default,plotoptions=`noborder`): print(display(p));
end:

pr:=proc(x) print(x); x; end:

grad:=(F,V)->map(q->diff(F,q),V):

linsplit:=(F,V)->subs(map(q->q=0,V),[op(grad(F,V)),F]):

corr:=proc(x,y) local i; seq(x[i]=y[i],i=1..nops(x)): end:

ssum:=(F,V)->convert([seq(F,V)],`+`):

pprod:=(F,V)->convert([seq(F,V)],`*`):

Lag:=proc(t,tx,kx) local i,j;
  ssum(kx[i]*pprod(piecewise(j=i,1,(t-tx[j])/(tx[i]-tx[j])),j=1..nops(tx)),i=1..nops(tx)):
end:

```

```
Lag(t, [ta, tb], [a, b]); Lag(t, [ta, tb, tc], [a, b, c]);
```

```
pi:=evalf(Pi);
```

```
gM:=evalf(solve((1-x)^2=x,x)[2]):
```

```
goldMin:=proc(f,T,epsilon) local a,b,c,d,fa,fb,fc,fd,k;
```

```
  a:=op(1,T); b:=op(2,T); fa:=f(a); fb:=f(b); k:=0;
```

```
  c:=a+(b-a)*gM; fc:=f(c); d:=b-(b-a)*gM; fd:=f(d);
```

```
  while abs(a-b)>epsilon do: k:=k+1;
```

```
    if fc>fd then a:=c; fa:=fc; c:=d; fc:=fd; d:=b-(b-a)*gM; fd:=f(d);
```

```
    else b:=d; fb:=fd; d:=c; fd:=fc; c:=a+(b-a)*gM; fc:=f(c);
```

```
    fi;
```

```
  od: #print(k);
```

```
  (a+b)/2;
```

```
end:
```

```
findMin1:=proc(F,V) local f,df,f0,f1,f2,V0,V1,V2,ff,t,dt,i,j;
```

```
  ff:=V->F(op(evalf(map(exp,V)))); V1:=evalf(map(ln,V)); f1:=F(op(V));
```

```
  f:=[seq(F(seq(evalf(exp(V1[j]+piecewise(j=i,0.0001,0))),j=1..nops(V))),i=1..nops(V))];
```

```
  df:=[seq((f[j]-f1)/0.1,j=1..nops(V))];
```

```
  V0:=V1-0.001*df; f0:=ff(V0); V2:=V1+0.001*df; f2:=ff(V2);
```

```
  dt:=0.0001; while f0<f1 do: V2:=V1; f2:=f1; V1:=V0; f1:=f0; V0:=V0-dt*df; f0:=ff(V0); dt:=dt*1.1; od;
```

```
  dt:=0.0001; while f2<f1 do: V0:=V1; f0:=f1; V1:=V2; f1:=f2; V2:=V2+dt*df; f2:=ff(V2); dt:=dt*1.1; od;
```

```
  t:=goldMin(t->ff(t*V0+(1-t)*V2),0..1,0.0001);
```

```
  map(exp,t*V0+(1-t)*V2);
```

```
end:
```

```
findMin:=proc(F,V) local V1,Z1,Z2;
```

```
  Z2:=pr(F(op(V))); V1:=findMin1(F,V); Z1:=pr(chi2(op(V1)));
```

```
  while abs(1-Z1/Z2)>0.0001 do: Z2:=Z1; V1:=findMin1(F,V1); Z1:=pr(chi2(op(V1))); end;
```

```
  V1;
```

```
end:
```

Region := SPB

url := "https://gogov.ru/covid-19/spb#data"

valp := [11.34559215, 14531.33433, 0.07651405402, 0.1357064959, 0.2088665537, 0.1529316885, 0.1062966889, 0.1061385194,

0.1591816715, 0.2012023713, 0.02219897076, 0.01230862757, 0.00009541581785]

$$\frac{a(t-tb)}{ta-tb} + \frac{b(t-ta)}{tb-ta}$$

$$\frac{a(t-tb)(t-tc)}{(ta-tb)(ta-tc)} + \frac{b(t-ta)(t-tc)}{(tb-ta)(tb-tc)} + \frac{c(t-ta)(t-tb)}{(tc-ta)(tc-tb)}$$

$$\pi := 3.141592654$$

(1)

```
> =====`;  
`VERHULST FITTING`;  
`=====`;
```

=====

VERHULST FITTING

=====

(2)

```
> f_:=d->sum(a[j]*d^j,j=0..n); fe_:=d->sum(a[j]*d^j,j=0..ne);  
  
M:='M':  
ff:=x->M*(1-1/(exp(x)+1)); ff_:=unapply(solve(y=ff(x),x),y); diff(ff_(x),x); dff_:=unapply  
(simplify(% ,x),x);  
ffe:=x->exp(x); ffe_:=unapply(solve(y=ffe(x),x),y); diff(ff_(x),x); dffe_:=unapply(simplify(% ,  
x),x);  
  
sigma:=x->simplify(sqrt(x));  
  
chi2:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dff_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));  
chi2e:=(T,f_)->simplify(sum(evalf(ff_(T[k])-f_(k))^2/dffe_(T[k])^2/sigma(T[k])^2,k=1..nops(T)));  
  
F:=proc(T,chi2,f_) chi2(T,f_);  
  indets(%); grad(% ,%); subs(solve(% ,%),f_(i)); unapply(% ,i);  
end;
```

$$f_ := d \mapsto \sum_{j=0}^n a_j \cdot d^j$$

$$fe_ := d \mapsto \sum_{j=0}^{ne} a_j \cdot d^j$$

$$ff := x \mapsto M \cdot \left(1 - \frac{1}{e^x + 1} \right)$$

$$ff_ := y \mapsto \ln \left(\frac{y}{M-y} \right)$$

$$\frac{\left(\frac{1}{M-x} + \frac{x}{(M-x)^2} \right) (M-x)}{x}$$

$$dff_ := x \mapsto \frac{M}{(M-x) \cdot x}$$

$$ffe := x \mapsto e^x$$

$$ffe_ := y \mapsto \ln(y)$$

$$\frac{1}{x}$$

$$dffe_ := x \mapsto \frac{1}{x}$$

$$\sigma := x \mapsto \text{simplify}(\sqrt{x})$$

$$\chi_2 := (T, f_) \rightarrow \text{simplify} \left(\sum_{k=1}^{nops(T)} \frac{\text{evalf}(ff_ (T_k) - f_ (k))^2}{dff_ (T_k)^2 \sigma(T_k)^2} \right)$$

$$\chi_{2e} := (T, f_) \rightarrow \text{simplify} \left(\sum_{k=1}^{nops(T)} \frac{\text{evalf}(ffe_ (T_k) - f_ (k))^2}{dffe_ (T_k)^2 \sigma(T_k)^2} \right)$$

(3)

```

> dig:={"0","1","2","3","4","5","6","7","8","9","0"}: val:=proc() global data,i; local j,f; f:=0;
  while not(data[i] in dig) or f=1 and data[i] in {"+"} union dig do:
    if f=1 and not(data[i] in dig) then f:=0; else if data[i]="+" then f:=1; fi fi; i:=i+1: od:
    j:=i; while (data[i] in dig or data[i] in {"-","+"}) do i:=i+1: od: parse(data[j..i-1]);
  end:
  ``; Region; status,data,headers:=HTTP:-Get(url): HTTP:-Code(status); i:=Search("<th>",data):

iter:=proc() global i; local r;
  r:=val(); if data[i]<>"." then NULL else [r,val(),val(),val(),val(),val()],iter() fi;

```

end:

```
[iter()]: tA:=[seq(%[nops(%) +1 -i], i=1..nops(%))];  
dd:=tA[1][1]+piecewise(tA[1][2]=2, -29, tA[1][2]=4, 31, 0) -1;  
T:=map(q->q[4], tA): #writedata(Region || '-i.txt', %): #  
T3:=map(q->q[5], tA): #writedata(Region || '-m.txt', %): #  
T1:=map(q->q[6], tA): #writedata(Region || '-r.txt', %): #  
T2:=[seq(T[i] - (T1[i] + T3[i]), i=1..nops(T))]: #writedata(Region || '-h.txt', %): #  
i:='i':  
Region; 'T'=T; 'T1'=T1; 'T2'=T2; 'T3'=T3;  
  
nops(T); [i+dd $ i=1..%];
```

``
SPB
"OK"

```
tA := [[5, 3, 20, 1, 0, 0], [6, 3, 20, 1, 0, 0], [7, 3, 20, 2, 0, 0], [8, 3, 20, 2, 0, 0], [9, 3, 20, 2, 0, 0], [10, 3, 20, 2, 0, 0], [11, 3, 20, 2, 0, 0],  
[12, 3, 20, 2, 0, 0], [13, 3, 20, 5, 0, 0], [14, 3, 20, 6, 0, 0], [15, 3, 20, 6, 0, 0], [16, 3, 20, 9, 0, 2], [17, 3, 20, 9, 0, 2], [18, 3, 20, 9, 0, 2],  
[19, 3, 20, 10, 0, 2], [20, 3, 20, 14, 0, 2], [21, 3, 20, 16, 0, 2], [22, 3, 20, 16, 0, 2], [23, 3, 20, 16, 0, 2], [24, 3, 20, 21, 0, 2], [25, 3, 20,  
21, 0, 5], [26, 3, 20, 26, 0, 5], [27, 3, 20, 26, 0, 5], [28, 3, 20, 37, 0, 5], [29, 3, 20, 42, 1, 5], [30, 3, 20, 50, 1, 5], [31, 3, 20, 98, 2, 7], [1,  
4, 20, 125, 2, 7], [2, 4, 20, 147, 2, 7], [3, 4, 20, 156, 2, 7], [4, 4, 20, 171, 2, 7], [5, 4, 20, 191, 2, 7], [6, 4, 20, 226, 2, 32], [7, 4, 20, 295,  
2, 32], [8, 4, 20, 329, 2, 32], [9, 4, 20, 373, 4, 43], [10, 4, 20, 408, 4, 43], [11, 4, 20, 488, 4, 74], [12, 4, 20, 557, 4, 74], [13, 4, 20, 678,  
4, 78], [14, 4, 20, 799, 4, 78], [15, 4, 20, 929, 5, 95], [16, 4, 20, 1083, 7, 110], [17, 4, 20, 1507, 7, 131], [18, 4, 20, 1646, 8, 232], [19, 4,  
20, 1760, 8, 239], [20, 4, 20, 1846, 8, 241], [21, 4, 20, 1973, 11, 280], [22, 4, 20, 2267, 14, 327], [23, 4, 20, 2458, 17, 368], [24, 4, 20,  
2711, 20, 411], [25, 4, 20, 2926, 23, 460], [26, 4, 20, 3077, 27, 489], [27, 4, 20, 3238, 27, 489], [28, 4, 20, 3436, 27, 544], [29, 4, 20,  
3726, 29, 708], [30, 4, 20, 4062, 29, 779], [1, 5, 20, 4411, 33, 779], [2, 5, 20, 4734, 33, 877], [3, 5, 20, 5029, 34, 1061], [4, 5, 20, 5346,  
37, 1197], [5, 5, 20, 5572, 37, 1468], [6, 5, 20, 5884, 40, 1532], [7, 5, 20, 6190, 44, 1552], [8, 5, 20, 6565, 48, 1597], [9, 5, 20, 6990, 53,  
1662], [10, 5, 20, 7404, 53, 1674], [11, 5, 20, 7711, 56, 1681], [12, 5, 20, 8050, 58, 1784], [13, 5, 20, 8485, 63, 1848], [14, 5, 20, 8945,  
69, 1899], [15, 5, 20, 9486, 74, 2005], [16, 5, 20, 10011, 80, 2109], [17, 5, 20, 10462, 85, 2175], [18, 5, 20, 10887, 90, 2209], [19, 5, 20,  
11340, 95, 2272]]
```

dd := 4
SPB

