УДК 539.142/144

MICROSCOPIC DESCRIPTION OF LOW-LYING STATES IN DEFORMED NUCLEI WITH ROTATION-VIBRATION COUPLING

V.O.Nesterenko

Joint Institute for Nuclear Research, Dubna

The extended version of the Quasiparticle-Phonon Model (QPM) for even-even, odd and oddodd deformed nuclei is presented. The main new point is taking into account the coupling of rotational and vibrational degrees of freedom. Applications of the model for all three types of nuclei are considered.

Представлен расширенный вариант квазичастично-фононной модели (КФМ) для четночетных, нечетных и нечетно-нечетных деформированных ядер, главной особенностью которого является учет связи ротационных и вибрационных степеней свободы. Рассматриваются приложения модели для всех трех типов ядер.

1. INTRODUCTION

The up-to-day status of investigation of low-lying states in deformed nuclei requires the construction of a general microscopic model which would include consistently such important ingredients of residual interaction as: the rotational and vibrational degrees of freedom, the Coriolis mixing, the coupling with even-even core excitations (for odd and odd-odd nuclei), the pairing and, finally, the interaction between an external proton and neutron in an odd-odd nucleus, which results in the Gallagher — Moszkowski splitting and the Newby shift. It is very important also that the model would be able to describe the properties of even-even, odd and odd-odd nuclei on the same microscopic footing. Up to now, such a general microscopic model has not been derived though some ingredients mentioned above have been incorporated into different microscopic models (see, e.g., refs. [1—8]). The QPM [1—4,10,11] seems to be the most appropriate ground for this aim since just the QPM is known to succeed in the description of the vibrational low-lying states in a wide region of deformed even-even and odd nuclei [1—3,10—17].

It is worth noting that in the QPM most of the model parameters are fixed at the stage of calculations for even-even core. In this sense the calculations in the QPM for even-even, odd and odd-odd nuclei are consistent.

Investigation of low-lying states in deformed nuclei within the QPM was developed last time in the following directions: two-phonon components in low-lying states of even-even nuclei, the Pauli principle effects, particleparticle channel of residual interaction, high multipolarity states, magnetic collective excitations and so on. These fields are described in the monograph [2] and will not be presented here. The main aim of this paper is a further extending of the QPM by taking into account rotational degrees of freedom together with its coupling (through the Coriolis interaction) with vibrational excitations. It is clear from very beginning that in deformed nuclei where rotational and vibrational excitations are in many cases quite entangled, such extending of the model should be very important for successful description of low-lying states. Also, additional modifications (mainly for odd-odd nuclei) providing the grounds for the calculation of the Gallagher — Moszkowski splitting, Newby shift, mixing of neutron-proton configurations and some others are proposed. The sketch of general microscopic scheme for description of low-lying states in strictly deformed nuclei, which satisfies in large extent the demands listed above, is given. In the framework of this scheme all degrees of freedom are considered on the same microscopic footing. Such extended model can be applied to even-even, odd and odd-odd deformed nuclei. Description of the model is given in section 2.

A practical application of the general scheme presented here is not a simple task. Rather sophisticated computer codes should be used. Now only for odd nuclei the main ingredients of the model (the quasiparticle-phonon and Coriolis interactions) are taken into account simultaneously in real calculations [18—20]. So, only for this kind of nuclei the general scheme is realized in large extent. In calculations for even-even and especially for odd-odd nuclei truncated version of the general scheme, embracing only one of the main ingredients, have been used up to now [1,2,4,13]. Nevertheless, we present here the examples of calculations for these nuclei also since in spite of simplified character of these calculations the results obtained seem to be rather interesting from physical point of view.

As a first example we will consider in subsection 3.1 the nonadiabatic behavior of $E2(\gamma \rightarrow gr)$ transitions in ¹⁶⁶Er, discovered recently in the Coulomb excitation reaction [21]. In the phenomenological two-rotor model [22] this behavior is explained by the coupling between the γ and ground bands through the $K^{\pi}=1^+$ state interpreted as a «scissors» mode [23]. The Coriolis interaction is considered as the main (but not the single) physical origin of this coupling. We will show that in the framework of the RPA the

Coriolis coupling between the ground and 1^+ states vanishes completely if the rotational invariance of the Hamiltonian is restored [24]. This effect was not mentioned before in spite of the intensive investigation of the «scissors» mode for a long time. So, the ground and 1^+ states represent a unique example of the states with the same parity and $\Delta K = 1$, which are not mixed by the Coriolis interaction in the framework of the familiar RPA. Under some special conditions, e.g. in the case of nuclear triaxiality, the Coriolis mixing appears again. So, the physical interpretation of the phenomenological description [22] is not trivial and needs careful analysis.

The second example presented in subsection 3.2 concerns odd nuclei. It will be shown that even very small (about 1%) octupole admixtures in wave functions of odd nuclei can influence very much E1 transitions between low-lying states. This is a challenge to numerous calculations of reduced probabilities B(E1) where only pairing and Coriolis mixing were taken into account (the main motivation for neglecting vibrational admixtures in such calculations was just their small magnitude). Also, it is demonstrated that in some expressive cases only the interplay of the quasiparticle-phonon and Coriolis interactions can explain experimental data [18,19].

In subsection 3.3 the calculations for low-lying states of 166 Ho are presented where the coupling of external nucleons with core vibrations is allowed for [8,9]. It turns out that low-lying states contain vibrational components whose magnitudes are sufficiently large to influence strongly reduced probabilities of electrical transitions. It means that, like odd nuclei, the traditional approach for calculations of $B(E\lambda)$ values in odd-odd nuclei where only pairing and Coriolis coupling are taken into account should be revised.

2. THE MODEL

2.1. The Hamiltonian. The Hamiltonian of the model is written as a sum of the rotational, intrinsic and Coriolis interaction terms:

$$H = H_{\text{rot}} + H_{\text{intr}} + H_{\text{cor}}, \tag{1}$$

where

$$H_{\text{rot}} = \frac{h^2}{2J} \cdot (I^2 - I_3^2),\tag{2}$$

$$H_{\rm cor} = -\frac{h^2}{2J} \cdot (I^+ j^- + I^- j^+). \tag{3}$$

In eqs. (2)—(3) I^{\pm} and j^{\pm} are the shift operators of the total and intrinsic angular moments, respectively; K is the projection of the angular momentum onto the axis z; J is the moment of inertia.

In accordance with [1,2,4,9]

$$H_{\text{intr}} = H_{\text{sp}} + H_{\text{pair}} + H_{\text{mm}}, \tag{4}$$

where H_{sp} is a single-particle potential,

$$H_{\text{pair}} = -\sum_{\tau} \sum_{q_1 q_2} G_{\tau} a_{q_1^{+}}^{\dagger} a_{q_1^{-}}^{\dagger} a_{q_2^{-}} a_{q_2^{+}}, \qquad (5)$$

is a monopole pairing and

$$H_{\text{res}} = -1/2 \sum_{\lambda \widetilde{\mu}} \sum_{\tau \tau'} (\kappa_0^{(\lambda \mu)} + \tau \tau' \kappa_1^{(\lambda \mu)}) Q_{\lambda \widetilde{\mu}}^{(\tau)} Q_{\lambda - \widetilde{\mu}}^{(\tau')}, \tag{6}$$

is an isoscalar and isovector interaction. In this paper the latter is taken in the form of multipole-multipole forces except for the special case of consideration of the Gallagher — Moszkowski splitting and Newby shift where a spin-spin forces are used. The use of a spin-multipole residual interaction for the description of magnetic type excitations in deformed nuclei is considered in [2] and is not presented here. The multipole operator in (6) is written as

$$Q_{\lambda \mu}^{(\tau)} = \sum_{\widetilde{q}_1 \widetilde{q}_2 \in \tau} \delta_{\widetilde{K}_1 - \widetilde{K}_2, \widetilde{\mu}} < \widetilde{q}_1 \mid \widehat{f}^{\lambda \mu} \mid \widetilde{q}_2 > a_{\widetilde{q}_1}^{\dagger} a_{\widetilde{q}_2}, \tag{7}$$

where $\langle \widetilde{q}_1 \mid \widehat{f}^{\lambda\mu} \mid \widetilde{q}_2 \rangle$ is the single-particle matrix element for the operator

$$\hat{f}^{\lambda \mu} = R(r) \left(Y_{\lambda \mu} + (-1)^{\mu} Y_{\lambda - \mu} \right) \left(1 + \delta_{\mu, 0} \right)^{-1}$$
 (8)

with unspecified radial dependence R(r). In exps. (5)—(7) τ is equal to -1 and +1 for neutron and proton systems, respectively; $a_{\overline{q}}^{\dagger}(a_{\overline{q}})$ is the particle creation (annihilation operator for the single-particle state \widetilde{q} ; $\widetilde{q}=q\sigma$, $\widetilde{K}=K\sigma$; $\widetilde{\mu}=\mu\sigma$, $\mu\geq 0$; $\sigma=\pm 1$ characterizes the symmetry with respect to the time reversal operation; G_{τ} is the pairing strength constant; $\kappa_0^{(\lambda\mu)}$ and $\kappa_1^{(\lambda\mu)}$ are the strength constants of isoscalar and isovector interaction, respectively.

Using the RPA equations for one-phonon excitations of the even-even core the intrinsic Hamiltonian (4) can be transformed to the form:

$$H_{\text{intr}} = H_{\alpha+Q} + H_{QB}^{\text{ph}} + H_{QB}^{\text{pair}} + H_{BB},$$
 (9)

where

$$H_{\alpha+Q} = \sum_{q} \varepsilon_{q} B(qq;0) - 1/4 \sum_{\lambda \widetilde{\mu}} \sum_{\tau} \sum_{ii'} \frac{X_{\tau}^{g} + X_{-\tau}^{g'}}{\sqrt{\widetilde{Y}_{\tau}^{g} \widetilde{Y}_{\tau}^{g'}}} Q_{\widetilde{g}}^{\dagger} Q_{\widetilde{g}'}, \qquad (10)$$

generates quasiparticle and phonon excitations,

$$H_{QB}^{\text{ph}} = -1/4 \sum_{\tau} \sum_{\tilde{g}} \sum_{q_1 q_2 \in \tau} \Gamma_{gq_1 q_2}^{\text{ph}}(\tau) [(Q_{\tilde{g}}^{\dagger} + Q_{-\tilde{g}}) B(q_1 q_2; -\tilde{\mu}) + \text{h.c.}]$$
 (11)

is the quasiparticle-phonon interaction in the particle-hole channel (just this interaction couples the quasiparticle excitations of external nucleons in odd and odd-odd nuclei with the phonon vibrations of the even-even core as well as multiphonon configurations differing from each other by one phonon in even-even nuclei),

$$H_{QB}^{\text{pair}} = \sum_{\tau} \sum_{i} \sum_{q_{1}q_{2} \in \tau} \left[\left(\Gamma_{iq_{1}q_{2}}^{\text{pair}(+)}(\tau) Q_{20i}^{\dagger} + \Gamma_{iq_{1}q_{2}}^{\text{pair}(-)}(\tau) Q_{20i} \right) B(q_{1}q_{2};0) + \text{h.c.} \right]$$
(12)

is the pairing quasiparticle-phonon interaction and

$$H_{BB} = -1/2 \sum_{\lambda \widetilde{\mu}} \sum_{\tau \tau'} (k_0^{(\lambda \mu)} + \tau \tau' \kappa_1^{(\lambda \mu)}) \times \\ \times \sum_{q_1 q_2 q'_1 q'_2 \in \tau} \Gamma_{\lambda \mu q_1 q_2 q'_1 q'_2}^{BB}(\tau) B(q_1 q_2; \widetilde{\mu}) B(q'_1 q'_2; -\widetilde{\mu})$$
(13)

is the so-called «scattering» interaction. In the case of spin-spin residual forces just this interaction is responsible for the Gallagher — Moszkowski splitting and the Newby shift [8,9].

In (10)—(13) the following notation is used: ε_q is the energy of the one-quasiparticle state q;

$$Q_{\widetilde{g}}^{\dagger} = 1/2 \sum_{q_1 q_2} (\psi_{q_1 q_2}^g A^{\dagger}(q_1 q_2; \widetilde{\mu}) - \phi_{q_1 q_2}^g A(q_1 q_2; -\widetilde{\mu}))$$
 (14)

is the creation operator of one-phonon state $\widetilde{g} \equiv g\sigma \equiv \lambda \mu i\sigma$, where i is the number of one-phonon state with given $\lambda \mu$; $\psi^g_{q_1q_2}$ and $\phi^g_{q_1q_2}$ are forward and backward amplitudes of two-quasiparticle component q_1q_2 ; two-quasiparticle operators $A^\dagger(q_1q_2;\widetilde{\mu})$ and $B(q_1q_2;\widetilde{\mu})$ are of the form

$$A^{\dagger}(q_1 q_2; \widetilde{\mu}) = -\frac{1}{\sqrt{1 + \delta_{\mu,0}}} \sum_{\sigma_1, \sigma_2} \delta_{\widetilde{K}_1 + \widetilde{K}_2, \widetilde{\mu}} \alpha_{\widetilde{q}_1}^{\dagger} \alpha_{\widetilde{q}_2}^{\dagger} \theta_{\sigma_1 - \sigma_2}$$
 (15)

and

$$B(q_1q_2;\widetilde{\mu}) = \sum_{\sigma_1,\sigma_2} \delta_{\widetilde{K}_1 + \widetilde{K}_2,\,\widetilde{\mu}} \,\alpha_{\widetilde{q}_1}^\dagger \,\alpha_{-\widetilde{q}_2} \,\theta_{-\sigma_1 - \sigma_2}, \tag{16}$$

where $\theta_{-\sigma_1-\sigma_2}=1-\delta_{\sigma_1,1}\delta_{\sigma_2,1}$. The expressions for the functions $\psi^g_{q_1q_2}$, $\psi^g_{q_1q_2}$, X^g_{τ} , \widetilde{Y}^g_{τ} , $\Gamma^{\rm ph}_{gq_1g_2}(\tau)$, $\Gamma^{\rm pair(+)}_{iq_1q_2}(\tau)$, $\Gamma^{\rm pair(-)}_{iq_1q_2}(\tau)$ and $\Gamma^{BB}_{\lambda\,\mu q_1q_2q'_1q'_2}(\tau)$ which are determined after solving the RPA equations are given in the Appendix.

2.2. Wave Functions for Even-Even, Odd and Odd-Odd Nuclei. The wave function of the Hamiltonian (1) has the form

$$|I^{\pi}M\rho\rangle = \sum_{K\nu} b_{\nu K}^{i\rho} |I^{\pi}MK\nu\rangle, \tag{17}$$

where $b_{\nu K}^{I\rho}$ are the Coriolis mixing coefficients; M and K are the angular momentum projections in the laboratory and intrinsic systems, respectively; ρ and ν are additional quantum numbers. Further [25],

$$|I^{\pi}MK\nu\rangle = \sqrt{\frac{2I+1}{16\pi^{2}(1+\delta_{K,0})}} \cdot (D_{MK}^{I} + (-1)^{I+K}D_{M-K}^{I}R_{i}) \cdot \Psi_{\nu}(K^{\pi}), \quad (18)$$

where Ψ_{ν} (K^{π}) is the eigenvector of H_{intr} ; R_{i} is the operator of rotation by an angle π around the second intrinsic axis.

In this paper the intrinsic wave function for even-even nucleus is written as a one-phonon state

 $\Psi_{\widetilde{g}}(\widetilde{K}^{\pi}) = Q_{\widetilde{g}}^{\dagger} \mid \rangle_{\text{RPA}}$ (19)

though the two-phonon version [2,26] (or the multiphonon one [27]) of the wave function may also be used. The case when the wave function of even-even nucleus contains both one- and two-phonon components is described in detail in [2] and is not considered here.

In an odd nucleus the intrinsic wave function has the form [1,2,4]

$$\Psi_{\nu}(\widetilde{K}^{\pi}) = \left\{ \sum_{\widetilde{q}_{1}} C_{q_{1}}^{\nu} \delta_{\widetilde{K}_{1},\widetilde{K}} \alpha_{\widetilde{q}_{1}}^{\dagger} + \sum_{\widetilde{q}_{1}\widetilde{g}_{1}} D_{q_{1}g_{1}}^{\nu} \delta_{\widetilde{K}_{1}+\widetilde{\mu}_{1},\widetilde{K}} \alpha_{\widetilde{q}_{1}}^{\dagger} Q_{\widetilde{g}_{1}}^{\dagger} \right\} | \rangle_{\text{RPA}} | \rangle_{q}, \quad (20)$$

where $C_{q_1}^{\nu}$ and $D_{q_1g_1}^{\nu}$ are amplitudes of one-quasiparticle and quasiparticle \otimes phonon components, respectively; $|\rangle_{\rm RPA}$ and $|\rangle_q$ are the RPA $(Q_{\widetilde{g}}\,|\,\rangle_{\rm RPA}=0)$ and quasiparticle $(\alpha_{\widetilde{q}}\,|\,\rangle_q=0)$ vacuum; ν is the number of the state with given K^{π} .

In an odd-odd nucleus the intrinsic wave function is [4,8,9]

$$\Psi_{\nu\gamma}(\widetilde{K}^{\pi}) = \left\{ \sum_{\widetilde{s_1}\widetilde{r_1}} C_{s_1r_1}^{\nu\gamma} A_{\gamma}^{\dagger}(\widetilde{s_1} \ \widetilde{r_1} \ \widetilde{K}) + \right. \\ \left. + \sum_{\widetilde{s_1}\widetilde{r_1}\widetilde{g_1}\gamma} k_{\mu}^{K} D_{s_1r_1g_1}^{\nu\gamma_1} A_{\gamma_1}^{\dagger} (\widetilde{s_1}\widetilde{r_1}\widetilde{K}_1) Q_{\widetilde{g_1}}^{\dagger} \delta_{\widetilde{K}_1 + \widetilde{\mu}, \widetilde{K}} \right\} \left. \right| \left. \right\rangle_{\text{RPA}} \left. \right| \left. \right\rangle_{q},$$
 (21)

where

$$A_{\gamma}^{\dagger} \left(\widetilde{s} \, \widetilde{r} \, \widetilde{K} \right) = \frac{1}{\sqrt{1 + \delta_{K0}}} \alpha_{\widetilde{s}}^{\dagger} \, \alpha_{\widetilde{r}}^{\dagger} \, \delta_{\widetilde{K}_{s} + \widetilde{K}_{r}, \widetilde{K}} \, k_{\gamma \sigma_{s} \sigma_{r}}^{K}$$
 (22)

and

$$k_{\mu}^{K} = \left(1 + \delta_{K,0} \left(1 - \delta_{\mu,0}\right)\right)^{-1/2}, \quad k_{\gamma\sigma_{s}\sigma_{r}}^{K} = 1 - \left(1 + \gamma\right) \delta_{K,0} \delta_{\sigma_{s},-1} \delta_{\sigma_{r},+1}. \tag{23}$$

Here, $C_{s_1r_1}^{\nu\gamma}$ and $D_{s_1r_1g_1}^{\nu\gamma}$ are amplitudes of neutron-proton and neutron-proton \otimes phonon components, respectively. For K=0 the function (21) depends on $\gamma=\pm 1$ which is eigenvalue of the operator R_i . In this case the condition $\gamma=(-1)^I$ takes place [25]. The coefficients k_{μ}^K and $k_{\gamma\sigma_s\sigma_r}^K$ are introduced to provide the simple form of the normalization condition for the wave function (21) [8,9].

After solving the RPA equations for the even-even core the phonon basis is used for the construction of the states (20)—(21). The energies and structure of the intrinsic states (20)—(21) are calculated by the variation method with keeping the normalization condition for the states. It should be noted that all the parameters of the model are fixed after solving the RPA equations.

If a wave function includes a complex components like two-phonon — in even-even nuclei, quasiparticle \otimes phonon — in odd nuclei and neutron-proton \otimes phonon — in odd-odd nuclei we should take into account the Pauli principle. This problem was considered for even-even and odd nuclei in ref. [2,3,10,27]. In [27] it was shown for even-even nuclei that taking into account multiphonon configurations (three-phonon and so on) decreases in large extent the excitation energy shifts caused by the Pauli principle effects. For the sake of brevity we do not present here the corresponding formalism.

2.3. Final Expressions of the Model. The RPA equations for one-phonon excitation in even-even nuclei are given in the Appendix. Below we present the final expressions for determining wave functions and excitation energies in odd and odd-odd nuclei. These expressions are derived in the framework of the variation procedure [1—3,8,9]. Since we do not discuss in this paper the Pauli principle effects, the corresponding corrections are omitted.

For odd nuclei the amplitudes $C_q^{\ \nu}$ and $D_{qg}^{\ \nu}$ of the wave function (20) are found from the system of equations

$$\sum_{q'} C_{q'}^{\nu} \left\{ (\varepsilon_q - \eta_{\nu}) \, \delta_{q,q'} - \frac{1}{4} \sum_{gq_1} \frac{\Gamma_{gq_1q}(\tau) \, \Gamma_{gq_1q'}(\tau)}{\varepsilon_{q_1} + \omega_g - \eta_{\nu}} \right\} = 0, \quad (24)$$

$$D_{qg}^{\nu} = (\varepsilon_q + \omega_g - \eta_{\nu}))^{-1} \cdot \frac{1}{2} \sum_{q'} C_{q'}^{\nu} \Gamma_{gqq'}(\tau)$$
 (25)

and the secular equation for determination of the excitation energy η_{v} is

$$\det \| (\varepsilon_q - \eta_{\nu}) \, \delta_{q,q'} - \frac{1}{4} \sum_{gq} \frac{\Gamma_{gq_1q'}(\tau) \, \Gamma_{gq_1q'}(\tau)}{\varepsilon_{q_1} + \omega_g - \eta_{\nu}} \| = 0. \tag{26}$$

For odd-odd nuclei the corresponding equations are

$$\sum_{s'r'} C_{s'r'}^{\nu\gamma} \left\{ \left(\varepsilon_s + \varepsilon_r + \langle rs \mid V_{np} \mid rs \rangle_{0\gamma} - \eta_{\nu} \right) \delta_{sr,s'r'} - \frac{\Gamma_{gss_1rr_1} \Gamma_{gs's_1r'r_1}}{\varepsilon_s + \varepsilon_r + \langle r_1s_1 \mid V_{np} \mid r_1s_1 \rangle_{\mu\gamma} + \omega_g - \eta_{\nu\gamma}} \right\} = 0, \tag{27}$$

$$D_{srg}^{\nu\gamma} = (\varepsilon_s + \varepsilon_r + \langle rs \mid V_{np} \mid rs \rangle_{\mu\gamma} + \omega_g - \eta_{\nu\gamma})^{-1} \frac{1}{2} \sum_{s'r'} C_{s'r'}^{\nu\gamma} \Gamma_{gss'rr'}$$
 (28)

and

$$\det \| (\varepsilon_{s} + \varepsilon_{r} + \langle rs \mid V_{np} \mid rs \rangle_{0\gamma} - \eta_{\nu}) \, \delta_{sr,s'r'} - \frac{\Gamma_{gss_{1}rr_{1}} \Gamma_{gs's_{1}r'r_{1}}}{\varepsilon_{s_{1}} + \varepsilon_{r_{1}} + \langle r_{1}s_{1} \mid V_{np} \mid r_{1}s_{1} \rangle_{\mu\gamma} + \omega_{g} - \eta_{\nu\gamma}} \| = 0, \qquad (29)$$

where

$$\Gamma_{gss_1rr_1} = \Gamma_{gss_1}(\tau = -1) \, \delta_{r,r_1} + \Gamma_{grr_1}(\tau = +1) \, \delta_{s,s_1}.$$
 (30)

In (27)—(29) only diagonal matrix elements of n-p interaction $\langle rs \mid V_{np} \mid rs \rangle_{\mu\gamma}$ are taken into account. These matrix elements are discussed in the subsection 2.5. Except for the n-p interaction terms final equations for odd and odd-odd nuclei are quite similar. The expression for $\Gamma_{gqq_1}(\tau)$ is given in the Appendix.

2.4. $E\lambda$ Transition Probabilities. The reduced probability of $E\lambda$ transition between states (17) is written as [25]

$$B(E\lambda, I_{\rho}^{\pi} \to I_{\rho'}^{\pi'} = 1/(2I+1) \left| \left\langle I_{\rho'}^{\pi'} \right| \left| E\lambda \right| \left| I_{\rho}^{\pi} \right\rangle \right|^{2}, \tag{31}$$

where the reduced matrix element has the form

$$\langle I_{\rho'}^{\pi'} \| E \lambda \| I_{\rho}^{\pi} \rangle = \sqrt{2I + 1} \sum_{K \nu K' \nu'} b_{\nu K}^{l \rho} b_{\nu' K'}^{l' \rho'} \times \\ \times \{ (IK \lambda K' - K | I' K') (\Psi_{\nu'}(K'^{\pi'}) \hat{M}(E \lambda, \mu = K' - K) \Psi_{\nu}(K^{\pi})) + \\ + (-1)^{I + K} (I - K \lambda K' + K | I' K') (\Psi_{\nu'}(K'^{\pi'}) \hat{M}(E \lambda, \mu = K' + K) \Psi_{\nu}(K^{\pi})) \}.$$
 (32)

The intrinsic matrix element $(\Psi_{\nu'}(K'^{\pi'})\hat{M}(E\lambda, \mu = K' \pm K) \Psi_{\nu}(K^{\pi}))$ is calculated using the operator for $E\lambda$ transition [2,10]

$$\widehat{M}(E\lambda,\widetilde{\mu}) = \sum_{i} L_{g}^{E\lambda}(Q_{\widetilde{g}}^{\dagger} + Q_{-\widetilde{g}}) + \sum_{q_{1}q_{2}} p_{q_{1}q_{2}}^{\lambda\mu} v_{q_{1}q_{2}}^{(-)} B(q_{1}q_{2};\widetilde{\mu}) + 2 \sum_{q} p_{qq}^{\lambda\mu} v_{q}^{2}.$$
(33)

Here

$$L_g^{E\lambda} = \sqrt{(1 + \delta_{\mu,0})/4} \sum_{q_1 q_2} p_{q_1 q_2}^{\lambda \mu} u_{q_1 q_2}^{(+)} (\psi_{q_1 q_2}^g + \phi_{q_1 q_2}^g) . \tag{34}$$

is the matrix element of $E\lambda$ the transition between the one-phonon state (19) and the ground state; $v_{q_1q_2}^{(\pm)} = u_{q_1}u_{q_2} \pm v_{q_1}v_{q_2}$ and $u_{q_1q_2}^{(\pm)} = u_{q_1}v_{q_2} \pm v_{q_1}u_{q_2}$; u_q and v_q are the Bogolubov transformation coefficients; $p_{q_1q_2}^{\lambda\mu}$ is the single-particle matrix element for the operator of $E\lambda$ transition:

$$\hat{p} = e e_{\text{eff}}^{\tau} r^{\lambda} (Y_{\lambda \mu} + (-1)^{\mu} Y_{\lambda - \mu}) (1 + \delta_{\mu, 0})^{-1}, \tag{35}$$

where the effective charge $e_{\rm eff}^{\tau} = (1+\tau)/2 + e_{\rm eff}$ is fitted so as to reproduce the experimental $B(E\lambda)$ values in the even-even core.