```
T = [1, 1, 2, 2, 2, 2, 2, 2, 5, 6, 6, 9, 9, 9, 10, 14, 16, 16, 16, 21, 21, 26, 26, 37, 42, 50, 98, 125, 147, 156, 171, 191, 226, 295, 329, 373, 408, 488,
```

557, 678, 799, 929, 1083, 1507, 1646, 1760, 1846, 1973, 2267, 2458, 2711, 2926, 3077, 3238, 3436, 3726, 4062, 4411, 4734, 5029, 5346, 5572, 5884, 6190, 6565, 6990, 7404, 7711, 8050, 8485, 8945, 9486, 10011, 10462, 10887, 11340]

$T1 = [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 2, 2, 2, 2, 2, 2, 2, 5, 5, 5, 5, 5, 5, 7, 7, 7, 7, 7, 7, 32, 32, 32, 43, 43, 74, 74, 78, 78, 95, 110, 131, 232, 239, 241, 280, 327, 368, 411, 460, 489, 489, 544, 708, 779, 779, 877, 1061, 1197, 1468, 1532, 1552, 1597, 1662, 1674, 1681, 1784, 1848, 1899, 2005, 2109, 2175, 2209, 2272]$

$T2 = [1, 1, 2, 2, 2, 2, 2, 2, 5, 6, 6, 7, 7, 7, 8, 12, 14, 14, 14, 19, 16, 21, 21, 32, 36, 44, 89, 116, 138, 147, 162, 182, 192, 261, 295, 326, 361, 410, 479, 596, 717, 829, 966, 1369, 1406, 1513, 1597, 1682, 1926, 2073, 2280, 2443, 2561, 2722, 2865, 2989, 3254, 3599, 3824, 3934, 4112, 4067, 4312, 4594, 4920, 5275, 5677, 5974, 6208, 6574, 6977, 7407, 7822, 8202, 8588, 8973]$

$T3 = [0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 4, 4, 4, 4, 4, 4, 5, 7, 7, 8, 8, 8, 11, 14, 17, 20, 23, 27, 27, 27, 29, 29, 33, 33, 34, 37, 37, 40, 44, 48, 53, 53, 56, 58, 63, 69, 74, 80, 85, 90, 95]$

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$[5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67, 68, 69, 70, 71, 72, 73, 74, 75, 76, 77, 78, 79, 80]$

(4)

> $h := x \rightarrow x;$

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T))]; [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..nops(%))];  
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+3,%%[i]],i=1..nops(%%))]:  
display(  
  plot([%%,%,%],style=point),  
  plot([%%,%,%],legend=[``,``,``]),  
  title=`      N[i]`,titlefont=[roman,15],gridlines=true  
);
```

```
[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T)): [seq((%[i]-%[i-3])/3.,i=4..nops(%)): [seq((%[i]-%[i-3])/3.,i=4..nops(%))]:  
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]],i=1..nops(%%))]:  
display(  
  plot([%%,%,%],style=point),  
  plot([%%,%,%],legend=[``,``,``]),  
  title=`      N[i]`,titlefont=[roman,15],gridlines=true  
);
```

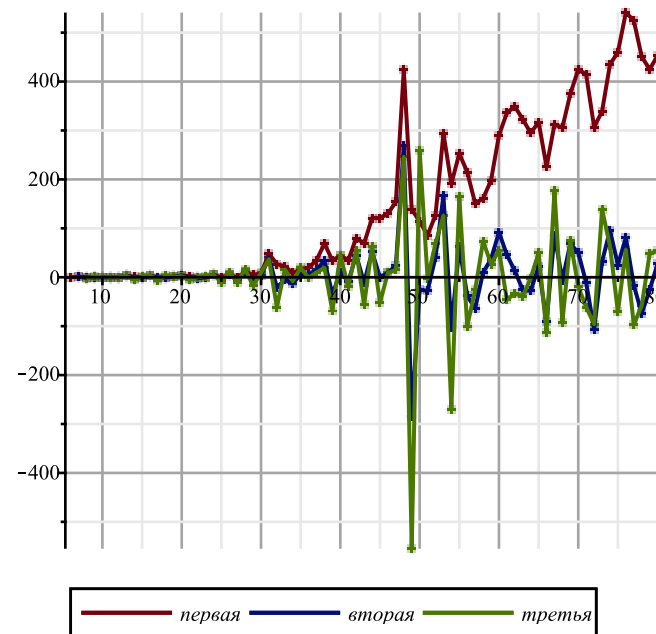
$h := x \mapsto x$

[0, 1, 0, 0, 0, 0, 3, 1, 0, 3, 0, 0, 1, 4, 2, 0, 0, 5, 0, 5, 0, 11, 5, 8, 48, 27, 22, 9, 15, 20, 35, 69, 34, 44, 35, 80, 69, 121, 121, 130, 154, 424, 139, 114, 86, 127, 294, 191, 253, 215, 151, 161, 198, 290, 336, 349, 323, 295, 317, 226, 312, 306, 375, 425, 414, 307, 339, 435, 460, 541, 525, 451, 425, 453]

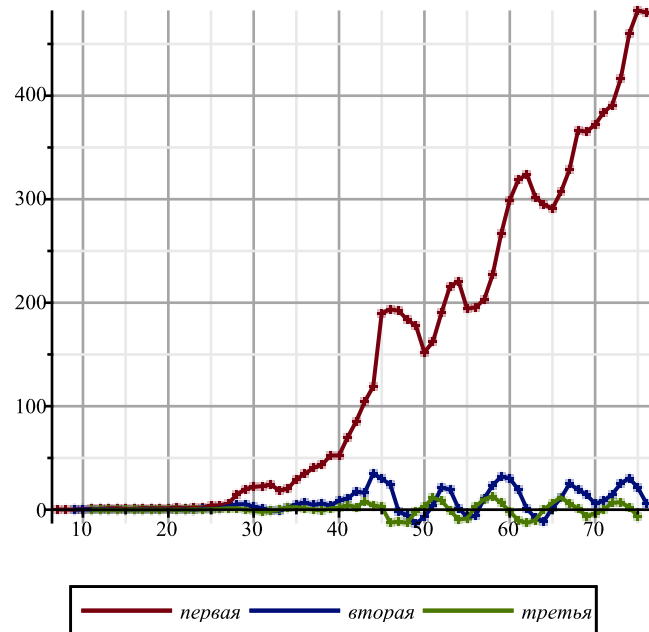
[1, -1, 0, 0, 0, 0, 3, -2, -1, 3, -3, 0, 1, 3, -2, -2, 0, 5, -5, 5, -5, 11, -6, 3, 40, -21, -5, -13, 6, 5, 15, 34, -35, 10, -9, 45, -11, 52, 0, 9, 24, 270, -285, -25, -28, 41, 167, -103, 62, -38, -64, 10, 37, 92, 46, 13, -26, -28, 22, -91, 86, -6, 69, 50, -11, -107, 32, 96, 25, 81, -16, -74, -26, 28]

[-2, 1, 0, 0, 0, 3, -5, 1, 4, -6, 3, 1, 2, -5, 0, 2, 5, -10, 10, -10, 16, -17, 9, 37, -61, 16, -8, 19, -1, 10, 19, -69, 45, -19, 54, -56, 63, -52, 9, 15, 246, -555, 260, -3, 69, 126, -270, 165, -100, -26, 74, 27, 55, -46, -33, -39, -2, 50, -113, 177, -92, 75, -19, -61, -96, 139, 64, -71, 56, -97, -58, 48, 54]

Разности ряда $N[i]$



Сглаженные разности ряда $N[i]$



```
> h:=x->ln(x);
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+3,%%[i]],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=['`', '`', '`']),
  title=' ln(N[i]) ',titlefont=[roman,15] ,gridlines=true
);
```

```
[seq((h(T[i])-h(T[i-5]))/5.,i=6..nops(T)): [seq((%[i]-%[i-3])/3.,i=4..nops(%)): [seq((%[i]-%[i-3])/3.,i=4..nops(%))]:
[seq([i+dd+2,%%[i]],i=1..nops(%%))]: [seq([i+dd+4,%%[i]],i=1..nops(%%))]: [seq([i+dd+6,%%[i]],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=['`', '`', '`']),
```



```
title = `
```

```
ln(N[i])`,titlefont=[roman,15],gridlines=true
```

```
);
```

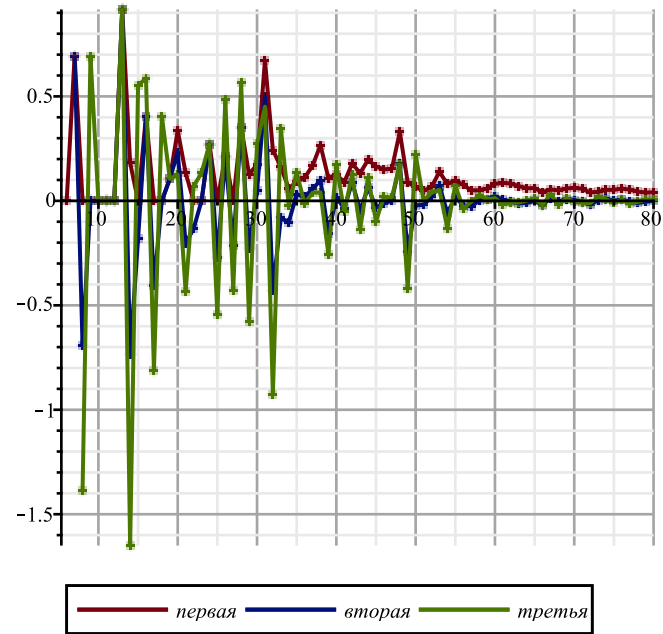
$$h := x \mapsto \ln(x)$$

```
[0, ln(2), 0, 0, 0, 0, 0, ln(5) - ln(2), ln(6) - ln(5), 0, 2 ln(3) - ln(6), 0, 0, ln(10) - 2 ln(3), ln(14) - ln(10), 4 ln(2) - ln(14), 0, 0,
ln(21) - 4 ln(2), 0, ln(26) - ln(21), 0, ln(37) - ln(26), ln(42) - ln(37), ln(50) - ln(42), ln(98) - ln(50), 3 ln(5) - ln(98),
ln(147) - 3 ln(5), ln(156) - ln(147), ln(171) - ln(156), ln(191) - ln(171), ln(226) - ln(191), ln(295) - ln(226), ln(329)
- ln(295), ln(373) - ln(329), ln(408) - ln(373), ln(488) - ln(408), ln(557) - ln(488), ln(678) - ln(557), ln(799) - ln(678),
ln(929) - ln(799), ln(1083) - ln(929), ln(1507) - ln(1083), ln(1646) - ln(1507), ln(1760) - ln(1646), ln(1846) - ln(1760),
ln(1973) - ln(1846), ln(2267) - ln(1973), ln(2458) - ln(2267), ln(2711) - ln(2458), ln(2926) - ln(2711), ln(3077) - ln(2926),
ln(3238) - ln(3077), ln(3436) - ln(3238), ln(3726) - ln(3436), ln(4062) - ln(3726), ln(4411) - ln(4062), ln(4734) - ln(4411),
ln(5029) - ln(4734), ln(5346) - ln(5029), ln(5572) - ln(5346), ln(5884) - ln(5572), ln(6190) - ln(5884), ln(6565) - ln(6190),
ln(6990) - ln(6565), ln(7404) - ln(6990), ln(7711) - ln(7404), ln(8050) - ln(7711), ln(8485) - ln(8050), ln(8945) - ln(8485),
ln(9486) - ln(8945), ln(10011) - ln(9486), ln(10462) - ln(10011), ln(10887) - ln(10462), ln(11340) - ln(10887)]
```