The first term in exp. (33) is responsible for the $E\lambda$ transitions between the states (or components of the states) which differ from each other by one phonon. This term determines the transitions between the ground and one-phonon states in even-even core and the collective part of the interband $E\lambda$ transitions in odd and odd-odd nuclei. The second term in (33) determines $E\lambda$ transitions between the wave function components with the same number of quasiparticles (phonons). This term plays the main role in interband transitions in odd and odd-odd nuclei if vibrational admixtures of wave functions can be neglected. The third term in (33) is responsible for the intraband transitions. Just this term determines the quadrupole moment of nucleus.

The intrinsic matrix elements for odd and odd-odd nuclei are, respectively,

$$(\Psi_{\nu'}(K^{\prime^{\pi'}}) \, \, \widehat{M} \, (E\lambda, \mu = K^\prime \pm K) \, \Psi_{\nu} \, (K^\pi)) = \sum_{qq'} \, C_q^{\,\nu} \, C_{q'}^{\,\nu'} \, v_{qq'}^{(-)} \, \widetilde{p}_{qq'}^{\,\lambda\mu} \, + \\$$

$$+ \sum_{i} L_{\lambda\mu i}^{E\lambda} \sum_{q_{1}} (C_{q'}^{\nu'} D_{q_{1}g}^{\nu} + D_{q_{1}g}^{\nu'} C_{q}^{\nu}) + \sum_{g_{1}} \sum_{q_{1}g'_{1}} D_{q_{1}g_{1}}^{\nu} D_{q'_{1}g_{1}}^{\nu'} v_{q_{1}q'_{1}}^{(-)} \widetilde{p}_{q_{1}q'_{1}}^{\lambda\mu}$$
(36) and
$$(\Psi_{\nu'\gamma'}(K'^{\pi'}) \widehat{M} (E\lambda, \mu = K' \pm K) \Psi_{\nu\gamma} (K^{\pi})) =$$
$$= \sum_{ss'rr'} C_{sr}^{\nu\gamma} C_{s'r'}^{\nu\gamma'} (v_{ss'}^{(-)} \widetilde{p}_{ss'}^{\lambda\mu} \delta_{r,r'} + v_{rr'}^{(-)} \{\widetilde{p}_{rr'}^{\lambda\mu} \delta_{s,s'}\} k_{\gamma\gamma'}^{CC} +$$
$$+ \sum_{i} L_{\lambda\mu i}^{E\lambda} \sum_{sr} (C_{sr}^{\nu'\gamma'} D_{srg}^{\nu\gamma} + D_{srg}^{\nu'\gamma'} C_{sr}^{\nu\gamma}) +$$

$$+\sum_{ss'rr'}\sum_{g_{1}}\sum_{\gamma_{1}\gamma'_{1}}D_{srg_{1}}^{\nu'\gamma_{1}}D_{s'r'g_{1}}^{\nu'\gamma'_{1}}(v_{ss'}^{(-)}\widetilde{p}_{ss'}^{\lambda\mu}\delta_{r,r'}+v_{rr'}^{(-)}\widetilde{p}_{rr'}^{\lambda\mu}\delta_{s,s'})k_{\gamma_{1}\gamma'_{1}}^{DD}.$$
 (37)

Expressions for the coefficients $k_{\gamma\gamma'}^{CC}$ and $k_{\gamma\gamma'}^{DD}$ are given in the Appendix. The single-particle matrix element $\widetilde{p}_{qq'}^{\lambda\mu}$ of operator (35) is of the same form as the matrix element $\widetilde{f}_{qq'}^{\lambda\mu}$ whose expression is also given in the Appendix.

2.5. Gallagher-Moszkowski Splitting (GMS) and Newby Shift (NS). It is well known that the GMS and NS in odd-odd nucleus are caused by the spin-spin part of interaction between external neutron and proton. Let us consider the neutron-proton part of the interaction (13) for the case of spin-spin residual forces. It is easy to show that the GMS and NS are implicitly involved in the equations for the intrinsic excitations of odd-odd nuclei just due to this term [8,9]. So, for odd-odd nuclei this term (denoted as V_{np}) should be taken into account in addition to the quasiparticle-phonon interaction.

The expressions for the Gallagher — Moszkowski splitting and Newby shift can be extracted from the secular equation (29) if the long-range residual interaction, except for V_{np} , is neglected $(\Gamma_{gq_1q_2}^{ph}(\tau) = \Gamma_{iq_1q_2}^{pair(-)}(\tau) = 0)$.

Then for general case of V_{np} to be hermitian and invariant under time reversal the secular equation (29) can be written as [8,9]

$$\eta_{\nu\gamma} = \varepsilon_{s} + \varepsilon_{r} + \langle rs \mid V_{np} \mid rs \rangle_{0\gamma} = \varepsilon_{s} + \varepsilon_{r} - \delta_{K,0} \gamma \langle r + s - | V_{np} | r - s + \rangle + \\ + \delta_{K_{s} + K_{r}, K} (\langle r + s + | V_{np} | r + s + \rangle (u_{r}^{2} u_{s}^{2} + v_{r}^{2} v_{s}^{2}) - \\ - \langle r - s + | V_{np} | r - s + \rangle (v_{r}^{2} u_{s}^{2} + u_{r}^{2} v_{s}^{2})) + \\ + \delta_{+K_{s} - K_{r}^{+}, K} (\langle r + s - | V_{np} | r + s - \rangle (u_{r}^{2} u_{s}^{2} + v_{r}^{2} v_{s}^{2}) - \\ - \langle r - s - | V_{np} | r - s - \rangle (v_{r}^{2} u_{s}^{2} + u_{r}^{2} v_{s}^{2})).$$
 (38)

Using the connection $\gamma = (-1)^I$ we finally obtain the well-known expression for the Gallagher — Moszkowski splitting energy, corresponding to the case of the independent quasiparticles:

$$\Delta E = \eta_{\nu\gamma} \, \delta_{|K_s - K_r|, K} - \eta_{\nu\gamma} \, \delta_{K_s + K_r, K} = \langle r + s - | V_{np} | r + s - \rangle -$$

$$- \langle r + s + | V_{np} | r + s + \rangle + \delta_{K,0} (-1)^{I+1} \langle r + s - | V_{np} | r - s + \rangle.$$
(39)

The last term in (39) is connected with the Newby shift:

$$\Delta E_{K=0} = \eta_{\nu \gamma = -1} - \eta_{\nu \gamma = +1} = 2\langle r + s - | V_{np} | r - s + \rangle. \tag{40}$$

Expressions (38)—(40) were derived for a general case of V_{np} . The same kind of spin splitting should be in even-even nuclei also. If neutron-proton interaction is approximated by exp.(13) with spin-spin forces, the expressions for the energy splitting between two-quasiparticle configurations with parallel and antiparallel spins has especially simple form:

$$\Delta E = -\tilde{\kappa}_1^{10} \, \sigma_1^{} \, \sigma_2^{} \, \wp_{q_1 q_1}^{10} \, \wp_{q_2 q_2}^{10} \tag{41}$$

for two-quasiparticle state q_1q_2 in even-even nucleus and

$$\Delta E = + \tilde{\kappa}_1^{10} \, \sigma_s \, \sigma_r \, \wp_{ss}^{10} \, \wp_{rr}^{10} \tag{42}$$

for neutron-proton state sr in odd-odd nucleus. In (41)—(42) $\tilde{\kappa}_1^{10}$ is the strength constant of isovector spin-spin interaction with multipolarity $\lambda\mu=10$ (this strength constant is negative); \wp_{ss}^{10} is a diagonal single-particle matrix element for the Pauli matrix operator; σ values are defined here as signs of K projections (do not confuse them with signs of spin projections!). The calculations for rare-earth even-even nuclei [28] have shown that expression (41) well reproduces the Gallagher rule for even-even nuclei. This rule states that two-quasiparticle configuration has lower excitation energy if spins of quasiparticles are antiparallel as compared with the case of parallel spins.

2.6. Coriolis Interaction Matrix Elements. The general expression (for even-even, odd and odd-odd nuclei) for the Coriolis matrix element is

$$\langle | I'^{\pi}M'K'\nu' | H_{\text{cor}} | I^{\pi}MK\nu \rangle = -\delta_{I'M',IM} \frac{h^{2}}{2J} \times \\ \times \left[\delta_{K',K-1} \sqrt{1 + \delta_{K',0}} \sqrt{(I+K)(I-K+1)} \left(\Psi_{\nu'} (K'^{\pi}) | j^{-} | \Psi_{\nu} (K^{\pi}) \right) + \\ + \delta_{K',K+1} \sqrt{1 + \delta_{K',0}} \sqrt{(I-K)(I+K+1)} \left(\Psi_{\nu'} (K'^{\pi}) | j^{+} | \Psi_{\nu} (K^{\pi}) \right) + \\ + (-1)^{I+1/2} \delta_{K,1/2} \delta_{K',1/2} \left(\Psi_{\nu'} (K'^{\pi} = \frac{1}{2}) | j^{+} | \Psi_{\nu} (K^{\pi} = \frac{1}{2}) \right) \right]. \tag{43}$$

In the most simple case of one-phonon excitations (19) in even-even nuclei the intrinsic matrix element $(\Psi_{\nu'}(K'^{\pi})|j^{+}|\Psi_{\nu}(K^{\pi}))$ is written as

$$\langle K'^{\pi}_{\nu'} = 1^{+}_{\nu} \mid j^{+} \mid \rangle_{RPA} \equiv {}_{RPA} \langle \mid Q_{21\nu} j^{+} \mid \rangle_{RPA} = \sum_{q_{1} \geq q_{2}} j^{+}_{q_{1}q_{2}} u^{(-)}_{q_{1}q_{2}} (\psi^{21\nu}_{q_{1}q_{2}} + \phi^{21\nu}_{q_{1}q_{2}})$$

$$\tag{44}$$

for the coupling between the ground and l_{ν}^{+} bands and

$$\langle K_{\nu'}^{,\pi} | j^{+} | K_{\nu}^{,\pi} \rangle \equiv {}_{RPA} \langle | Q_{\lambda'\mu'\nu'} | j^{+} Q_{\lambda\mu\nu}^{\dagger} | \rangle_{RPA} =$$

$$= \delta_{K',K+1} \sum_{q_{1} \geq q_{2}} j_{q_{1}q_{2}}^{+} v_{q_{1}q_{2}}^{(+)} \sum_{q_{3}} (\psi_{q_{1}q_{3}}^{\lambda'\mu'\nu'} \psi_{q_{2}q_{3}}^{\lambda\mu\nu} + \psi_{q_{3}q_{2}}^{\lambda'\mu'\nu'} \psi_{q_{3}q_{1}}^{\lambda\mu\nu}) (1 + \delta_{K_{1}+K_{2},1})$$
(45)

for the coupling between bands with one-phonon band heads (the γ and 1_{ν}^+ bands, octupole bands and so on). In (44), (45) the boson ($\sim a_{q_1\sigma_1}^{\dagger} a_{q_2\sigma_2}^{\dagger}$) and fermion ($\sim a_{q_1\sigma_1}^{\dagger} a_{q_2\sigma_2}^{\dagger}$) parts of the operator j^+ are taken into account, respectively; $j_{q_1q_2}^+$ is the single-particle matrix element for this operator.

It is easy to see that the well-known condition of restoration of the rotational invariance in even-even nuclei

$$\langle 1_{\nu}^{+} \mid I^{+} \mid \rangle_{RPA} \equiv {}_{RPA} \langle \mid Q_{21\nu} I^{+} \mid \rangle_{RPA} = 0 \tag{46}$$

in the intrinsic system can be written as

$$\langle 1_{\nu}^{+} \mid j^{+} \mid \rangle_{RPA} \equiv {}_{RPA} \langle \mid Q_{21\nu} j^{+} \mid \rangle_{RPA} = 0, \tag{47}$$

since in this case only the intrinsic part of the total momentum operator affects the RPA wave functions. As a result, exp. (47) for the Coriolis matrix element has the same form as the relation of the orthogonality of the RPA wave function with respect to the spurious state in ref. [29]. Exp. (47) leads to important consequence: if in the RPA calculations the rotational invariance is restored correctly, the Coriolis interaction between the ground band and the $K^{\pi} = 1^{+}_{\nu}$ bands should be exactly zero. For the case of two-quasiparticle states (without a residual interaction) the similar result has been obtained in ref. [30]. So, in the framework of the RPA the ground band has no the Coriolis coupling with any other band. It should be noted that under some special conditions (for example, a triaxiality of nucleus) the Coriolis coupling of the ground band with $K^{\pi} = 1^{+}_{\nu}$ bands appears again.

The intrinsic matrix elements of the Coriolis interaction for odd and oddodd nuclei are respectively:

$$(\Psi_{\nu'}(K'^{\pi}) | j^{+} | \Psi_{\nu}(K^{\pi})) =$$

$$= \sum_{qq'} C_{q'}^{\nu} V_{qq'}^{(+)} \widetilde{j}_{qq'}^{+} + \sum_{g_{1}} \sum_{q_{1}q'_{1}} D_{q_{1}g_{1}}^{\nu} D_{q_{1}g_{1}}^{\nu'} V_{q_{1}q'_{1}}^{(+)} \widetilde{j}_{q_{1}q'_{1}}^{+}, \qquad (48)$$

and

$$(\Psi_{\nu}(K^{\pi}) \mid j^{+} \mid \Psi_{\nu'}(K'^{\pi})) = \sum_{ss'rr'} C_{sr}^{\nu\gamma} C_{s'r'}^{\nu\gamma'} (v_{rr'}^{(+)}) \widetilde{j}_{ss'}^{+} \delta_{r,r'} + v_{rr'}^{(+)}) \widetilde{j}_{rr'}^{+} \delta_{s,s'} k_{\gamma\gamma'}^{CC} + \\ + \sum_{ss'rr'} \sum_{g_{1}} \sum_{\gamma_{1}\gamma'_{1}} D_{srg_{1}}^{\nu'\gamma_{1}} D_{s'r'g_{1}}^{\nu'\gamma'_{1}} (v_{ss'}^{(+)}) \widetilde{j}_{ss'}^{+} \delta_{r,r'} + v_{rr'}^{(+)}) \widetilde{j}_{rr'}^{+} \delta_{s,s'} k_{\gamma_{1}\gamma'_{1}}^{DD}.$$

$$(49)$$

Note that terms of $C^{\nu} \cdot D^{\nu'}$ type are absent in (48),(49). This is the case if we take into account the rotational invariance of the Hamiltonian (see above the comment for even-even nuclei) and neglect the Pauli principle effects.

In [31] it has been shown that vibrational admixtures in wave functions of odd deformed nuclei can be the main reason of the well-known attenuation of the Coriolis coupling matrix elements. Indeed, vibrational admixtures in wave function of odd nucleus (20) decrease the absolute values of amplitudes C_q^{ν} of one-quasiparticle configurations. As a result, if heads of two rotational bands can be approximated by one-quasiparticle configurations q_1 and q_2 we can easy get in first approximation the following attenuation coefficient (caused by vibrational admixtures only!) for the Coriolis coupling between these bands:

$$k_{q_1 q_2}^{\text{att}} = C_{q_1}^{\nu_1} \cdot C_{q_2}^{\nu_2}. \tag{50}$$

In section 4 this coefficient will be used for estimation of the Coriolis attenuation in odd Eu and Tb isotopes. It is clear that similar attenuation coefficient should take place for odd-odd nuclei also.

3. NONADIABATIC BEHAVIOR OF $E2(\gamma \rightarrow gr)$ TRANSITIONS IN ¹⁶⁶Er

An almost complete set of reduced E2 matrix elements for the ground and γ bands up to spin 14⁺ and 12⁺, respectively, has recently been measured for ¹⁶⁶Er in a Coulomb excitation experiment [21]. In total, 44 E2 matrix elements have been determined in a model-independent way. Some of them clearly show a non-adiabatic behavior (deviation from the Alaga rule). Calculations of the E2 matrix elements were performed [21] within four collective

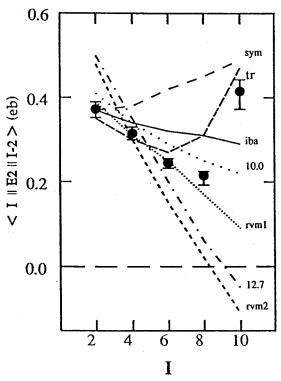


Fig.1. The experimental and calculated values [21] of the $I_{\gamma} \rightarrow (I-2)_{gr}$ matrix elements in 166 Er. The calculations were performed within the symmetric rotor model (sym), the asymmetric rotor model [32] $(\gamma = 10^{\circ} \text{ and } 12.7^{\circ}, \text{ respectively})$, the rotation-vibration model [33] (rvml and rvm2), the IBA-1 model [34] (iba) and a two-rotor model [22] (tr). The adiabatic behavior corresponds to the results of the symmetric rotor model

models: the symmetrical rotor model, the asymmetric rotor model [32], the rotation-vibration model [33], and the IBA-1 model [34]. It has been shown that both the γ deformation and rotation-vibration coupling may be responsible for the strong slope in the $I_{\gamma} \rightarrow (I-2)_{gr}$ transitions (see figure 1 taken from ref. [21]). How-

ever, these models failed in explaining the sudden increase of the E2 matrix element of the $10^+_{\nu} \rightarrow 8^+_{gr}$ transition.

The Dubna group has previously succeeded in describing the nonadiabatic effects of the E2 transitions between the γ and ground bands (hereafter denoted as $E2(\gamma \rightarrow gr)$) in the framework of the two-rotor [22] and Coriolis coupling [35] phenomenological models. In both models the coupling between the γ and ground bands takes place due to the 1^+ state interpreted as a «scissors» mode [23]. In the latter model the Coriolis interaction is considered as the origin of this coupling. Both the models use the band head energies, moments of inertia, the band coupling matrix elements as well as some basic E2 matrix elements as parameters fitted so as to reproduce the experimental data for the spectrum and electromagnetic transitions. In some sense the models take into account, through these parameters, the γ deformation. Figure 1 shows that the calculations [22] give a satisfactory description of the experimental data for 1^{66} Er.

The main idea of the model [35], i.e. the Coriolis coupling between the γ and ground bands through one 1⁺ state, seems to be attractive. However, the energy excitation interval 2—5 MeV embracing the «scissors» mode includes a large number of 1⁺ states. So it is worth to perform a microscopic study of the role of the Coriolis coupling in the nonadiabatic behavior of the $E2(\gamma \rightarrow gr)$) transitions taking into account all the 1⁺ states in this energy interval and not using any free parameters. The γ deformation is not taken into account since this would result in rather cumbersome calculations. It is worth noting that although the «scissors» mode has been investigated very carefully (see the review [36] and refs. therein) the problem discussed here has not been considered on a microscopic footing.

The RPA calculations have been performed within the model described in the previous section. The intrinsic Hamiltonian (4) includes the Woods — Saxon single-particle potential as a sum of the spherical and quadrupole parts

$$H_{sp} = V_{WS}^{(0)}(r) + V_{WS}^{(2)}(r) Y_{20}(\theta, \varphi), \tag{51}$$

the monopole pairing and the quadrupole isoscalar and isovector interaction with $\lambda\mu=22$ and 21 [2,10].

The reduced matrix element (32) for the E2 transition between the γ and ground bands can be written as

$$\langle I_{gr}^{+} || E2 || I_{\gamma}^{+} \rangle = \sqrt{2I_{\gamma} + 1} \left(M(E2)_{Q_0} + M(E2)_{1^{+}} + M(E2)_{\gamma} \right),$$
 (52)

where

$$M(E2)_{Q_0} = \sqrt{\frac{5}{16\pi}} e Q_0 \left\{ \sum_{\rho = gr, \gamma} b_{\rho}^{l_{gr}} b_{\rho}^{l_{\gamma}} C_{l_{\gamma}K_{\rho};20}^{l_{gr}K_{\rho}} + \sum_{\nu=1} b_{l_{\nu}}^{l_{gr}} b_{l_{\nu}}^{l_{\gamma}} C_{l_{\nu}1;20}^{l_{gr}1} \right\}, \quad (53)$$

$$M(E2)_{1^{+}} = \sqrt{2} \sum_{\nu=1} L_{1_{\nu}}^{E2} \left\{ b_{gr}^{I_{gr}} b_{1_{\nu}}^{I_{\nu}} C_{I_{\nu}^{1};2-1}^{I_{gr}0} - b_{1_{\nu}}^{I_{gr}} b_{gr}^{I_{\nu}} C_{I_{\nu}0;21}^{I_{gr}1} \right\},$$
 (54)

$$M(E2)_{\gamma} = \sqrt{2} L_{\gamma}^{E2} \left\{ b_{gr}^{I_{gr}} b_{\gamma}^{I_{\gamma}} C_{I_{\gamma}2;2-2}^{I_{gr}0} + b_{\gamma}^{I_{gr}} b_{gr}^{I_{\gamma}} C_{I_{\gamma}0;22}^{I_{gr}2} \right\}.$$
 (55)

In exp. (53) Q_0 is the quadrupole moment calculated in the microscopic way (see subsection 2.4).

In the calculations the γ -vibrational $K^{\pi}=2^+$ state and 30 $K^{\pi}=1^+$ RPA states (all 1^+ states with excitation energies up to 5 MeV) have been taken into account. Without going into details of calculations which can be found in [24] let us consider the most delicate point of the task — determination of the isoscalar strength constant $\kappa_0^{(21)}$ which is known to be connected with the problem of extraction of the spurious admixtures caused by the violation of the rotation invariance of the Hamiltonian. There are different prescriptions

for the extraction of the spurious admixtures (see, for example, [29,30,37,38]). We used the method proposed in ref. [37] which seems to be most simple and convenient if the single-particle potential has the form (51). It is easy to show that in this case the restoration of the rotational invariance leads just to the $\lambda\mu=21$ residual interaction with the radial dependence

$$R_{21}(r) = V_{WS}^{(2)}(r). (56)$$

Indeed, for a single-particle potential of the form

$$H_{sp} = -V_0 \sum_{\lambda=0,2,4,...} F_{\lambda}(r) Y_{\lambda 0}(\theta, \phi)$$
 (57)

we have

$$[H_{sp}, I_{\nu}] = -\nu V_{0} \sum_{\lambda=0,2,4,\dots,\nu=\pm 1} \sqrt{\frac{\lambda(\lambda+1)}{2}} F_{\lambda}(r) Y_{\lambda\nu}(\theta, \phi)$$
 (58)

and the rotational invariance violated by the single-particle potential (57) can be restored by the quadrupole residual interaction with radial dependence (56). The isoscalar strength constant should be adjusted so as to put the first solution of the secular equation for 1^+ states to be zero. For the generalization of this method to the case of both isoscalar and isovector interactions we followed the prescription of ref. [38]. In accordance with [38] the $\lambda\mu=21$ residual interaction is written as

$$H_{QQ} = -1/2 \sum_{T=0,1} \kappa_T^{(21)} \tilde{Q}_{21}^{\dagger} \tilde{Q}_{21}, \tag{59}$$

where $\widetilde{Q}_{21} = Q_{21}^n + Q_{21}^p$ and $Q_{21}^n - \gamma Q_{21}^p$ for T = 0 and 1, respectively, and

$$\gamma = \frac{\langle \mid [Q_{21}^n, I_x] \mid \rangle}{\langle \mid [Q_{21}^p, I_x] \mid \rangle}.$$
 (60)

Then, the isoscalar and isovector interactions are decoupled and the strength constant of the isovector interaction can be fitted so as to reproduce the energy of the isovector giant quadrupole resonance. In this case we have $\kappa_1^{(2\mu)} = -1.5\kappa_0^{(2\mu)}$.

The Coriolis matrix elements we need for the calculations have the form (44)-(45). If in the RPA calculations the rotational invariance is restored correctly, the Coriolis interaction between the ground band and the $K^{\pi} = 1^{+}_{\nu}$ bands should be exactly zero. For the case of two-quasiparticle states (without a residual interaction) the similar result has been obtained in ref. [30]. So, in the framework of this approach the 1^{+}_{ν} bands are coupled by the Coriolis interaction with the γ band only. The ground band is coupled

neither with the γ band nor with the 1_{ν}^{+} bands. In this case, $M(E2)_{Q_0} = 0$, whereas $M(E2)_{1}^{+}$ and $M(E2)_{\gamma}$ contain the first terms only and the influence of the Coriolis coupling should be rather weak, which is confirmed by our calculations presented below. To switch on the coupling of the ground band with the 1_{ν}^{+} and γ band, it is necessary to generalize the approach by, e.g., taking into account γ deformation [32].

Let us consider the results of the calculations. In table 1 the largest Coriolis mixing coefficients for the γ band are given. The mixing with the 1^+_{ν} states is shown to be noticeable both for the low-lying and high-lying (the «scissors» mode region) states.