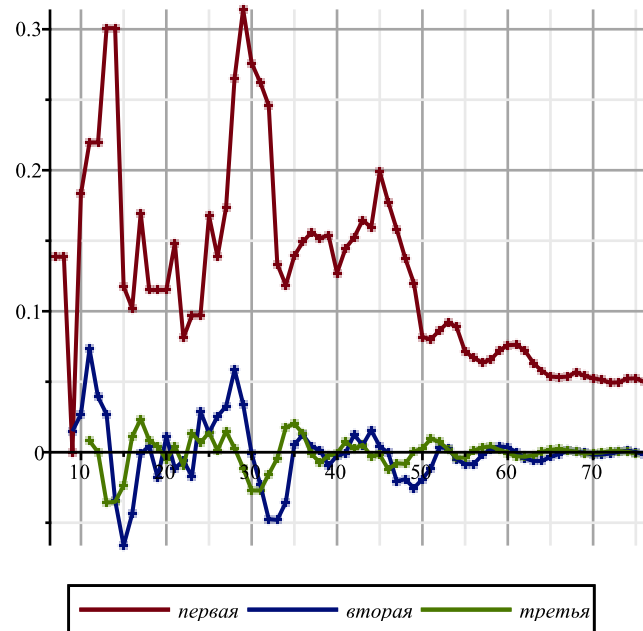
```
[ln(2), -ln(2), 0, 0, 0, 0, ln(5) - ln(2), ln(6) - 2 ln(5) + ln(2), -ln(6) + ln(5), 2 ln(3) - ln(6), -2 ln(3) + ln(6), 0, ln(10) - 2 ln(3),
ln(14) - 2 ln(10) + 2 ln(3), 4 ln(2) - 2 ln(14) + ln(10), -4 ln(2) + ln(14), 0, ln(21) - 4 ln(2), -ln(21) + 4 ln(2), ln(26)
- ln(21), -ln(26) + ln(21), ln(37) - ln(26), ln(42) - 2 ln(37) + ln(26), ln(50) - 2 ln(42) + ln(37), ln(98) - 2 ln(50) + ln(42),
3 ln(5) - 2 ln(98) + ln(50), ln(147) - 6 ln(5) + ln(98), ln(156) - 2 ln(147) + 3 ln(5), ln(171) - 2 ln(156) + ln(147), ln(191)
- 2 ln(171) + ln(156), ln(226) - 2 ln(191) + ln(171), ln(295) - 2 ln(226) + ln(191), ln(329) - 2 ln(295) + ln(226), ln(373)
- 2 ln(329) + ln(295), ln(408) - 2 ln(373) + ln(329), ln(488) - 2 ln(408) + ln(373), ln(557) - 2 ln(488) + ln(408), ln(678)
- 2 ln(557) + ln(488), ln(799) - 2 ln(678) + ln(557), ln(929) - 2 ln(799) + ln(678), ln(1083) - 2 ln(929) + ln(799), ln(1507)
- 2 ln(1083) + ln(929), ln(1646) - 2 ln(1507) + ln(1083), ln(1760) - 2 ln(1646) + ln(1507), ln(1846) - 2 ln(1760) + ln(1646),
ln(1973) - 2 ln(1846) + ln(1760), ln(2267) - 2 ln(1973) + ln(1846), ln(2458) - 2 ln(2267) + ln(1973), ln(2711) - 2 ln(2458)
+ ln(2267), ln(2926) - 2 ln(2711) + ln(2458), ln(3077) - 2 ln(2926) + ln(2711), ln(3238) - 2 ln(3077) + ln(2926), ln(3436)
- 2 ln(3238) + ln(3077), ln(3726) - 2 ln(3436) + ln(3238), ln(4062) - 2 ln(3726) + ln(3436), ln(4411) - 2 ln(4062)
+ ln(3726), ln(4734) - 2 ln(4411) + ln(4062), ln(5029) - 2 ln(4734) + ln(4411), ln(5346) - 2 ln(5029) + ln(4734), ln(5572)
- 2 ln(5346) + ln(5029), ln(5884) - 2 ln(5572) + ln(5346), ln(6190) - 2 ln(5884) + ln(5572), ln(6565) - 2 ln(6190)
+ ln(5884), ln(6990) - 2 ln(6565) + ln(6190), ln(7404) - 2 ln(6990) + ln(6565), ln(7711) - 2 ln(7404) + ln(6990), ln(8050)
- 2 ln(7711) + ln(7404), ln(8485) - 2 ln(8050) + ln(7711), ln(8945) - 2 ln(8485) + ln(8050), ln(9486) - 2 ln(8945)
+ ln(8485), ln(10011) - 2 ln(9486) + ln(8945), ln(10462) - 2 ln(10011) + ln(9486), ln(10887) - 2 ln(10462) + ln(10011),
ln(11340) - 2 ln(10887) + ln(10462)]
```

[-2 ln(2), ln(2), 0, 0, 0, ln(5) - ln(2), ln(6) - 3 ln(5) + 2 ln(2), -2 ln(6) + 3 ln(5) - ln(2), 2 ln(3) - ln(5), -4 ln(3) + 2 ln(6),
 2 ln(3) - ln(6), ln(10) - 2 ln(3), ln(14) - 3 ln(10) + 4 ln(3), 4 ln(2) - 3 ln(14) + 3 ln(10) - 2 ln(3), -8 ln(2) + 3 ln(14)
 - ln(10), 4 ln(2) - ln(14), ln(21) - 4 ln(2), -2 ln(21) + 8 ln(2), ln(26) - 4 ln(2), -2 ln(26) + 2 ln(21), ln(37) - ln(21), ln(42)
 - 3 ln(37) + 2 ln(26), ln(50) - 3 ln(42) + 3 ln(37) - ln(26), ln(98) - 3 ln(50) + 3 ln(42) - ln(37), 3 ln(5) - 3 ln(98) + 3 ln(50)
 - ln(42), ln(147) - 9 ln(5) + 3 ln(98) - ln(50), ln(156) - 3 ln(147) + 9 ln(5) - ln(98), ln(171) - 3 ln(156) + 3 ln(147)
 - 3 ln(5), ln(191) - 3 ln(171) + 3 ln(156) - ln(147), ln(226) - 3 ln(191) + 3 ln(171) - ln(156), ln(295) - 3 ln(226) + 3 ln(191)
 - ln(171), ln(329) - 3 ln(295) + 3 ln(226) - ln(191), ln(373) - 3 ln(329) + 3 ln(295) - ln(226), ln(408) - 3 ln(373) + 3 ln(329)
 - ln(295), ln(488) - 3 ln(408) + 3 ln(373) - ln(329), ln(557) - 3 ln(488) + 3 ln(408) - ln(373), ln(678) - 3 ln(557) + 3 ln(488)
 - ln(408), ln(799) - 3 ln(678) + 3 ln(557) - ln(488), ln(929) - 3 ln(799) + 3 ln(678) - ln(557), ln(1083) - 3 ln(929)
 + 3 ln(799) - ln(678), ln(1507) - 3 ln(1083) + 3 ln(929) - ln(799), ln(1646) - 3 ln(1507) + 3 ln(1083) - ln(929), ln(1760)
 - 3 ln(1646) + 3 ln(1507) - ln(1083), ln(1846) - 3 ln(1760) + 3 ln(1646) - ln(1507), ln(1973) - 3 ln(1846) + 3 ln(1760)
 - ln(1646), ln(2267) - 3 ln(1973) + 3 ln(1846) - ln(1760), ln(2458) - 3 ln(2267) + 3 ln(1973) - ln(1846), ln(2711)
 - 3 ln(2458) + 3 ln(2267) - ln(1973), ln(2926) - 3 ln(2711) + 3 ln(2458) - ln(2267), ln(3077) - 3 ln(2926) + 3 ln(2711)
 - ln(2458), ln(3238) - 3 ln(3077) + 3 ln(2926) - ln(2711), ln(3436) - 3 ln(3238) + 3 ln(3077) - ln(2926), ln(3726)
 - 3 ln(3436) + 3 ln(3238) - ln(3077), ln(4062) - 3 ln(3726) + 3 ln(3436) - ln(3238), ln(4411) - 3 ln(4062) + 3 ln(3726)
 - ln(3436), ln(4734) - 3 ln(4411) + 3 ln(4062) - ln(3726), ln(5029) - 3 ln(4734) + 3 ln(4411) - ln(4062), ln(5346)
 - 3 ln(5029) + 3 ln(4734) - ln(4411), ln(5572) - 3 ln(5346) + 3 ln(5029) - ln(4734), ln(5884) - 3 ln(5572) + 3 ln(5346)
 - ln(5029), ln(6190) - 3 ln(5884) + 3 ln(5572) - ln(5346), ln(6565) - 3 ln(6190) + 3 ln(5884) - ln(5572), ln(6990)
 - 3 ln(6565) + 3 ln(6190) - ln(5884), ln(7404) - 3 ln(6990) + 3 ln(6565) - ln(6190), ln(7711) - 3 ln(7404) + 3 ln(6990)
 - ln(6565), ln(8050) - 3 ln(7711) + 3 ln(7404) - ln(6990), ln(8485) - 3 ln(8050) + 3 ln(7711) - ln(7404), ln(8945)
 - 3 ln(8485) + 3 ln(8050) - ln(7711), ln(9486) - 3 ln(8945) + 3 ln(8485) - ln(8050), ln(10011) - 3 ln(9486) + 3 ln(8945)
 - ln(8485), ln(10462) - 3 ln(10011) + 3 ln(9486) - ln(8945), ln(10887) - 3 ln(10462) + 3 ln(10011) - ln(9486), ln(11340)
 - 3 ln(10887) + 3 ln(10462) - ln(10011)]