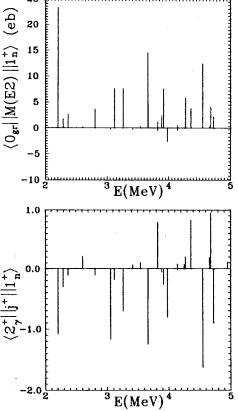
l 1, 1,, 1 + 22 1, 1 * 1 17 1+23 γ 1,3 .9992 2 ~.0277 -.0137 -.0076-.0116 .0071 -.0066.0063 -.0127 3 -.0426-.0212-.0118-.0180.0109 -.0105.0097 -.01819981 .9968 4 -.0554-.0276-.0153-.0234.0142 -.0137.0127 -.0236 9953 5 -.0667-.0334-.0185-.0283 .0172 -.0165.0153 -.0285-.0768-.0327 .0199 -.0191-.03309938 6 -.0386-.0214.0177 -.0860-.0433 -.0241-.0368.0223 -.0215.0199 -.0371.9922 7 -.0942-.0265-.0236 .0219 -.0408 .9906 8 -.0476-.0405.0246 -.1017-.0516-.0287 -.0439.0266 -.0256 .0238 -.0443.9889 -.1085-.0470 .0285 -.0274.0255 -.0475.9873 -.0552-.030710 -.1147-.0586-.0326-.0499 .0303 -.0292 .0271 -.0504.9858 11 12 -.1205-.0618-.0344-.0526 .0319 -.0307 .0286 .0532 .9842

Table 1. Coriolis Mixing Coefficients for the γ Band

It is interesting to compare the collectivity of the 1_{ν}^{+} states from the lowenergy and «scissors» mode regions. For this aim the $B(E2, 0^{+}0_{gr} \rightarrow 2^{+}K_{\nu})$ values and the structure of the lowest 1^{+} state, two most collective 1^{+} states from the «scissors» mode region and the γ vibrational state are-presented in table 2. It is seen that in both regions there are quite collective 1^{+} states.

Table 2. Calculated Excitation Energies (MeV), Reduced Transition Probabilities $B(E2, 0^+0_{gr} \rightarrow 2^+K_{\nu})$ (Wu) and Main Two-Qiasiparticle Components of the $K^{\pi}_{\nu} = 2^+_1, 1^+_1, 1^+_{11}$ and 1^+_{23} States

K_{ν}^{π} E_{ν} $B(E2) \uparrow$	The main two-quasiparticle components	%	K_{ν}^{π} E_{ν} $B(E2) \uparrow$	The main two-quasiparticle components	%
2 ₁ ⁺ 0.786 22	$nn523 \downarrow -521 \downarrow \\ pp411 \uparrow +411 \downarrow \\ nn523 \uparrow +521 \downarrow \\ pp413 \downarrow -411 \downarrow$	30 28 16 6	1 ⁺ ₁₁ 3.66 1.3	nn532 ↓ -521 ↓ pp402 ↑ -411 ↑ nn514 ↓ -512 ↑ nn523 ↓ -532 ↓	20 16 16 10
1 † 1.81 3.5	nn633 † -642 † pp514 † -523 † nn512 † -521 † nn624 † -633 †	71 9 8 2	1 ⁺ ₂₃ 4.55 0.75	nn521 \(\frac{-510}{}\) nn512 \(\frac{-521}{}\) nn523 \(\frac{-512}{}\) pp411 \(\frac{-420}{}\)	58 9 8 5



The correlation between the collectivity of the 1, states and the Coriolis matrix elements (45) is demonstrated in figure 2. The larger the collectivity of the 1+ band head, the stronger the Coriolis coupling between this band and the y band. Indeed, this should be the case since according to equation (45) the coupling takes place only if the 1^+ state and the γ vibrational state contain identical quasiparticles in their structures. This is most probable for the collective state and table 2 confirms this assertion. On the other hand, this correlation clearly shows the importance of the residual interaction for description of the Coriolis coupling of 1,+ excitations with other states.

Fig. 2. The calculated reduced E2 matrix elements $\langle 0_{gr}^+ || M(E2) || 1_{\nu}^+ \rangle$ and Coriolis coupling matrix elements $\langle 2_{\nu}^+ || j^+ || 1_{\nu}^+ \rangle$ in 166 Er

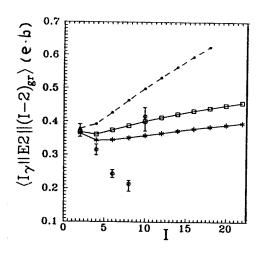
It should be also noted that the signs of the reduced E2 matrix elements $\langle 0_{gr}^+ \| M(E2) \| 1_{\nu}^+ \rangle$ and of the Coriolis coupling matrix elements $\langle 2_{\gamma}^+ \| j^+ \| 1_{\nu}^+ \rangle$ are mainly positive and negative, respectively, which means that the contribution of the 1_{ν}^+ states to the matrix element of equation (45) is quite coherent. This favors the nonadiabatic effects caused by coupling with the 1_{ν}^+ states.

The results of the microscopic calculations of the reduced E2 matrix elements for the $I_{\gamma} \rightarrow (I-2)_{gr}$ transitions in ¹⁶⁶Er as well as the experimental data [21] are shown in figure 3. The figure also includes calculations in the adiabatic approximation, i.e. without any Coriolis coupling. The microscopic calculations are performed with two values of the effective charge in the matrix element $M(E2)_{1+}$: $e_{eff} = 0.02$ and 0.3 (in matrix elements $M(E2)_{Q_0}$ and $M(E2)_{\gamma}$ we keep $e_{\rm eff} = 0.02$ in both cases). The value $e_{\rm eff} = 0.3$ was used to demonstrate the extremal case of very collective 1⁺ states. As is seen from figure 3, the calculations do not reproduce the deep minimum in the experimental data. So, the conventional (without γ deformation) Coriolis interaction obtained within the familiar RPA cannot account for the nonadiabatic behavior. It is necessary to take into account other effects like γ deformation. The γ deformation results in a mixing of the ground and γ bands and the corresponding enhancement of the Coriolis coupling should improve the description of the experimental data [21]. Such investigations are now in progress.

Since the main physical mechanism (Coriolis interaction) usually responsible for the $\Delta K = 1$

coupling is suppressed for the ground and 1^+ bands, these two bands can be used for investigation of more delicate effects (manifestation of γ deformation, etc.).

Fig. 3. The reduced E2 matrix elements for the $I_{\gamma} \rightarrow (I-2)_{\rm gr}$ transitions in $^{166}{\rm Er}$: o—experimental data, •—adiabatic calculations,—nonadiabatic calculations with $e_{\rm eff}=0.02$, *—nonadiabatic calculations with $e_{\rm eff}=0.3$ (see the text)



4. E1 TRANSITIONS IN ODD NUCLEI: INTERPLAY BETWEEN CORIOLIS INTERACTION AND COUPLING WITH CORE VIBRATIONS

The most wide and complete application of the model derived in the sect.2 takes place for odd nuclei. In this section two expressive examples of competition between the Coriolis interaction and coupling with core vibrations are analyzed.

The E1 transitions between the members of the $5/2^-$ [532] rotational band and the members of the $5/2^+$ [413] and $3/2^+$ [411] bands in 153,155 Eu and 155,157 Tb are of special interest because they have strong fluctuations amounting to two orders of magnitude. The models taking into account only the pairing and the Coriolis mixing, e.g. the nonadiabatic rotational model

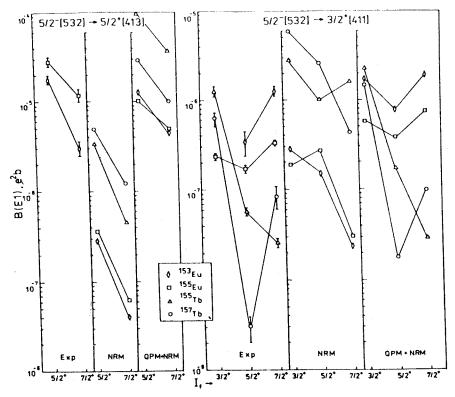


Fig. 4. The reduced probabilities of E1 transitions between the members of the $5/2^{-}[532]$ band and the $5/2^{+}[413]$ and $3/2^{+}[411]$ bands in $^{153,155}Eu$ and $^{155,157}Tb$ calculated within the NRM and the present model labeled as the QPM + NRM

Table 3. The Calculated Energies and Structure of Low-Lying Nonrotational States in ¹⁵³Eu

K^{π}	Energ	y, keV			Stru	cture		
	Exp.	Calc.						
5/2+	0	0	413↓	94%	$ \begin{array}{c c} 411 \downarrow + Q_{221} \\ 532 \uparrow + Q_{301} \end{array} $	3%, 0.1%	$523\uparrow + Q_{311}$ $541\uparrow + Q_{311}$	0.2% 0.03%
5/2	97	69	532↑	92%	$411 \uparrow + Q_{311} 402 \uparrow + Q_{301}$	0.8%, 0.3%	$413\downarrow+Q_{301}$	0.1%
3/2+	103	96	411↑	86%	$ \begin{array}{c c} 411 \downarrow + Q_{221} \\ 532 \uparrow + Q_{311} \end{array} $	6%, 0.6%	$523\uparrow + Q_{321}$ $541\uparrow + Q_{301}$	4%, 0.2%
3/2	637	448	541 †	84%	$550 \uparrow + Q_{221} \\ 422 \downarrow + Q_{301}$	5%, 1%	$420\uparrow + Q_{311}$ $411\uparrow + Q_{301}$	1.7%, 0.4%
7/2	_	467	523↑	86%	$\begin{array}{c} 411 \uparrow + Q_{321} \\ 404 \downarrow + Q_{301} \end{array}$	9%, 0.4%	$413\downarrow +Q_{311}$	0.4%
1/2	_	550	550↑	64%	$532 \uparrow + Q_{321} 541 \uparrow + Q_{221}$	10%, 8%	$420\uparrow + Q_{301}$	9%
1/2+	789	612	411↓	47%	$411\uparrow + Q_{221}$	27%	$413 \downarrow + Q_{221}$	22%
1/2+	635	645	420↑	76%	$550 \uparrow + Q_{201} 532 \uparrow + Q_{321}$	6%, 4%	$422 \downarrow + Q_{221} \\ 541 \uparrow + Q_{311}$	5%, 2%
5/2		915	523↓	0.3%	$532\uparrow + Q_{201}$	100%		Ì
5/2 ⁺	618	934	402↑	5%	$413 \downarrow + Q_{201}$	91%	$532 \uparrow + Q_{301}$	2.5%
5/2 ⁺	707	1118	402↑	16%	$532\uparrow + Q_{301}$	73%	$413 \downarrow + Q_{201}$	7%
7/2+	570	1609	404↓	63%	$523 \uparrow + Q_{301} 532 \uparrow + Q_{311}$	21%, 4%	$411\uparrow + Q_{221}$	7%

(NRM) [39], fail in the description of these transitions. The deviation of the calculated B(E1) values is up to two orders of magnitude of the experimental ones The hindrance factors are F >> 1 for $\Delta K = 0$ transitions and F << 1 for $\Delta K = 1$ transitions (see figure 4). As will be shown below, the use of the wave function (20) with quadrupole and octupole vibrational admixtures improves crucially the agreement with the experimental data [18].

The calculations have been done according to the prescription of Sec.2 but with the complicated version of the RPA, where the $K^{\pi} = 1^{-}0$ and $K^{\pi} = 1^{-}1$ one-phonon states are calculated with simultaneous use of the isoscalar octupole and isoscalar and isovector dipole forces as well as with extracting

Table 4. Attenuation Coefficients of the Coriolis Matrix Elements $(\alpha_{fit} = \langle f | H_{cor} | i \rangle_{fit} / \langle f | H_{cor} | i \rangle_{QPM} \quad \alpha_{QPM} = C_q^{\nu_i} C_q^{\nu_f})$

f i	¹⁵³ Eu		15.	⁵ Eu	155	Ть	¹⁵⁷ Tb		
	α_{fit}	аорм	α_{fit}	α_{QPM}	α_{fit}	α_{QPM}	α_{fit}	α _{QPM}	
523 ↑ 532 ↑	0.7	0.9	0.8	0.9	0.7	0.9	0.8	0.9	
532↑-541↑	0.6	0.9	0.6	0.9	0.6	0.9	0.7	0.9	
541 ↑550 ↑	0.8	0.7	0.7	0.7	0.8	0.7	0.8	0.6	
404↓-413↓	0.8	0.9	0.8	0.9	0.8	0.9	0.8	0.9	
402 411	0.4	0.4	0.5	0.7	0.7	0.8	0.6	0.7	
411 1 420 1	0.5	0.8	0.6	0.7	0.9	0.8	0.8	0.8	

spurious admixtures caused by the violation of the transitional invariance of the Hamiltonian [18,40].

The calculations have shown that the dominating contribution to E1 transition matrix element for the odd nuclei comes (due to the octupole admixtures) from the E1 transition $0^+0_{gr} \rightarrow 1^-K_1$ in even-even core. The influence on this transition of the «tail» of giant dipole resonance (GDR) can be estimated by calculating the contribution to the E1 transition matrix element (34) of the q_1q_2 terms with energies $\epsilon_1+\epsilon_2$ from the GDR region. The contribution turns out to be 91-97% both for $\Delta K=0$ and 1 [40]. Thus just the «tail» of GDR causes $0^+0_{gr} \rightarrow 1^-K_1$ transitions whereas low-energy two-quasiparticle configurations mixed by octupole forces determine main structure of the 1^-K_1 states.

In table 3 the calculated energies and structure of low-lying nonrotational states in ¹⁵³Eu are presented. It is seen that the level energies are reproduced rather well. The main vibrational admixtures are, as a role, of quadrupole character whereas the octupole admixtures amount usually of several percent and less. The vibrational admixtures lead to decrease of the amplitude of main one-quasiparticle component, and as a result, to the attenuation of the Coriolis-mixing matrix elements. Table 4 shows that just this effect can be the main reason of the Coriolis attenuation at low spins.