Разности ряда $\ln(N[i])$



Сглаженные разности ряда $\ln(N[i])$



```
> h:=x->ln(x);
```

```
[seq(h(T[i])-h(T[i-1]),i=2..nops(T)); [seq(%[i]-%[i-1],i=2..nops(%))]; [seq(%[i]-%[i-1],i=2..
nops(%))];
[seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+1,%%[i]],i=1..nops(%%))]: [seq([i+dd+1,%%[i]
],i=1..nops(%%))]:
display(
  plot([%%,%,%],style=point),
  plot([%%,%,%],legend=['`',``,'`'],
  title='` ln(N[i]) `',titlefont=[roman,15] ,gridlines=true
);
```

$$h := x \mapsto \ln(x)$$

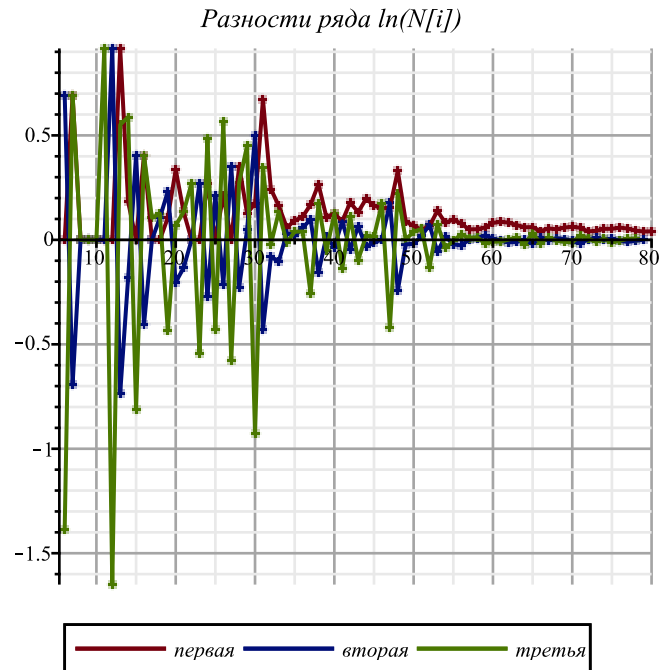
```
[0, ln(2), 0, 0, 0, 0, 0, ln(5) - ln(2), ln(6) - ln(5), 0, 2 ln(3) - ln(6), 0, 0, ln(10) - 2 ln(3), ln(14) - ln(10), 4 ln(2) - ln(14), 0, 0,
ln(21) - 4 ln(2), 0, ln(26) - ln(21), 0, ln(37) - ln(26), ln(42) - ln(37), ln(50) - ln(42), ln(98) - ln(50), 3 ln(5) - ln(98),
ln(147) - 3 ln(5), ln(156) - ln(147), ln(171) - ln(156), ln(191) - ln(171), ln(226) - ln(191), ln(295) - ln(226), ln(329)
- ln(295), ln(373) - ln(329), ln(408) - ln(373), ln(488) - ln(408), ln(557) - ln(488), ln(678) - ln(557), ln(799) - ln(678),
```

$\ln(929) - \ln(799), \ln(1083) - \ln(929), \ln(1507) - \ln(1083), \ln(1646) - \ln(1507), \ln(1760) - \ln(1646), \ln(1846) - \ln(1760),$
 $\ln(1973) - \ln(1846), \ln(2267) - \ln(1973), \ln(2458) - \ln(2267), \ln(2711) - \ln(2458), \ln(2926) - \ln(2711), \ln(3077) - \ln(2926),$
 $\ln(3238) - \ln(3077), \ln(3436) - \ln(3238), \ln(3726) - \ln(3436), \ln(4062) - \ln(3726), \ln(4411) - \ln(4062), \ln(4734) - \ln(4411),$
 $\ln(5029) - \ln(4734), \ln(5346) - \ln(5029), \ln(5572) - \ln(5346), \ln(5884) - \ln(5572), \ln(6190) - \ln(5884), \ln(6565) - \ln(6190),$
 $\ln(6990) - \ln(6565), \ln(7404) - \ln(6990), \ln(7711) - \ln(7404), \ln(8050) - \ln(7711), \ln(8485) - \ln(8050), \ln(8945) - \ln(8485),$
 $\ln(9486) - \ln(8945), \ln(10011) - \ln(9486), \ln(10462) - \ln(10011), \ln(10887) - \ln(10462), \ln(11340) - \ln(10887)]$

$[\ln(2), -\ln(2), 0, 0, 0, 0, \ln(5) - \ln(2), \ln(6) - 2 \ln(5) + \ln(2), -\ln(6) + \ln(5), 2 \ln(3) - \ln(6), -2 \ln(3) + \ln(6), 0, \ln(10) - 2 \ln(3),$
 $\ln(14) - 2 \ln(10) + 2 \ln(3), 4 \ln(2) - 2 \ln(14) + \ln(10), -4 \ln(2) + \ln(14), 0, \ln(21) - 4 \ln(2), -\ln(21) + 4 \ln(2), \ln(26)$
 $- \ln(21), -\ln(26) + \ln(21), \ln(37) - \ln(26), \ln(42) - 2 \ln(37) + \ln(26), \ln(50) - 2 \ln(42) + \ln(37), \ln(98) - 2 \ln(50) + \ln(42),$
 $3 \ln(5) - 2 \ln(98) + \ln(50), \ln(147) - 6 \ln(5) + \ln(98), \ln(156) - 2 \ln(147) + 3 \ln(5), \ln(171) - 2 \ln(156) + \ln(147), \ln(191)$
 $- 2 \ln(171) + \ln(156), \ln(226) - 2 \ln(191) + \ln(171), \ln(295) - 2 \ln(226) + \ln(191), \ln(329) - 2 \ln(295) + \ln(226), \ln(373)$
 $- 2 \ln(329) + \ln(295), \ln(408) - 2 \ln(373) + \ln(329), \ln(488) - 2 \ln(408) + \ln(373), \ln(557) - 2 \ln(488) + \ln(408), \ln(678)$
 $- 2 \ln(557) + \ln(488), \ln(799) - 2 \ln(678) + \ln(557), \ln(929) - 2 \ln(799) + \ln(678), \ln(1083) - 2 \ln(929) + \ln(799), \ln(1507)$
 $- 2 \ln(1083) + \ln(929), \ln(1646) - 2 \ln(1507) + \ln(1083), \ln(1760) - 2 \ln(1646) + \ln(1507), \ln(1846) - 2 \ln(1760) + \ln(1646),$
 $\ln(1973) - 2 \ln(1846) + \ln(1760), \ln(2267) - 2 \ln(1973) + \ln(1846), \ln(2458) - 2 \ln(2267) + \ln(1973), \ln(2711) - 2 \ln(2458)$
 $+ \ln(2267), \ln(2926) - 2 \ln(2711) + \ln(2458), \ln(3077) - 2 \ln(2926) + \ln(2711), \ln(3238) - 2 \ln(3077) + \ln(2926), \ln(3436)$
 $- 2 \ln(3238) + \ln(3077), \ln(3726) - 2 \ln(3436) + \ln(3238), \ln(4062) - 2 \ln(3726) + \ln(3436), \ln(4411) - 2 \ln(4062)$
 $+ \ln(3726), \ln(4734) - 2 \ln(4411) + \ln(4062), \ln(5029) - 2 \ln(4734) + \ln(4411), \ln(5346) - 2 \ln(5029) + \ln(4734), \ln(5572)$
 $- 2 \ln(5346) + \ln(5029), \ln(5884) - 2 \ln(5572) + \ln(5346), \ln(6190) - 2 \ln(5884) + \ln(5572), \ln(6565) - 2 \ln(6190)$
 $+ \ln(5884), \ln(6990) - 2 \ln(6565) + \ln(6190), \ln(7404) - 2 \ln(6990) + \ln(6565), \ln(7711) - 2 \ln(7404) + \ln(6990), \ln(8050)$
 $- 2 \ln(7711) + \ln(7404), \ln(8485) - 2 \ln(8050) + \ln(7711), \ln(8945) - 2 \ln(8485) + \ln(8050), \ln(9486) - 2 \ln(8945)$
 $+ \ln(8485), \ln(10011) - 2 \ln(9486) + \ln(8945), \ln(10462) - 2 \ln(10011) + \ln(9486), \ln(10887) - 2 \ln(10462) + \ln(10011),$
 $\ln(11340) - 2 \ln(10887) + \ln(10462)]$

$[-2 \ln(2), \ln(2), 0, 0, 0, \ln(5) - \ln(2), \ln(6) - 3 \ln(5) + 2 \ln(2), -2 \ln(6) + 3 \ln(5) - \ln(2), 2 \ln(3) - \ln(5), -4 \ln(3) + 2 \ln(6),$
 $2 \ln(3) - \ln(6), \ln(10) - 2 \ln(3), \ln(14) - 3 \ln(10) + 4 \ln(3), 4 \ln(2) - 3 \ln(14) + 3 \ln(10) - 2 \ln(3), -8 \ln(2) + 3 \ln(14)$
 $- \ln(10), 4 \ln(2) - \ln(14), \ln(21) - 4 \ln(2), -2 \ln(21) + 8 \ln(2), \ln(26) - 4 \ln(2), -2 \ln(26) + 2 \ln(21), \ln(37) - \ln(21), \ln(42)$
 $- 3 \ln(37) + 2 \ln(26), \ln(50) - 3 \ln(42) + 3 \ln(37) - \ln(26), \ln(98) - 3 \ln(50) + 3 \ln(42) - \ln(37), 3 \ln(5) - 3 \ln(98) + 3 \ln(50)$
 $- \ln(42), \ln(147) - 9 \ln(5) + 3 \ln(98) - \ln(50), \ln(156) - 3 \ln(147) + 9 \ln(5) - \ln(98), \ln(171) - 3 \ln(156) + 3 \ln(147)$
 $- 3 \ln(5), \ln(191) - 3 \ln(171) + 3 \ln(156) - \ln(147), \ln(226) - 3 \ln(191) + 3 \ln(171) - \ln(156), \ln(295) - 3 \ln(226) + 3 \ln(191)$
 $- \ln(171), \ln(329) - 3 \ln(295) + 3 \ln(226) - \ln(191), \ln(373) - 3 \ln(329) + 3 \ln(295) - \ln(226), \ln(408) - 3 \ln(373) + 3 \ln(329)$