The results of our calculations for the B(E2) values (labeled as QPM + NRM) as compared with the results of the NRM and experimental data (see refs.in [18]) are shown in figure 4. It is seen that the NRM does not provide even a qualitative description of the E1 transitions. On the contrary, the QPM + NRM gives the excellent agreement with the experimental data. It is remarkable, that inclusion of the vibrational admixtures leads to more than

an order of magnitude increase in the $\Delta K = 0$ transitions and simultaneously provides a deep minimum in the $\Delta K = 1$ transition in ¹⁵⁷Tb.

For understanding of the obtained results the different parts of the E1 transition matrix element (36) have been analyzed (see table 5 and details in ref. [18]). It turns out that the E1 ($\Delta K = 0$) transitions in the Eu nuclei are mainly accomplished between principal K-components of initial and final states. These transitions are very enhanced due to the coupling with eveneven core (see $C \cdot D$ term in (36)). On the other hand, in describing E1 ($\Delta K = 1$) transitions in 157 Tb it is important to take into account not only principal but also small Coriolis-mixing components. Then, both $\Delta K = 1$ and $\Delta K = 0$ terms will contribute to the total E1 ($\Delta K = 1$) transition. Moreover, due to large intrinsic matrix element the contribution to the total E1 ($\Delta K = 1$) transition from the $\Delta K = 0$ term turns out to be considerable. Because of different signs of $\Delta K = 1$ and $\Delta K = 0$ contributions to the total E1 ($\Delta K = 1$) matrix element we have a mutual compensation which just explains the deep minimum in $B(E1, \Delta K = 1)$ values for 157 Tb.

As can be seen from table 3 the octupole admixtures in wave functions are rather small. Thus, our calculations show that even small octupole admixtures in the wave functions of odd nuclei influence very much E1 transitions and, in particular, can enhance B(E1) values to an order of magnitude. Earlier, the similar results have been obtained for small quadrupole admixtures in wave functions of odd nuclei [12]. It was shown that even very small quadrupole admixtures (about 1%) can dramatically influence E2 transitions in some odd nuclei.

It is clear that large collectivity of octupole $K^{\pi}=0^-$ and 1^- states in even-even core lead to large octupole admixtures in wave functions of corresponding odd nucleus and, as a result, to strong effects like ones considered above. Nuclei at the onset of the rare-earth region have the most collective octupole low-lying states [1,13,41]. The nuclei considered above belong just to this group. But what will be for more heavy odd nuclei? Do octupole admixtures influence much E1 transitions in these nuclei also? In general, this does not seem to be the case since for heavier nuclei the low-lying octupole states in even-even cores are usually less collective. Also, some calculations for E1 transitions in odd nuclei of this sector show that often E1 transitions are satisfactorily described without taking into account octupole admixtures [41]. Nevertheless, we will demonstrate that in some cases the octupole admixtures play crucial role in description of E1 transitions for more heavy nuclei as well.

Let us consider dipole $I_i^+ 9/2[624] \rightarrow I_f^- 7/2[514]$ transitions in ¹⁷⁷Hf, the data for which are given at table 6. Numerous calculations are devoted to

Table 5. Structure of the Reduced E1 Matrix Elements $M(E1, I_i^{\pi_i} \to I_f^{\pi_f}) = \langle I_f^{\pi_f} | | E1 | | I_i^{\pi_i} \rangle / \sqrt{2I_i + 1} \text{ (see exp. (32)) Between }$ Members of the $5/2^-[532]$ Band and $5/2^+[413]$ and $3/2^+[411]$ Bands in 153 Eu and 151 Tb. $(M_{fi}(E1) = (\Psi_f (K_f^{\pi_f}) \hat{M}(E1, \mu = K_f \pm K_i) \Psi_i (K_i^{\pi_f})),$ $F = B(E1)_{\text{exp}} / B(E1)_{QPM+NRM}, \ a_{if} = b_{K_f Y_f}^{I_f} b_{K_f Y_i}^{I_i} (I_i \pm K_i 1 \mu | I_f K_f)$

			153 Eu , <i>I</i>	$I_i^{\pi_i} 5/2[53]$	$32] \to I_f^{\pi_f} 5/$	2[413], 4	$\Delta K = 0$		
$I_i^{\pi_i}$	$rac{\pi_f}{I_f}$			5/2" → 5	5/2 ⁺	5/2 → 7	7/2+	11/2 →	9/2+
f	i	ΔΚ	$M_{fi}(E1)$ $10^{-2} \mathrm{e} \cdot \mathrm{fm}$	a_{if}	$a_{ij}M_{fi}(E1)$ $10^{-2} \mathrm{e\cdot fm}$	a _{if}	$a_{if}M_{fi}(E1)$ $10^{-2} \text{ e} \cdot \text{fm}$	a _{if}	$\frac{a_{if}M_{fi}(E1)}{10^{-2}\mathrm{e\cdot fm}}$
404	. —523↑	0	-27.4				_	-0.031	0.84
413	↓ —523 †	1	1.5			_		0.199	0.30
413,	↓ <i>—5</i> 32↑	0	-4.4	0.832	-3.68	0.519	-2.29	-0.521	2.30
413,	↓—541 †	1	0.6	-0.083	0.04	0.130	-0.06	0.097	-0.05
	† <i>—5</i> 32 †	0	71.0	0.002	0.14	0.005	0.31	-0.0010	-0.58
411	† —532 †	1	-2.4	0.034	-0.08	0.020	-0.05	0.066	-0.16
411	† —541 †	0	-7.4	0.005	-0.04	0.010	-0.07	-0.024	0.18
M(E	$E1, I_i^{\pi_i} \rightarrow I$	$f^{\pi_{f}}$		-3.62 · 1	0 ⁻² e·fm	-2.62·1	0 ⁻² e·fm	3.84 · 1	0 ⁻² e·fm
B(E	$1, I_i^{\pi_i} \to I_f$	T _(f)		1.8(2)	$\cdot 10^{-5} e^2 b$	3.0(6)	$\cdot 10^{-6} e^2 b$	8.0(14	$10^{-6} e^2$
F				0.7		2.6		1.0	
			¹⁵⁷ Tb,	$I_i^{\pi_i} 5/2[5]$	$32] \rightarrow I_f^{\pi_f} 3/$	2[411],	$\Delta K = 1$		
$I_i^{\pi_i}$	$\rightarrow I_f^{\pi_f}$			5/2 →			5/2 ⁺	5/2 →	7/2+
f	i	ΔΚ	$M_{fi}(E1)$ $10^{-2} \mathrm{e} \cdot \mathrm{fm}$	a_{if}	$a_{if}M_{fi}(E1)$ $10^{-2} e \cdot fm$	a _{if}	$a_{if}M_{fi}(E1)$ $10^{-2} e \cdot fm$	a _{if}	$a_{if}M_{fi}(E1110^{-2} e \cdot fn$
413	↓532↑	0	6.4	_		0.038	0.24	0.037	0.24
	↑—532↑	0	13.0			0.026	0.33	0.025	0.32
	↑532↑	1	0.6	0.813	0.47	0.531	0.31	0.216	0.13
411	† —541 †	0	-17.4	-0.044	0.77	0.043	-0.75	0.059	-1.02
420	† —541 †	1	3.7	0.002	0.01	0.003	0.01	0.002	0.01
				1.25	10 ⁻² e∙fm	0.14	10 ⁻² e·fm	-0.32 · 1	0-2 e·fm
	$E1, I_i^{\pi_i} \rightarrow I$	$(\frac{\pi_f}{f})$		1.20					
M(1	$E1, I_i^{\pi_i} \to I$ $E1, I_i^{\pi_i} \to I_j$,			$2)\cdot 10^{-7} e^2 b$	3.1(13	$3)\cdot 10^{-9} e^2 b$	8.4(24	$1) \cdot 10^{-8} e^2 t$

Table 6. Energies and Structure of Low-Lying States in ¹⁷⁷Hf

Κ ^π		Energy, keV	/		Structure, %					
	exp.	IQM*	QPM							
7/2	0	0	0	514↓	97.3	$512\downarrow +Q_{221}$	2.1			
9/2+	321.3	294	353	624↑	98.8					
5/2	508.1	711	542	512↑	95.5	$510\uparrow +Q_{221}$	2.1			
5/2	_	1994	1542	{-523↓	9.5	$512\uparrow +Q_{201}$ $521\uparrow +Q_{221}$	83.1 7.0			
1/2	559.4	783	585	{521 ↓ 510 ↑	83.1 5.4	$523\downarrow +Q_{221}$ $521\uparrow +Q_{221}$	2.7 4.1			
1/2	(567)	1111	604	{510↑ {521↓	71.6 7.3	$512\downarrow +Q_{221}$ $512\uparrow +Q_{221}$	12.1 7.0			
7/2+	745.9	801	796	633 †	95.7	651 † +Q ₂₂₁	2.5			
3/2	805.7	1486	780	{-512↓	66.2	$510\uparrow +Q_{221}$ $514\downarrow +Q_{221}$	16.2 14.7			
3/2	(1502)	2066	1284	{ -521 ↑	42.0	$521 \downarrow +Q_{221}$ $633 \uparrow +Q_{321}$	41.2 14.4			
5/2 ⁺		1132	951	{-642↑	89.4	$660\uparrow +Q_{221}$ $624\uparrow +Q_{221}$	5.5 1.3			
7/2	1057.8	1883	1213	{-503↑	22.2	$514 \downarrow +Q_{201}$ $501 \uparrow +Q_{221}$	74.2 2.2			
7/2	_		1457	{-503↑	61.9	$514 \downarrow +Q_{201}$ $501 \uparrow +Q_{221}$	25.8 7.0			
3/2	1434	3673	1536	{-501 ↑	52.7	$503 \uparrow + Q_{221}$ $514 \downarrow + Q_{221}$	23.3 15.2			

^{*} Energies calculated within Independent Quasiparticle Model.

these transitions (see, for example, [25,42,43]) with the main purpose of explanation of extremely small experimental value of $B(E1, 9/2^+ \rightarrow 7/2^-)$. Though these calculations have not provided a good description of the experimental data, they, nevertheless, have shown that both the Coriolis interaction and octupole admixtures have to be allowed for. Calculations [25,42,43] take into account the coupling with octupole core vibrations. Nevertheless, they have serious shortcomings: 1) the octupole phonons are

Table 7. Hindrance Factors $F = B(E1)_{\text{exp}}/B(E1)_{\text{theor}}$ for E1 Transitions $I_i^+9/2[624] \rightarrow I_f^-7/2[514]$ in ¹⁷⁷Hf (see comments in the text)

ΔJ	$J_i^{\pi} \rightarrow J_f^{\pi}$	E_{γ} , keV	$B(E1)_{\rm exp}$, $10^{-7} {\rm e}^2 {\rm b}$		F	
				a	b	С
-1	21/2 ⁺ → 19/2 ⁻	283.4	9.32(29)	0.73	2.42	0.89
	$19/2^+ \rightarrow 17/2^-$	292.5	7.46(27)	0.74	2.59	0.91
	$17/2^+ \rightarrow 15/2^-$	291.4	6.06(9)	0.68	2.56	0.86
	$15/2^+ \rightarrow 13/2^-$	299.0	3.93(25)	0.66	2.77	0.92
	$13/2^+ \rightarrow 11/2^-$	305.5	1.79(3)	0.65	3.48	1.12
	$11/2^+ \rightarrow 9/2^-$	313.7	0.495(66)	0.27	3.78	1.16
	$9/2^+ \to 7/2^-$	321.3	0.0393(39)	10.3	1.40	0.88
0	$19/2^+ \rightarrow 19/2^-$	69.2	7,67(20)	1.03	2.82	0.19
	$17/2^+ \rightarrow 17/2^-$	88.4	8,32(10)	1.06	2.85	0.30
	$15/2^+ \rightarrow 15/2^-$	117.2	9.58(10)	1.00	2.67	0.38
	$13/2^+ \rightarrow 13/2^-$	145.8	9.16(7)	1.11	2.92	0.54
	$11/2^+ \rightarrow 11/2^-$	177.0	9.11(57)	1.10	2.86	0.66
	9/2 ⁺ → 9/2	208.3	6.74(38)	1.15	2.98	0.82
+1	9/2 ⁺ → 11/2 ⁻	71.7	2.44(23)	1.52	4.10	1.92

included by phenomenological way; 2) the calculations for E1 transitions are not followed to description of the low-energy spectrum in 177 Hf.

More realistic microscopic calculations have been performed recently [19] within the model given in section 2. The calculations of B(E1) values have been done following to three prescriptions: with the Coriolis interaction only (a), with both the Coriolis interaction and coupling with core quadrupole and octupole vibrations (b), improved version of (b) where E1 matrix elements L_g^{E1} for even-even core were calculated taking into account the «tail» of the GDR (c).

The results obtained are presented at tables 6 and 7. It is seen that they are in quite satisfactory agreement with experimental data for both the energy spectrum and B(E1) values. The most important result is that inclusion of octupole admixtures dramatically improves description of the $B(E1, 9/2^+ \rightarrow 7/2^-)$ value as compared with the case where the Coriolis coupling is taken into account only. Simultaneously, description of other transitions remains to be quite appropriate.

Thus, our calculations show that the most correct way of description of E1 transitions in rare-earth odd nuclei is a simultaneous use of the Coriolis interaction and coupling with even-even core vibrations. Just interplay of these two interactions leads to anomalous behavior of E1 transitions. The microscopic

scheme presented in section 2 provides satisfactory description of both electrical transitions and low-energy spectrum. Moreover, in the framework of this scheme the calculations for odd nuclei are consistent with calculations for neighbour even-even nuclei.

5. STRUCTURE OF LOW-LYING STATES IN ODD-ODD 166Ho

Results presented here [9] are the first systematic application of the model described in sec.2 to odd-odd nuclei. At this first stage the coupling with core vibrations is taken into account only. The calculations with the Coriolis interaction are in progress and will be presented later. The calculations presented here have been performed for the states with excitation energy up to 0.5 MeV in isotopes ^{160–168}Ho. The results of systematic microscopic calculations within the same model for neighbouring odd and even nuclei can be found in [14,20] and [13], respectively. For the sake of brevity we present here only results for ¹⁶⁶Ho. Details of the calculations are given in [9].

The calculated energies and structure of nonrotational states in 166 Ho are presented in table 8. For each level two theoretical values are given: $E'_{th} =$

$$=\eta_{\nu\gamma}-\eta_{\nu_0\gamma_0} \text{ and } E_{\text{th}}=\eta_{\nu\gamma}-\eta_{\nu_0\gamma_0}+\frac{h^2}{2J}(I^2-K_{I=K}^2)-\frac{h^2}{2J}(I^2-K_{I=K_0}^2). \text{ It is }$$

seen that the model provides satisfactory description of the energy spectrum (together with the spectrum of the neighbouring odd nuclei, see ref. [20]). The most interesting result of the calculations is the existence in low-lying states of rather large vibrational admixtures. The simple estimations (like those for odd nuclei in [12]) with using the amplitudes of components of the states from table 8 show that these vibrational admixtures influence very much on E2 and E1 transitions. We have quite the same situation as in odd nuclei. This is not surprising since matrix elements of $E\lambda$ transitions in odd and odd-odd nuclei have similar structure (see (36) and (37)).

Table 8. The Level Energies and Structure of Low-Lying States in 166Ho

K ^π	Structure	%	$E_{ m exp}$ $E_{ m Th}$ $E_{ m Th}$ (keV)	K ⁿ	Structure	%	$E_{ m exp} \ E_{ m Th} \ E_{ m Th} \ m (keV)$
0	7/2 523-7/2 633	89%	0	7	7/2 523+7/2 633	79%	6
	$7/2523-3/2651-Q_{22}^{+}$	10%	0		$7/2523+3/2651+Q_{22}^{+}$	11%	-45
			0		$3/2541+7/2633+Q_{22}^{+}$	5%	18
					$7/2523+11/2615-Q_{22}^{+}$	3%	

Κ ^π	Structure	%	$E_{\rm exp}$ $E_{\rm Th}$ $E_{\rm Th}$ (keV)	Κ ^π	Structure	%	$E_{ m exp} \ E_{ m Th} \ ({ m keV})$
5	7/2 523+3/2 651 3/2 541+7/2 633 7/2 523+7/2 633-Q ₂₂ ⁺	81% 12% 6%	215 260	2	7/2 523-3/2 651 3/2 541-7/2 633 7/2 523-7/2 633 $\pm Q_{22}^{+}$	66% 5% 26% 7%	(543) 507 525
3 ⁺	7/2 523-1/2 521 3/2 541-1/2 521+Q ₂₂	92% 4%	191 178	4+	$3/2541+1/2521+Q_{22}^{+}$	92% 4% 2%	372 222 258
6 ⁺	$3/2 \cdot 411-1/2 \cdot 521+Q_{32}^+$ $7/2 \cdot 523+5/2 \cdot 512$ $7/2 \cdot 523+5/2 \cdot 523$ $7/2 \cdot 523+9/2 \cdot 624-Q_{32}^+$ $7/2 \cdot 523+1/2 \cdot 660+Q_{32}^+$	2% 82% 3% 5% 2%	205 295 263 317	1*	$3/2 ext{ 411+1/2 } 521+Q_{32}^{+}$ $7/2 ext{ 523-5/2 } 512$ $7/2 ext{ 523-5/2 } 523$ $7/2 ext{ 523-9/2 } 624+Q_{32}^{+}$ $7/2 ext{ 523-1/2 } 660-Q_{32}^{+}$ $7/2 ext{ 523-1/2 } 400-Q_{32}^{+}$	80% 18% 1% 1%	426 411 420
1	7/2 523+1/2 400+ Q_{32}^+ 3/2 411-1/2 521 3/2 411-5/2 642+ Q_{32}^+ 3/2 411+3/2 651- Q_{32}^+ 5/2 523+1/2 521- Q_{32}^+	95% 1% 1%	351 354 363	2	3/2 41 1+1/2 521 $7/2$ 523+1/2 521- Q_{32}^+ $3/2$ 541+1/2 521+ Q_{30}^+	94% 2.5% 1%	563 % 526 544
0	$3/2 541-1/2 521+Q_{30}^+$ $1/2 411-1/2 521$ $1/2 411+3/2 521-Q_{22}^+$	1% 96% 2%	525 560	i ⁻	$1/2 \ 411+1/2 \ 521$ $1/2 \ 411-3/2 \ 521+Q_{22}^+$	96% 2% 1%	373 381 390
5 ⁺	$3/2 411+1/2 521-Q_{22}^+$ $7/2 523+3/2 521$ $3/2 411+7/2 633$ $7/2 523+7/2 633-Q_{32}^+$ $7/2 532+7/2 514-Q_{22}^+$	1% 70% 21% 5% 3%	560 264 259 304	2+	$3/2 411 - 7/2 633$ $7/2 523 - 7/2 514 + Q_{22}^+$ $7/2 523 - 7/2 633 + Q_{32}^+$	79% 1% 6% 5%	430 409 427
1*	7/2 523-5/2 512 $7/2 523-9/2 624-Q_{32}^+$ $3/2 541-5/2 523+Q_{22}^+$	71 % 13 % 4 % 3 %	567 554 563	64	7/2 523+1/2 521- Q_{22}^+ 7/2 523+5/2 523 7/2 523+5/2 512 7/2 523+9/2 624- Q_{32}^+ 3/2 541+5/2 523+ Q_{22}^+	2% 72% 11% 5% 3%	 660 714
2*	7/2 523-1/2 530- Q_{22}^+ 7/2 523-1/2 651- Q_{32}^+ 3/2 411-7/2 633 7/2 523-3/2 521	2% 2% 82% 14%	— 646	5 ¹	7/2 523+1/2 $651-Q_{32}^+$ 7/2 523+1/2 $530+Q_{22}^+$ 7/2 523+1/2 633 7/2 523+3/2 521	2% 2% 82% 13%	

Κ ^π	Structure	%	$E_{ m exp}$ $E_{ m Th}$ $E_{ m Th}$ (keV)	Κ ^π	Structure	%	E _{exp} E' _{Th} E _{Th} (keV)
	3/2 411-3/2 651+Q+	4%	664		3/2 411+3/2 651+Q ₂₂	5%	653
0+	$7/2\ 404-7/2\ 633$ $7/2\ 404-3/2\ 651-Q_{22}^{+}$	75% 14%	803 839	7 ⁺	7/2 404+7/2 633 7/2 404+3/2 651+Q ₂₂ +	75% 14%	915 915
	$7/2 \ 404-11/2 \ 505-Q_{32}^+$ $3/2 \ 402-7/2 \ 633-Q_{22}^+$	4% 3%	839		$7/2 \ 404+11/2 \ 505-Q_{32}^+$ $3/2 \ 402+7/2 \ 633+Q_{32}^+$	3.5% 3%	975
2	3/2 541-7/2 633 7/2 523-7/2 633+Q ₂₂ ⁺ 1/2 550-7/2 633-Q ₂₂ ⁺ 3/2 541-3/2 651+Q ₂₂ ⁺	70% 10% 8% 5%	708 726	5	3/2 541+7/2 633 7/2 523+7/2 633-Q ₂₂ ⁺ 1/2 550-7/2 633-Q ₂₂ ⁺ 3/2 541+3/2 651+Q ₂₂ ⁺	73% 9% 7% 5%	- 815 , 860
2	7/2 523-11/2 615 7/2 523-7/2 633+ Q_{22}^+ 7/2 523-7/2 504+ Q_{32}^+	78% 12% 6%	 1131 1149	9"	7/2 523+11/2 615 7/2 523+7/2 633+Q ⁺ ₂₂ 7/2 523+7/2 504+Q ⁺ ₃₂	77% 14% 9%	 1082 1154

Table 9. The $\log ft$ of β _ Transitions Leading to the Low-Lying 1⁺ States in Odd-Odd ^{166,168}Ho Isotopes

Daughter nucleus	Final level E [keV], I^{π}	$\left C_{\pi 7/2[523], \nu 5/2[523]}^{1+}\right ^2$	log <i>ft</i> Theory	log <i>ft</i> Experiment	
¹⁶⁶ Ho	426.0(1 ⁺)	0.18	4.96	5.12	
¹⁶⁸ Ho	192.5(1+)	0.02	5.86	5.50	
¹⁶⁸ Ho	630.4(1 ⁺)	0.66	4.34	4.60	

The calculations for Ho isotopes show that the main strength of the γ vibrations built on the ground state configurations is concentrated in intrinsic states with excitation energies above 1 MeV. An exception to this generality is the 2^- (525 keV) state in 166 Ho which has a 26% of the γ vibrational component. Recently, a $2^-\gamma$ vibrational band was suggested [44] in 166 Ho with a band head at 543 keV which is in rather nice agreement with our calculations. It is interesting that up to the present theré is no conclusive experimental evidence for the calculated 5^- (260 keV) state.

The mixing of the neutron-proton configurations with the same K^{π} should be noted. The mixing is caused by the quasiparticle-phonon interaction. Such kind of the mixing (do not confuse this with the Coriolis

mixing) is well known in odd nuclei but has not been calculated before in odd-odd nuclei. This effect can be very important for the study of the structure of low-lying states in odd-odd nuclei. For example, just the admixture of the spin-flip configuration $1^+\{\pi7/2[523], \nu5/2[523]\}$ to the low-lying states in odd-odd 166,168 Ho explains the low experimental values of log ft in these nuclei [9]. The results of corresponding calculations are presented in table 9.

6. CONCLUSIONS

The extending of the Quasiparticle-Phonon Model is proposed by taking into account the rotation-vibration coupling in even-even, odd and odd-odd nuclei. This extending is an important step in derivation of general microscopic model for description of vibrational and rotational degrees of freedom in strictly deformed nuclei on the same microscopic footing. Three examples of calculations for even-even, odd and odd-odd nuclei are considered.

- 1) In 166 Er the Coriolis interaction between ground and γ bands through low-lying 1^+ states (together with the «scissors» mode) is analyzed as a possible origin of the nonadiabatic effects in $E2(\gamma \rightarrow gr)$ transitions [24]. It is shown that the Coriolis coupling between ground and 1^+ bands is absent within the RPA for axially deformed nuclei. This is rather unexpected result of general character, which was not mentioned before in spite of intensive investigation of the «scissors» mode. Therefore, the Coriolis coupling can exist and lead to the nonadiabatic effects in 166 Er only under some special conditions, for example, if a triaxiality of this nucleus takes place. The contribution of the «scissors» mode to the nonadiabatic effects in $E2(\gamma \rightarrow gr)$ transitions can be much more noticeable in nuclei like 172 Yb. Due to a small collectivity of the γ -vibrational state in such nuclei direct E2 transition $(2^+_{\gamma} \rightarrow 0^+_{gr})$ is weak and, as a result, the effects of indirect (due to the Coriolis interaction) E2 transitions should be larger.
- 2) The strong influence of small octupole vibrational admixtures in the wave functions of odd nuclei on the E1 transitions in Eu—Tb isotopes and in 177 Hf was shown [18,19]. It was demonstrated that the anomalous behavior of E1 transitions in these nuclei can be explained by the competition between the quasiparticle-phonon and Coriolis interaction effects. It should be noted that the model provides the possibility for simultaneous description of electrical transition and energy spectrum in odd nuclei.
- 3) In low-lying states of odd-odd ¹⁶⁶Ho rather large vibrational admixtures are predicted as well as the mixing of neutron-proton configurations due

to the quasiparticle-phonon interaction. Both the effects are quite important for the study of level structure, E1 and E2 transitions and β transitions in odd-odd nuclei.