$-\ln(295), \ln(488) - 3 \ln(408) + 3 \ln(373) - \ln(329), \ln(557) - 3 \ln(488) + 3 \ln(408) - \ln(373), \ln(678) - 3 \ln(557) + 3 \ln(488)$
 $-\ln(408), \ln(799) - 3 \ln(678) + 3 \ln(557) - \ln(488), \ln(929) - 3 \ln(799) + 3 \ln(678) - \ln(557), \ln(1083) - 3 \ln(929)$
 $+ 3 \ln(799) - \ln(678), \ln(1507) - 3 \ln(1083) + 3 \ln(929) - \ln(799), \ln(1646) - 3 \ln(1507) + 3 \ln(1083) - \ln(929), \ln(1760)$
 $- 3 \ln(1646) + 3 \ln(1507) - \ln(1083), \ln(1846) - 3 \ln(1760) + 3 \ln(1646) - \ln(1507), \ln(1973) - 3 \ln(1846) + 3 \ln(1760)$
 $-\ln(1646), \ln(2267) - 3 \ln(1973) + 3 \ln(1846) - \ln(1760), \ln(2458) - 3 \ln(2267) + 3 \ln(1973) - \ln(1846), \ln(2711)$
 $- 3 \ln(2458) + 3 \ln(2267) - \ln(1973), \ln(2926) - 3 \ln(2711) + 3 \ln(2458) - \ln(2267), \ln(3077) - 3 \ln(2926) + 3 \ln(2711)$
 $-\ln(2458), \ln(3238) - 3 \ln(3077) + 3 \ln(2926) - \ln(2711), \ln(3436) - 3 \ln(3238) + 3 \ln(3077) - \ln(2926), \ln(3726)$
 $- 3 \ln(3436) + 3 \ln(3238) - \ln(3077), \ln(4062) - 3 \ln(3726) + 3 \ln(3436) - \ln(3238), \ln(4411) - 3 \ln(4062) + 3 \ln(3726)$
 $-\ln(3436), \ln(4734) - 3 \ln(4411) + 3 \ln(4062) - \ln(3726), \ln(5029) - 3 \ln(4734) + 3 \ln(4411) - \ln(4062), \ln(5346)$
 $- 3 \ln(5029) + 3 \ln(4734) - \ln(4411), \ln(5572) - 3 \ln(5346) + 3 \ln(5029) - \ln(4734), \ln(5884) - 3 \ln(5572) + 3 \ln(5346)$
 $-\ln(5029), \ln(6190) - 3 \ln(5884) + 3 \ln(5572) - \ln(5346), \ln(6565) - 3 \ln(6190) + 3 \ln(5884) - \ln(5572), \ln(6990)$
 $- 3 \ln(6565) + 3 \ln(6190) - \ln(5884), \ln(7404) - 3 \ln(6990) + 3 \ln(6565) - \ln(6190), \ln(7711) - 3 \ln(7404) + 3 \ln(6990)$
 $-\ln(6565), \ln(8050) - 3 \ln(7711) + 3 \ln(7404) - \ln(6990), \ln(8485) - 3 \ln(8050) + 3 \ln(7711) - \ln(7404), \ln(8945)$
 $- 3 \ln(8485) + 3 \ln(8050) - \ln(7711), \ln(9486) - 3 \ln(8945) + 3 \ln(8485) - \ln(8050), \ln(10011) - 3 \ln(9486) + 3 \ln(8945)$
 $-\ln(8485), \ln(10462) - 3 \ln(10011) + 3 \ln(9486) - \ln(8945), \ln(10887) - 3 \ln(10462) + 3 \ln(10011) - \ln(9486), \ln(11340)$
 $- 3 \ln(10887) + 3 \ln(10462) - \ln(10011)]$



```
> n:=1: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);
```

```
fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:
```

```
` `; `Approximation of the infection schedule by the solution of the Verhulst equation`; ` `;
```

```
M:=goldMin(fM,max(T)+2..max(T)*2,1);
```

```
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t): Chi2:=chi2(T,%%);
```

```
cat(`Next day forecast: ` ,round(f(nops(T)+1)));
```

```
cat(`The level of 0.5 M is reached at ` ,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31), ` apr`);
```

```
cat(`The level of 0.85 M is reached at ` ,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31), ` apr`);
```

```
` `; `Approximation of the infection schedule by solving the Malthus equation`; ` `;
```

```
nue:=F(T,chi2e,f_): fe:=unapply(ff(%(t)),t): N(t)=%(t);
```

```
simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]: [coeff(%[1],d,i) $ i=0..n-1];
```

```
plot(%%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[` ` ,` `],
```

```
linestyle=[solid,dash],title=` ` ,titlefont=[roman,20],labels=[t,alpha(t)],
```

```
gridlines=true);
```

```
d1:=fsolve(f(d)=0.5*M,d=30)+dd; K_:=M; alpha_:=coeff(nu(t),t,1);
```

```

n:=4: ne:=n: 'f(t)'=Sum(a[j]*t^j,j=0..n);

fM:=proc(x) global M,chi2,F,T,f_; M:=x; chi2(T,F(T,chi2,f_)); end:

``; `Approximation of the infection schedule by the solution of the Verhulst equation`; ``;
M:=goldMin(fM,max(T)+2..max(T)*2,1);
nu:=F(T,chi2,f_): f:=unapply(ff(%(t)),t): N(t)=%(t); Chi2:=chi2(T,%%);
cat(`Next day forecast:`,round(f(nops(T)+1)));
cat(`The level of 0.5 M is reached at`,round(1+fsolve(f(d)=0.5*M,d=30)+dd-31),` apr`);
cat(`The level of 0.85 M is reached at`,round(1+fsolve(f(d)=0.85*M,d=30)+dd-31),` apr`);
``; `Approximation of the infection schedule by solving the Malthus equation`; ``;
nue:=F(T,chi2e,f_): fe:=unapply(fffe(%(t)),t): N(t)=%(t);

[seq([i,(
(T[i-dd]-T[i-dd-1])/(T2[i-dd]+T2[i-dd-1])/((1-T[i-dd]/M)+(1-T[i-dd-1]/M))
)*4],i=1+dd+1..nops(T)+dd): [seq([%[i][1],(%[i-1][2]+[%i][2]+[%i+1][2])/3],i=2..nops(%)-1)]:
Palpha:=display(plot([%],color=blue),plot([%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):

simplify([diff(nu(d-dd),d),diff(nue(d-dd),d)]): [coeff(%[1],d,i) $ i=0..n-1];
plot(%%,d=1+dd..nops(T)+dd,view=[0..nops(T)+dd,0..0.5],legend=[``,``],
linestyle=[solid,dash],title=`,titlefont=[roman,20],labels=[t,alpha(t)],
gridlines=true):

display(Palpha,%);

```

$$f(t) = \sum_{j=0}^1 a_j t^j$$

Approximation of the infection schedule by the solution of the Verhulst equation

$$M := 11342.37476$$

$$N(t) = 11342.37476 - \frac{11342.37476}{e^{0.1273592714t - 7.801871537} + 1}$$

$Chi2 := 1398.499948$

Next day forecast: 9996

The level of 0.5 M is reached at 35 apr

The level of 0.85 M is reached at 49 apr

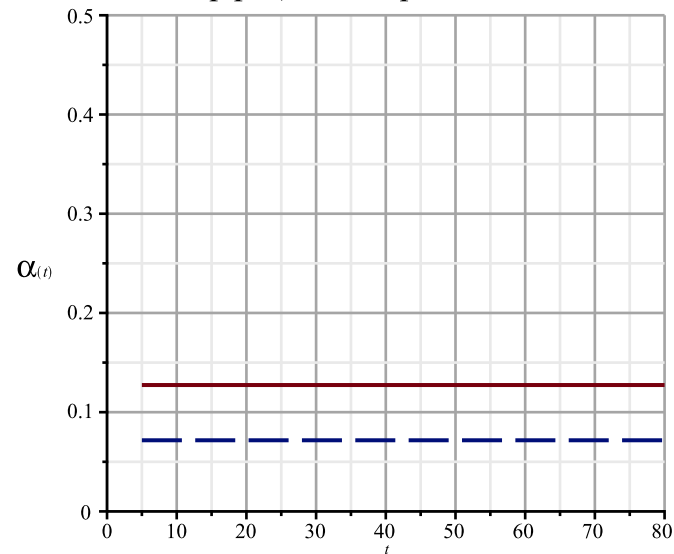
``

Approximation of the infection schedule by solving the Malthus equation

``

$$N(t) = e^{0.07168670941 t + 4.061147549} [0.1273592714]$$

Коэффициент заражения



Ферхольст Мальтус

$dI := 65.25876390$

$K_ := 11342.37476$

$alpha_ := 0.1273592714$

$$f(t) = \sum_{j=0}^4 a_j t^j$$

Approximation of the infection schedule by the solution of the Verhulst equation

$$N(t) = 14237.28217 - \frac{14237.28217}{e^{1.429013308 \cdot 10^{-6} t^4 - 0.0002431249094 t^3 + 0.01313835729 t^2 - 0.09599565753 t - 8.167476882} + 1}$$

$$Chi2 := 212.2370327$$

Next day forecast: 11801

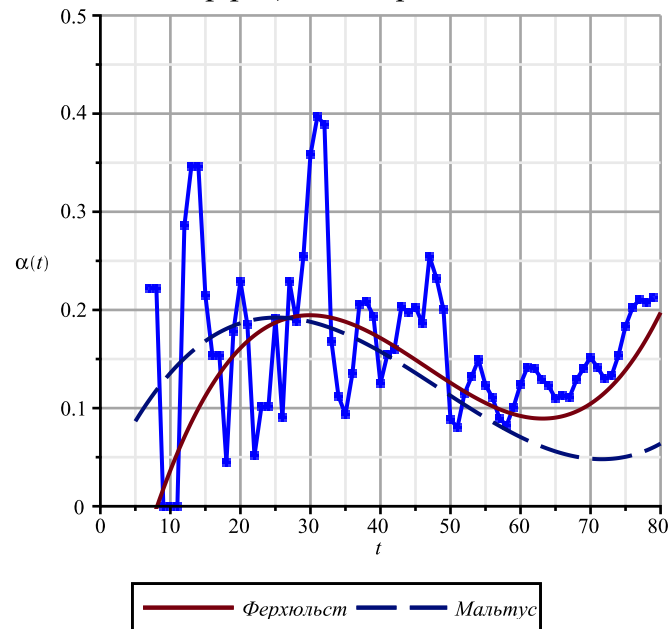
The level of 0.5 M is reached at 41 apr

The level of 0.85 M is reached at 52 apr

Approximation of the infection schedule by solving the Malthus equation

$$N(t) = e^{7.215877955 \cdot 10^{-7} t^4 - 0.0001281422841 t^3 + 0.006201697490 t^2 + 0.07457631737 t + 0.05598033495} [-0.213138338900000, 0.0323860829700000, -0.000797967367000000, 5.716053232 \cdot 10^{-6}]$$

Коэффициент заражения



```
> df:=unapply(diff(f(i),i),i): ddf:=unapply(diff(f(i),i,i),i):

display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(90,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(90,dd+nops(T))),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..80,1..M*1.1],labels=[t,N(t)],gridlines=true
);

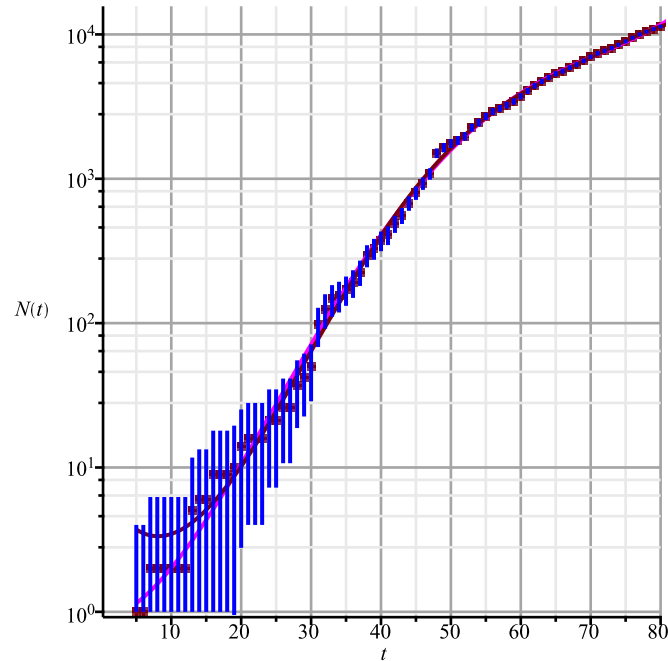
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(120,dd+nops(T))),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  axis[2]=[mode=log],
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);
```

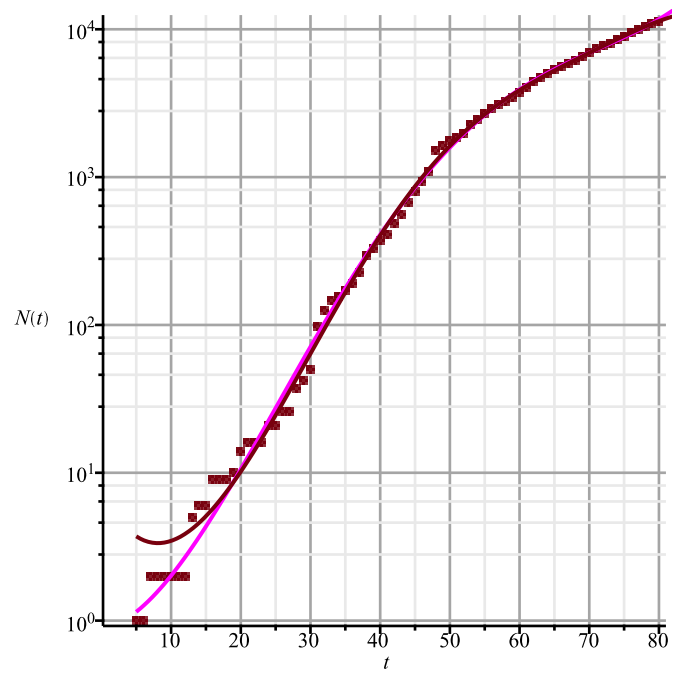
```

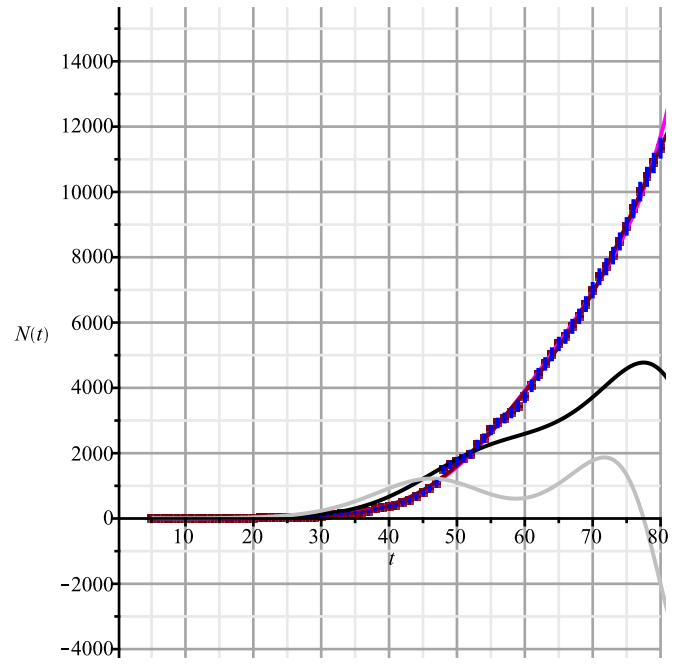
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=10,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),90)),
  plot(10*df(i-dd),i=1+dd..max(dd+nops(T),120),color=black),
  plot(100*ddf(i-dd),i=1+dd..max(dd+nops(T),120),color=gray),
  seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..80,-M*0.3..M*1.1],labels=[t,N(t)],gridlines=true
);

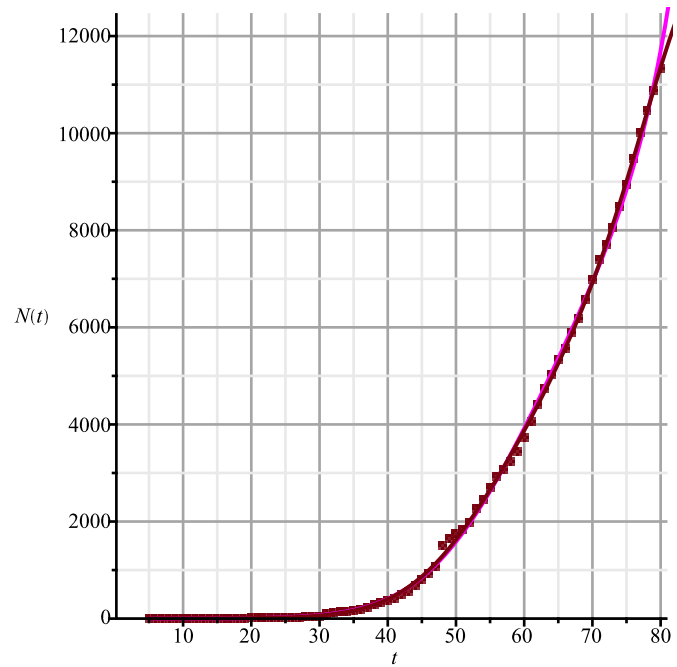
display(
  plot([[i+dd,T[i]] $ i=1..nops(T)],style=point,symbolsize=8,symbol=solidcircle),
  plot(fe(i-dd),i=1+dd..max(120,dd+nops(T)),color=magenta),
  plot(f(i-dd),i=1+dd..max(dd+nops(T),120)),
  # seq(plot([[i+dd,T[i]+3*sqrt(T[i])],[i+dd,T[i]-3*sqrt(T[i])]],color=blue),i=1..nops(T)),
  view=[1..nops(T)+dd+1,1..T[nops(T)]*1.1],labels=[t,N(t)],gridlines=true
);

```

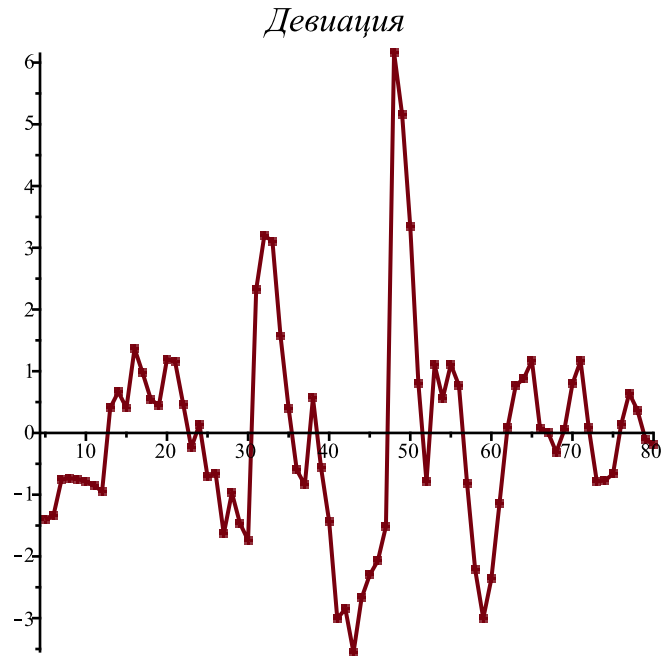








```
> dT:=[i, (T[i-dd]-f(i-dd))/sigma(f(i-dd))] $ i=1+dd..dd+nops(T)]:
display( plot(%), plot(% ,style=point,symbolsize=8,symbol=solidcircle),title = ` ` ,titlefont=
[roman,20] );
```



```

> ===== ` ;
`FORECAST ` ;
===== ` ;

=====
FORECAST
=====

> proc3:=proc (E)
  E[1]*convert (map (X->X^coeff (E[2] ,X,1) ,M) , `*` ) ;
end:

proc2:=proc (X,E)
  proc3 (E) * (coeff (E[3] ,X,1) -coeff (E[2] ,X,1)) ;
end:

proc1:=proc (X)
  convert (map (E->proc2 (X,E) ,L) , `+` ) ;
end:

```



```

> A:='A': B:='B': C:='C': M:=[A,B,C];

L:=
 [P[`01`],0,A],
 [(B/K)*P[`12`],A,B],
 [P[`23`],B,C],
 [P[`10`],A,0], [P[`20`],B,0], [P[`30`],C,0]
]: Matrix(%);

eqs:=map(X->Diff(X,t)=procl(X),M); Vector(%);

```

$$M := [A, B, C]$$

$$\begin{bmatrix} P_{01} & 0 & A \\ \frac{BP_{12}}{K} & A & B \\ P_{23} & B & C \\ P_{10} & A & 0 \\ P_{20} & B & 0 \\ P_{30} & C & 0 \end{bmatrix}$$

$$eqs := \left[\frac{\partial}{\partial t} A = P_{01} - \frac{BP_{12}A}{K} - P_{10}A, \frac{\partial}{\partial t} B = \frac{BP_{12}A}{K} - P_{23}B - P_{20}B, \frac{\partial}{\partial t} C = P_{23}B - P_{30}C \right]$$

$$\begin{bmatrix} \frac{\partial}{\partial t} A = P_{01} - \frac{BP_{12}A}{K} - P_{10}A \\ \frac{\partial}{\partial t} B = \frac{BP_{12}A}{K} - P_{23}B - P_{20}B \\ \frac{\partial}{\partial t} C = P_{23}B - P_{30}C \end{bmatrix}$$

```

> v:=M; alpha:='alpha': K:=k0; tA:=[1,15,35,50,58,62,73,nops(T)+dd]; kA:=['k1x||i' $ i=1..nops(tA)]
;

par:=[d0,k0,op(kA),k2a,k2b,k3];

param:=[
  P[`01`] = 0, P[`12`] = alpha(t,op(kA)), P[`23`] = beta(t,k2a,k2b),
  P[`10`] = 0, P[`20`] = k3
];

init:=[ A(-d0)=K, B(-d0)=1, C(-d0)=0 ];