7. APPENDIX

In subsection 2.1 the following functions characterizing the RPA phonons are used:

$$\psi_{q_{1}q_{2}}^{g} = \sqrt{\frac{1 + \delta_{\mu,0}}{2\tilde{Y}_{\tau}^{g}}} \frac{f_{q_{1}q_{2}}^{\lambda\mu} u_{q_{1}q_{2}}^{(+)}}{\varepsilon_{q_{1}q_{2}} - \omega_{g}}, \tag{61}$$

$$\varphi_{q_{1}q_{2}}^{g} = \sqrt{\frac{1 + \delta_{\mu,0}}{2\tilde{Y}_{x}^{g}}} \frac{f_{q_{1}q_{2}}^{\lambda\mu} u_{q_{1}q_{2}}^{(+)}}{\varepsilon_{q_{1}q_{2}} + \omega_{g}}, \tag{62}$$

$$X_{\tau}^{g} = (1 + \delta_{\mu,0}) \sum_{q_{1}q_{2} \in \tau} \frac{(f_{q_{1}q_{2}}^{\lambda\mu} u_{q_{1}q_{2}}^{(+)})^{2} \varepsilon_{q_{1}q_{2}}}{\varepsilon_{q_{1}q_{2}}^{2} + \omega_{g}^{2}},$$
 (63)

$$\widetilde{Y}_{\tau}^{g} = Y_{\tau}^{g} + Y_{-\tau}^{g} \left\{ \frac{1 - (\kappa_{0}^{(\lambda\mu)} + \kappa_{1}^{(\lambda\mu)}) X_{\tau}^{g}}{(\kappa_{0}^{(\lambda\mu)} - \kappa_{1}^{(\lambda\mu)}) X_{-\tau}^{g}} \right\}^{2}, \tag{64}$$

where

$$Y_{\tau}^{g} = (1 + \delta_{\mu,0}) \sum_{q_{1}q_{2} \in \tau} \frac{(f_{q_{1}q_{2}}^{\lambda\mu} u_{q_{1}q_{2}}^{(+)})^{2} \varepsilon_{q_{1}q_{2}} \omega_{g}}{(\varepsilon_{q_{1}q_{2}}^{2} + \omega_{g}^{2})^{2}}$$
(65)

and the secular equation for determining the one-phonon energies ω_g is

$$1 - (\kappa_0^{(\lambda\mu)} + \kappa_1^{(\lambda\mu)}) (X_{\tau}^g + X_{-\tau}^g) + 4\kappa_0^{(\lambda\mu)} \kappa_1^{(\lambda\mu)} X_{\tau}^g X_{-\tau}^g = 0.$$
 (66)

Here, $\varepsilon_{q_1q_2} = \varepsilon_{q_1} + \varepsilon_{q_2}$. For $\lambda\mu = 20$ the expressions (61)—(66) are more complicated since in this case the interaction in particle-particle channel is embraced to extract the spurious admixtures connected with particle number nonconservation. The corresponding expressions can be found in refs. [1,2,10].

The functions $\Gamma^{\text{ph}}_{gq_1q_2}(\tau)$, $\Gamma^{\text{pair}(+)}_{iq_1q_2}(\tau)$ and $\Gamma^{BB}_{\lambda\mu q_1q_2{q'}_1{q'}_2}(\tau)$ involved in (11)—(13) have the form

$$\Gamma^{\text{ph}}_{gq_{1}q_{2}}(\tau) = \sqrt{\frac{2}{\widetilde{\gamma}_{s}}} f_{q_{1}q_{2}}^{\lambda\mu} v_{q_{1}q_{2}}^{(-)}, \tag{67}$$

$$\Gamma_{iq_{1}q_{2}}^{\text{pair}(+)}(\tau) = 1/\sqrt{2} G_{\tau} u_{q_{1}}^{} v_{q_{1}}^{} (u_{q_{2}}^{2} - v_{q_{2}}^{2}) \psi_{q_{1}q_{2}}^{20i}, \tag{68}$$

$$\Gamma_{iq_{1}q_{2}}^{\mathsf{pair}(-)}(\tau) = 1/\sqrt{2} \ G_{\tau} \ u_{q_{1}} \mathsf{v}_{q_{1}} \ (u_{q_{2}}^{2} - \mathsf{v}_{q_{2}}^{2}) \ \varphi_{q_{1}q_{2}}^{20i} \tag{69}$$

and

$$\Gamma^{BB}_{\lambda\mu q, q', q', q'_2}(\tau) = f^{\lambda\mu}_{q_1 q_2} f^{\lambda\mu}_{q'_1 q'_2} v^{(-)}_{q_1 q_2} v^{(-)}_{q'_1 q'_2}. \tag{70}$$

Further,

$$\Gamma_{gq_1q_2}(\tau) = \sqrt{\frac{2}{\widetilde{Y}_{\tau}^g(1+\delta_{K,0}\left(1-\delta_{\mu,0}\right))}}\widetilde{f}_{q_1q_2}^{\lambda\mu}v_{q_1q_2}^{(-)} -$$

$$- \delta_{q_1 q_2} \delta_{\lambda \mu, 20} \sqrt{2} G_{\tau} u_{q_1} v_{q_1} \sum_{q \in \tau} (u_q^2 - v_q^2) \sum_i (\psi_{qq}^{20i} + \phi_{qq}^{20i}), \tag{71}$$

where we have for the operator of electrical type $\hat{f}^{\lambda\mu}$

$$\widetilde{f}_{q,q_{2}}^{\prime \mu} = \langle \widetilde{q}_{1} \mid \widehat{f}^{\lambda \mu} \mid \widetilde{q}_{2} \rangle \left(\delta_{\sigma_{1},\sigma_{2}} - \sigma_{1} \delta_{1} \sigma_{1}, -\sigma_{2} \right) \tag{72}$$

(the same expression is for $\widetilde{p}_{q_1q_2}^{\lambda\mu}$) and for the operator of magnetic type \hat{j}^+

$$\widetilde{j}_{q_{1}q_{2}}^{+} = \langle \widetilde{q}_{1} \mid \widehat{j}^{+} \mid \widetilde{q}_{2} \rangle (\sigma_{1} \delta_{\sigma_{1},\sigma_{2}} + \delta_{\sigma_{1},-\sigma_{2}}). \tag{73}$$

The coefficient $k_{\gamma\gamma'}^{CC}$ from (37) is equal to 1 except for the cases

$$k_{\gamma\gamma'}^{CC} = \begin{pmatrix} \frac{1}{\sqrt{2}} \left(\delta_{\sigma_s,+1} \delta_{\sigma_r,-1} - \gamma \delta_{\sigma_s,-1} \delta_{\sigma_r,+1} & \text{for } K = 0, K' \neq 0 \\ \frac{1}{\sqrt{2}} \left(\delta_{\sigma_s,+1} \delta_{\sigma_r,-1} - \gamma' \delta_{\sigma_s,-1} \delta_{\sigma_r,+1} & \text{for } K \neq 0, K' = 0 \end{pmatrix}$$
(74)

and the coefficient $k_{\gamma_q\gamma_1'}^{DD}$ is equal to $k_{\mu}^{K'}$ k_{μ}^{K} $(1+\delta_{K,0}\delta_{K',0}(1-\delta_{\mu,0}))$ except for the cases

$$k_{\gamma\gamma'}^{DD} = \begin{pmatrix} \frac{1}{\sqrt{2}} k_{\mu}^{K'} (\delta_{\sigma_{s'}+1} \delta_{\sigma_{r'}-1} - \gamma \delta_{\sigma_{s'}-1} \delta_{\sigma_{r'}+1} & \text{for } K = 0, K' \neq 0 \\ \frac{1}{\sqrt{2}} k_{\mu}^{K} (\delta_{\sigma_{s'}+1} \delta_{\sigma_{r'}-1} - \gamma' \delta_{\sigma_{s'}-1} \delta_{\sigma_{r'}+1} & \text{for } K \neq 0, K' = 0 \end{pmatrix}$$
(75)

ACKNOWLEDGEMENT

The author is grateful to Profs. V.G.Soloviev, I.N.Mikhailov, V.M.Mikhailov, R.Sheline, Drs. N.A.Bonch-Osmolovskaya, B.A.Alikov, C.Fahlander, J.Kvasil, R.Kulessa, R.Nazmitdinov, P.N.Usmanov and A.A.Okhunov for fruitful discussions, collaboration and help.

REFERENCES

- Soloviev V.G. Theory of Complex Nuclei, Moscow, Nauka, 1971 (transl. Pergamon Press, 1976).
- Soloviev V.G. Theory of Atomic Nuclei (Quasiparticles and Phonons), Moscow, Energoatomizdat, 1989 (transl. Institute of Physics Publishing, Bristol and Philadelfia, 1992.
- 3. Soloviev V.G., Nesterenko V.O., Bastrukov S.I. Z.Phys., 1983, A309, p.353.
- 4. Soloviev V.G. Phys.Lett., 1966, 21, p.320.
- 5. Boisson J.P., Peipenbring R., Ogle W. Phys.Rep., 1976, 26, p.99.
- 6. Paar V. Nucl. Phys., 1979, A331, p.16.
- 7. Bennour L., Libert J., Meyer V., Quentin P. Nucl. Phys., 1987, A465, p.35.
- 8. Kvasil J., Nesterenko V.O., Hrivnacova I. Czech J. Phys., 1991, 41, p.345.
- 9. Kvasil J., Sheline R.K., Nesterenko V.O., Hrivnacova I., Nosek D. Z.Phys.A, 1992, 343, p.145.
- Nesterenko V.O., Soloviev V.G., Sushkov A.V. JINR Preprint, P4-86-115, Dubna, 1986.
- 11. Soloviev V.G. Z.Phys., 1989, A334, p.143.
- Bastrukov S.I., Nesterenko V.O. Proc. Intern. Symp. on In-Beam Nucl. Spectr., Debrecen, Hungary, 1984, p.689.
- Grigorjev E.P., Soloviev V.G. Structure of Even Deformed Nuclei, Moscow, Nauka, 1974.
- 14. Gareev F.A., Ivanova S.P., Soloviev V.G., Fedotov S.I. Part. Nuclei, 1973, 4, p.357.
- Ivanova S.P., Komov A.L., Malov L.A., Soloviev V.G. Izv.Akad.Nauk SSSR, Ser.Fiz., 1973, 37, p.911; 1975, 39, p.1612.
- 16. Gareev F.A., Ivanova S.P., Soloviev V.G., Fedotov S.I. Nucl. Phys., 1971, A171, p.134.
- 17. Bonch-Osmolovskaya N.A., Morozov V.A., Nesterenko V.O. Izv.Akad.Nauk SSSR, Ser.Fiz., 1985, 49, p.843.
- Alikov B.A., Badalov Kh.N., Nesterenko V.O., Sushkov A.V., Wawryszczuk J. Z.Phys., 1988, A331, p.265.
- 19. Alikov B.A., Bonch-Osmolovskaya N.A., Nesterenko V.O. Izv. Ross. Akad. Nauk, Ser. Fiz., 1992, 56, n.11, p.43.
- Bonch-Osmolovskaya N.A., Nesterenko V.O. Izv.Ross.Akad.Nauk, Ser.Fiz., 1992, 56, n.11, p.53.
- 21. Fahlander C., Varnesting B., Backlin A. et al. Nucl. Phys., 1992, A537, p.183.
- 22. Mikhailov I.N., Usmanov Ph.N. Ann. Physik, 1993, 2, p.239.
- 23. Lo Iudice N., Palumbo F. Phys.Rev.Lett., 1978, 41, p.1532.
- Nesterenko V.O., Usmanov Ph.N., Okhunov A.A., Fahlander C. J.Phys.G, 1993, 19, p.1339.
- 25. Bohr A., Mottelson B.R. Nuclear Structure, v.2, W.A.Benjamin Inc., New-York, Amsterdam, 1974.
- 26. Soloviev V.G., Shirikova N.Yu. Z.Phys., 1981, A301, p.263.
- 27. Nesterenko V.O. Z.Phys., 1990, A335, p.147.

- Nesterenko V.O., Soloviev V.G., Sushkov A.V., Shirikova N.Yu. Yad.Fiz., 1986, 44, p.1143.
- 29. Nojarov R., Faessler A. Nucl. Phys., 1988, A484, p.1.
- 30. De Coster C., Heyde K. Nucl. Phys., 1991, A524, p.441.
- 31. Kvasil J., Mikhailov I.N., Safarov R.Ch., Choriev B. Czech. J. Phys., 1979, B29, p. 843.
- 32. Davydov A.S., Filippov G.F. Nucl. Phys., 1958, 8, p.237.
- 33. Faessler A., Greiner W., Sheline R.K. Nucl. Phys., 1965, 70, p.33.
- 34. Arima A., Iachello F. Advanc. in Nucl. Phys., 1984, 13, p.139.
- 35. Mikhailov I.N., Usmanov Ph.N. Yad. Phys., 1991, 54, p.1239.
- 36. Faessler A., Nojarov R., Scholtz F.G. Nucl. Phys., 1990, A515, p.237.
- 37. Baznat M.I., Pyatov N.I. Yad.Fys., 1975, 21,p.708.
- 38. Magnusson C. Phys.Scr., 1991, 43, p.460.
- 39. Baznat M.I., Pyatov N.I., Cherney M.I. Part. Nucl., 1973, 4, p.941.
- Alikov B.A., Badalov Kh.N., Nesterenko V.O., Sushkov A.V., Wawryszczuk J. JINR Preprint E4-87-917, Dubna, 1987.
- 41. Andreychev V. Part. Nucl., 1976, 7, p.1038.
- 42. Bernthal F.M., Rasmussen J.O. Nucl. Phys., 1976, 101, p.513.
- 43. Hamamoto I., Holler J., Zhang X.Z. Phys.Lett., 1989, B226, p.17.
- 44. Balodis M.K. et al. Izv. Akad. Nauk SSSR, Ser. Fiz., 1988, 52, p. 2117.