```

$$\begin{aligned}
 v &:= [A, B, C] \\
 K &:= k0 \\
 tA &:= [1, 15, 35, 50, 58, 62, 73, 80] \\
 kA &:= [k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8] \\
 par &:= [d0, k0, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8, k2a, k2b, k3] \\
 param &:= [P_{01} = 0, P_{12} = \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8), P_{23} = \beta(t, k2a, k2b), P_{10} = 0, P_{20} = k3] \\
 init &:= [A(-d0) = k0, B(-d0) = 1, C(-d0) = 0]
 \end{aligned}$$

(7)

```

> res:=solve(map(rhs,eqs[1..2]),v[1..2]); res:=res[2]: subs(P[`30`]=P[`10`],param,res);

J:=Matrix(subs(res,map(q->grad(rhs(q),v[1..2]),eqs[1..2]))); evalm(%-lambda): collect(Determinant
(%),lambda);

subs(P[`30`]=P[`10`],pr(param),%); solve(%,{lambda});

```

$$\begin{aligned}
 res &:= \left[\left[A = \frac{P_{01}}{P_{10}}, B = 0 \right], \left[A = \frac{k0(P_{23} + P_{20})}{P_{12}}, B = -\frac{k0P_{10}P_{20} + k0P_{10}P_{23} - P_{01}P_{12}}{P_{12}(P_{23} + P_{20})} \right] \right] \\
 &\quad \left[A = \frac{k0(\beta(t, k2a, k2b) + k3)}{\alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8)}, B = 0 \right]
 \end{aligned}$$

$$J := \begin{bmatrix} \frac{k0 P_{10} P_{20} + k0 P_{10} P_{23} - P_{01} P_{12}}{(P_{23} + P_{20}) k0} & -P_{10} & -P_{23} & -P_{20} \\ -\frac{k0 P_{10} P_{20} + k0 P_{10} P_{23} - P_{01} P_{12}}{(P_{23} + P_{20}) k0} & & & 0 \end{bmatrix}$$

$$\frac{(k0 P_{20} + k0 P_{23}) \lambda^2}{(P_{23} + P_{20}) k0} + \frac{P_{01} P_{12} \lambda}{(P_{23} + P_{20}) k0} + \frac{-k0 P_{10} P_{20}^2 - 2 k0 P_{10} P_{20} P_{23} - k0 P_{10} P_{23}^2 + P_{01} P_{12} P_{20} + P_{01} P_{12} P_{23}}{(P_{23} + P_{20}) k0}$$

$$[P_{01} = 0, P_{12} = \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8), P_{23} = \beta(t, k2a, k2b), P_{10} = 0, P_{20} = k3]$$

$$\frac{(k0 k3 + k0 \beta(t, k2a, k2b)) \lambda^2}{(\beta(t, k2a, k2b) + k3) k0}$$

$$\{\lambda = 0\}, \{\lambda = 0\}$$

(8)

```
> Eqs:=subs(map(q->q=q(t),v),Diff=diff,P[`30`]=P[`10`],param,eqs); #dsolve(%);
```

$$Eqs := \left[\frac{d}{dt} A(t) = -\frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0}, \frac{d}{dt} B(t) \right]$$

(9)

$$= \frac{B(t) \alpha(t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) A(t)}{k0} - \beta(t, k2a, k2b) B(t) - k3 B(t), \frac{d}{dt} C(t) = \beta(t, k2a, k2b) B(t)$$

```
> N:='N': A:='A': B:='B': C:='C': val:=valp:
```

```
#alpha:=unapply(simplify(evalf(piecewise(t<tA[1],kA[1],t<tA[2],Lag(t,tA[1..3],kA[1..3]),
# seq(op([t<tA[i+1],(Lag(t,tA[i-1..i+1],kA[i-1..i+1])+Lag(t,tA[i..i+2],kA[i..i+2]))/2]),i=2..nops
(kA)-2),
#t<tA[nops(tA)],Lag(t,tA[nops(tA)-2..nops(tA)],kA[nops(kA)-2..nops(kA)]),
#kA[nops(kA)]))) , t, op(kA));
```

```
alpha:=unapply(simplify(evalf(piecewise(t<tA[1],kA[1],t<tA[3],Lag(t,tA[1..4],kA[1..4]),
seq(op([t<tA[i+1],Lag(t,tA[i-1..i+2],kA[i-1..i+2])]),i=3..nops(kA)-3),
t<tA[nops(tA)],Lag(t,tA[nops(tA)-3..nops(tA)],kA[nops(kA)-3..nops(kA)]),
kA[nops(kA)]))) , t, op(kA));
```

```
beta:=(t,k2a,k2b)->piecewise(t<69,k2a,k2b);
```

```

EQS:=[op(Eqs),op(init)]:

res:=dsolve(EQS,numeric,map(q->q(t),v),output=listprocedure,parameters=par); assign('v[i]=subs
(res,v[i](t))' $ i=1..nops(v)):

chi2a:='chi2a': chi2:=unapply(chi2a(x0,xx,kA,x2a,x2b,x3),x0,xx,op(kA),x2a,x2b,x3):

chi2a:=proc(x0,xx,x1,x2a,x2b,x3) local i; global K; K:=xx;
  res(parameters=[corr(par,[x0,xx,op(x1),x2a,x2b,x3])]):
  sum((T[i]-K-A(i+dd))^2/(K-A(i+dd)),i=1..nops(T))+
  sum((T2[i]-B(i+dd))^2/B(i+dd),i=1..nops(T2))+
  sum((T1[i]-C(i+dd))^2/C(i+dd),i=1..nops(T1));
end:

chi2(op(pr(val))); val:=findMin(chi2,val); chi2(op(%));

#plot(map(q->q(t),v),t=0..3.0e4,legend=['`', '`', '`'],
#linestyle=[solid,dash,dashdot],gridlines=true);

writedata(cat(Region,`3c.txt`),val);

display(
  plot(map(q->q(t),v),t=0..300,legend=['`', '`', '`'],
  linestyle=[solid,dash,dashdot],gridlines=true),
  plot([[seq([i+dd,K-T[i]],i=1..nops(T))]],style=point,symbolsize=7,symbol=asterisk),
  plot([[seq([i+dd,T1[i]],i=1..nops(T1))]],style=point,symbolsize=7,symbol=circle),
  plot([[seq([i+dd,T2[i]],i=1..nops(T2))]],style=point,symbolsize=7,symbol=diamond,color=black),
  size=[1000,400],legendstyle=[font=[roman,15]]
): fdisplay(cat(Region,`3c`),%);

```

$$\alpha := (t, k1x1, k1x2, k1x3, k1x4, k1x5, k1x6, k1x7, k1x8) \mapsto \left\{ \begin{array}{l} (-0.00004287429258 \cdot k1x1 + 0.0001020408163 \cdot k1x2 - 0.00009803921574 \cdot k1x3 + 0.00009803921574 \cdot k1x4 - 0.00009803921574 \cdot k1x5 + 0.00009803921574 \cdot k1x6 - 0.00009803921574 \cdot k1x7 + 0.00009803921574 \cdot k1x8) \\ (-0.00003322259134 \cdot k1x2 + 0.0001449275363 \cdot k1x3 - 0.0002380952381 \cdot k1x4 + 0.0002380952381 \cdot k1x5 - 0.0002380952381 \cdot k1x6 + 0.0002380952381 \cdot k1x7 - 0.0002380952381 \cdot k1x8) \\ (-0.0001073537306 \cdot k1x3 + 0.0006944444445 \cdot k1x4 - 0.001358695652 \cdot k1x5 + 0.001358695652 \cdot k1x6 - 0.001358695652 \cdot k1x7 + 0.001358695652 \cdot k1x8) \\ (-0.0004528985509 \cdot k1x4 + 0.002083333333 \cdot k1x5 - 0.001893939394 \cdot k1x6 + 0.001893939394 \cdot k1x7 - 0.001893939394 \cdot k1x8) \\ (-0.0007575757577 \cdot k1x5 + 0.001262626263 \cdot k1x6 - 0.0008658008661 \cdot k1x7 + 0.0008658008661 \cdot k1x8) \end{array} \right.$$

$$\beta := (t, k2a, k2b) \mapsto \begin{cases} k2a & t < 69 \\ k2b & \text{otherwise} \end{cases}$$

res := [t = **proc**(t) ... **end proc**, A(t) = **proc**(t) ... **end proc**, B(t) = **proc**(t) ... **end proc**, C(t) = **proc**(t) ... **end proc**]
 [11.34559215, 14531.33433, 0.07651405402, 0.1357064959, 0.2088665537, 0.1529316885, 0.1062966889, 0.1061385194, 0.1591816715,
 0.2012023713, 0.02219897076, 0.01230862757, 0.00009541581785]

743.349780566288

743.349780566288

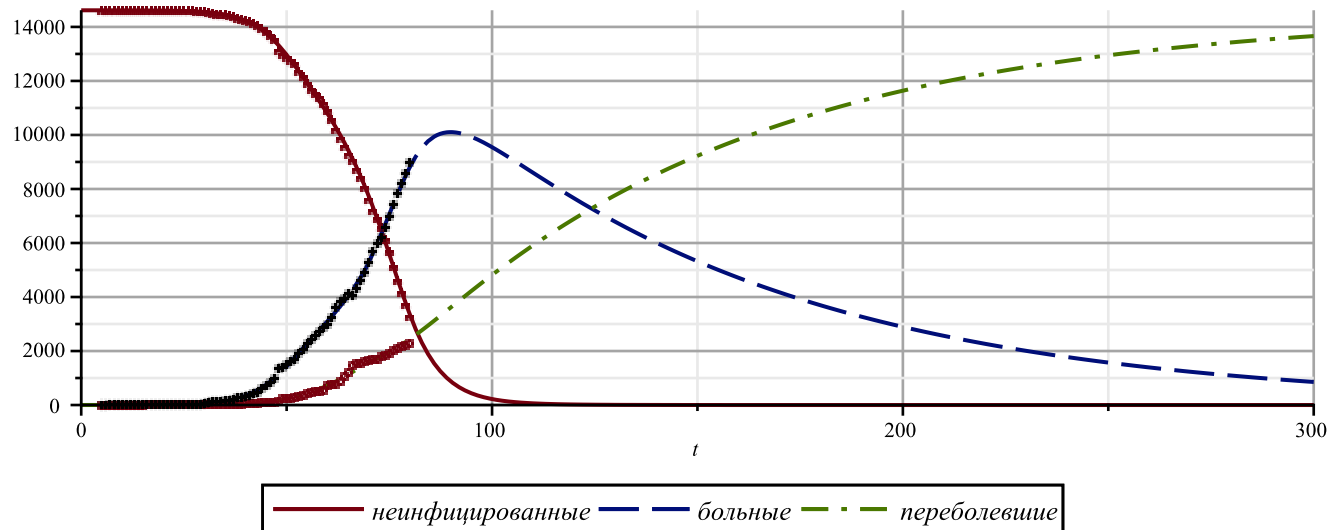
742.177551494445

741.274962353396

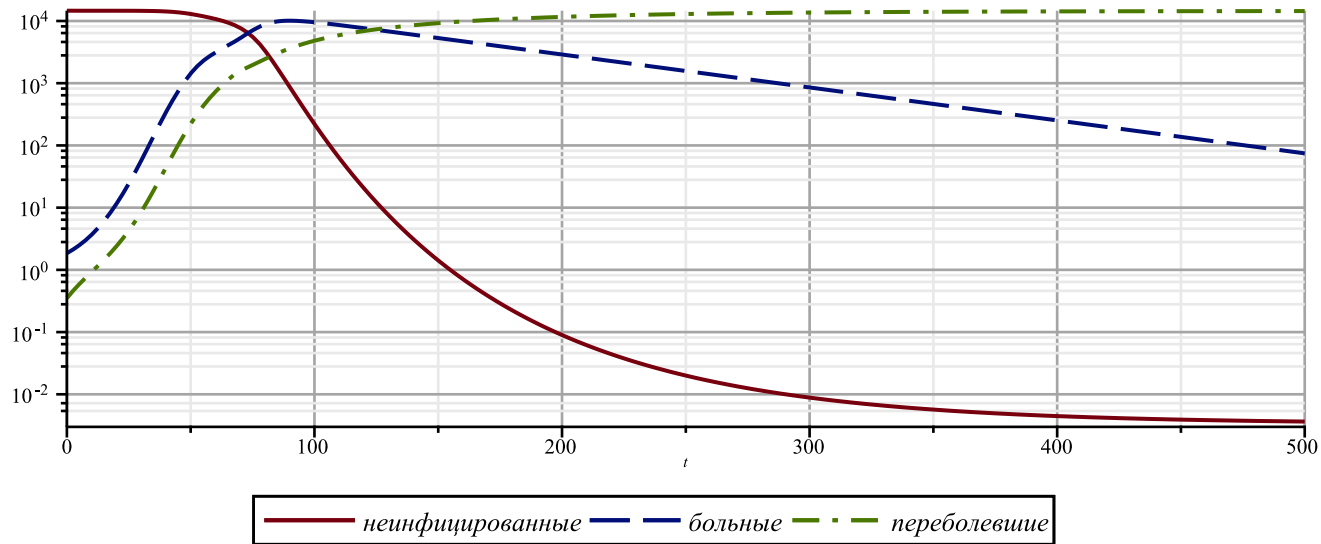
740.414525099945
739.660148789923
735.689479004759
732.642623549470
732.595851000334

```
val := [11.3587206604216, 14617.2131685064, 0.0765903056909774, 0.136357628568500, 0.208270932909720, 0.152801373545001,  
0.106458216711037, 0.106407573025571, 0.157368001654036, 0.202490835571148, 0.0223078797676930, 0.0120993811440648,  
0.0000955363750265005]
```

732.595851000334
SPB3c.jpg



```
> logplot(map(q->q(t),v), t=0..500, legend=[` ` , ` ` , ` ` ],  
linestyle=[solid,dash,dashdot],gridlines=true,size=[1000,400],legendstyle=[font=[roman,15]]);
```

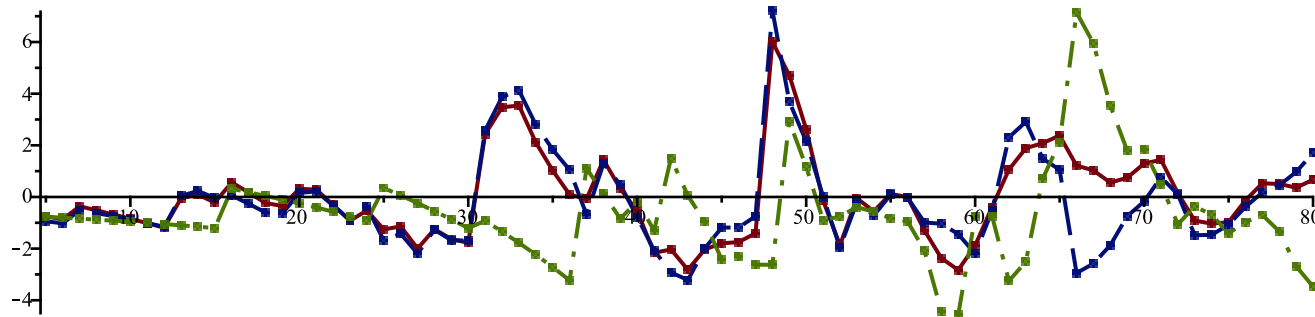


```

> display(
  plot([
    [[i, (T[i-dd]-(K -A(i)))/sigma(K -A(i))] $ i=1+dd..dd+nops(T)],
    [[i, (T2[i-dd]-(\bar{B}(i)))/sigma(B(i))) $ i=1+dd..dd+nops(T)],
    [[i, (T1[i-dd]-(C(i)))/sigma(C(i))] $ i=1+dd..dd+nops(T)]
  ], linestyle=[solid,dash,dashdot], legend = [ '\`', '\`', '\`' ]
),
  plot([
    [[i, (T[i-dd]-(K -A(i)))/sigma(K -A(i))] $ i=1+dd..dd+nops(T)],
    [[i, (T2[i-dd]-(\bar{B}(i)))/sigma(B(i))) $ i=1+dd..dd+nops(T)],
    [[i, (T1[i-dd]-(C(i)))/sigma(C(i))] $ i=1+dd..dd+nops(T)]
  ], style=point, symbolsize=8, symbol=solidcircle),
  size=[1000,300], legendstyle=[font=[roman,15]]
): fdisplay(cat(Region, `3c-dev`), %);

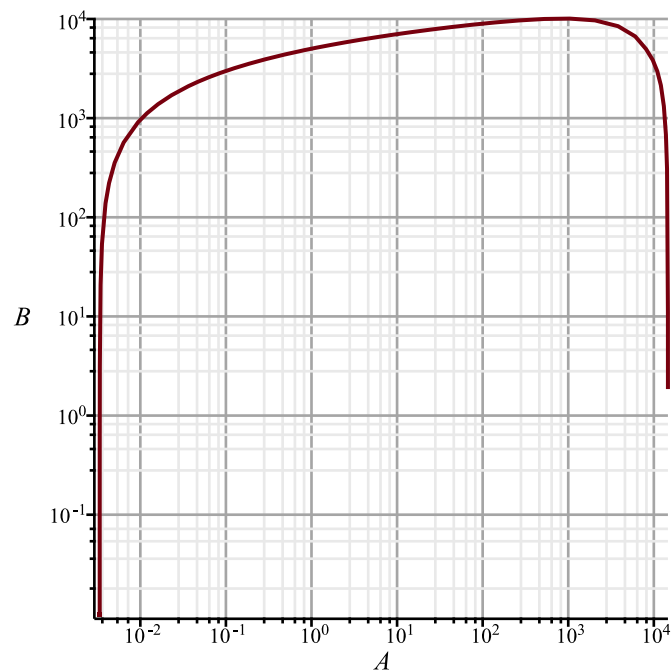
```

[SPB3c-dev.jpg](#)



— неинфицированные — больные - - - переболевшие

```
> plot([v[1](t),v[2](t),t=0..3.0e4],axis[1]=[mode=log],axis[2]=[mode=log],labels=[v[1],v[2]],
labelfont=[roman,15],gridlines=true);
```



```
> [seq([i,(
(T[i-dd]-T[i-dd-1]) / (T2[i-dd]+T2[i-dd-1]) / ((1-T[i-dd]/K)+(1-T[i-dd-1]/K))
)*4,i=1+dd+1..nops(T)+dd)]: [seq([%[i][1],(%[i-1][2]+[%i][2]+[%i+1][2])/3],i=2..nops(%)-1)]:
```



```

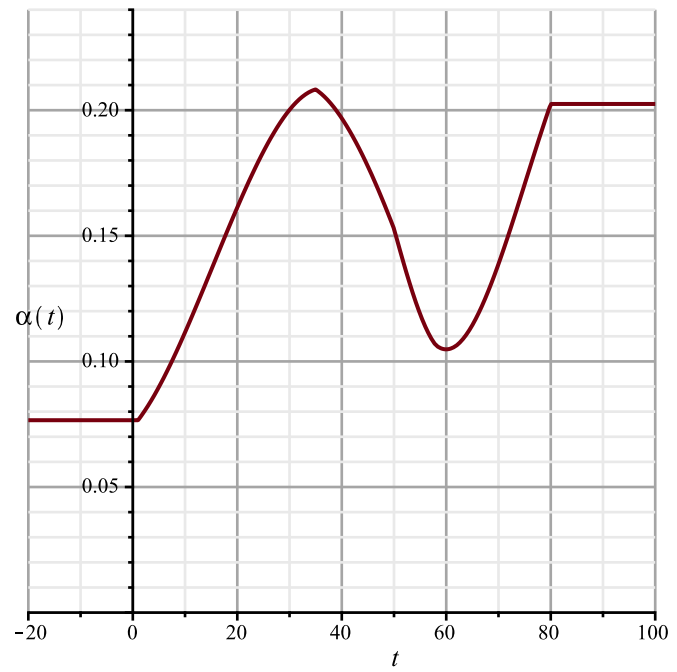
Palpha:=display(plot([%],color=blue),plot([%],style=point,symbolsize=8,symbol=solidcircle,color=
blue)):
#display(% ,gridlines=true,labels=['t','alpha(t)'],labelfont=[roman,15],view=[0..nops(T)+dd,0.
.0.9]);

subs(corr(par,val),alpha(t,op(kA)));
plot(% ,t=-20..100,gridlines=true,labels=['t','alpha(t)'],labelfont=[roman,15],view=[-20..100,0.
.0.24]):
fdisplay(cat(Region,`3c-zar`),%); display([Palpha,%],title=` ` ,titlefont=
[roman,20]);

```

$$\left\{ \begin{array}{ll}
 0.0765903056909774 & t < 1. \\
 -3.84862964920808 \cdot 10^{-6} t^3 + 0.000176473367889358 t^2 + 0.00237304036491047 t + 0.0740446405199615 & t < 35. \\
 2.72804522693861 \cdot 10^{-6} t^3 - 0.000481194116053977 t^2 + 0.0222674817334916 t - 0.0985930738544079 & t < 50. \\
 0.0000212136959903423 t^3 - 0.00312464218931587 t^2 + 0.145751629362511 t - 1.97488663036761 & t < 58. \\
 -7.47786945863886 \cdot 10^{-6} t^3 + 0.00175292393704114 t^2 - 0.129572632868148 t + 3.18385683017360 & t < 62. \\
 -9.49787804158353 \cdot 10^{-6} t^3 + 0.00214278561098058 t^2 - 0.154531859766153 t + 3.71412527026160 & t < 80. \\
 0.202490835571148 & 80. \leq t
 \end{array} \right.$$

SPB3c-zar.jpg



Коэффициент заражения

