

FEMTOSCOPY WITHIN A HYDRODYNAMIC APPROACH BASED ON FLUX TUBE INITIAL CONDITIONS

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In pp scattering at LHC energies, large numbers of elementary scatterings will contribute significantly, and the corresponding high multiplicity events will be of particular interest. Elementary scatterings are parton ladders, identified with color flux tubes. In high multiplicity events, many of these flux tubes are produced in the same space region, creating high energy densities. We argue that there is good reason to employ the successful procedure used for heavy ion collisions: matter is assumed to thermalize quickly, so that the energy from the flux tubes can be taken as initial condition for a hydrodynamic expansion. This scenario gets spectacular support from very recent results on Bose–Einstein correlations in pp scattering at 900 GeV at the LHC.

В протон-протонных соударениях при энергиях большого адронного коллайдера значительный интерес представляют процессы множественного рождения. В этих процессах элементарные рассеяния представляются в виде партонных диаграмм лестничного типа, которые связаны с трубками, несущими цветной заряд. В событиях с высокой множественностью большое количество трубок возникает в одной и той же пространственной области, создавая большую плотность энергии. Утверждается, что есть все основания для применения метода, успешно используемого в соударениях тяжелых ионов. А именно предполагается быстрая термализация вещества, и плотность энергии распределения трубок выступает в качестве начальных условий для гидродинамического расширения. Такой сценарий согласуется с недавними измерениями бозе-эйнштейновских корреляций в протон-протонных соударениях при энергии 900 ГэВ на LHC.

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EPOS is a multiple scattering model in the spirit of the Gribov–Regge approach [1]. Here, one does not refer to simply multiple hard scatterings, the elementary processes correspond to complete parton ladders, which means hard scatterings plus initial state radiation. In this case, this elementary process carries an important fraction of the available energy, and therefore we treat very carefully the question of energy sharing in the multiple scattering process. Open and closed ladders have to be considered, in order to have a consistent quantum mechanical treatment. The corresponding graphs are squared, and we employ cutting rule techniques and Markov chains to obtain finally partial cross sections. The cut parton ladders are identified with longitudinal color fields or flux tubes, treated via relativistic string theory.

In case of very high energy pp collisions (at the LHC) or heavy ion scatterings already at RHIC, many flux tubes overlap and produce high energy densities. Let us consider the energy density at an early time in an AuAu scattering at RHIC, as obtained from an EPOS simulation [1]. The energy density shows a very bumpy structure concerning the x – y dependence (transverse coordinates), whereas the variation with the space-time rapidity η_s is small. There are in particular peaks in the x – y plane, which show up at the same position at different values of η_s . So we have sub-flux-tubes which exhibit a long range structure in the longitudinal variable η_s , with a typical transverse width of the order of a fermi. This is exactly the width we obtain if we compute the initial energy density in proton–proton scattering at the LHC. This means, if a hydrodynamic treatment is justified for Au–Au collisions at RHIC, it is equally justified for pp scattering at the LHC, provided the energy densities are high enough, which seems to be the case.

We are therefore going to employ a new tool for treating very high energy hadronic interactions including a hydrodynamic evolution (even in pp), as explained in [1]. In [1], we test the approach by investigating all soft observables of heavy ion physics, in case of AuAu scattering at 200 GeV. Let us consider proton–proton scattering now. In [2], we compare three different scenarios: the full calculations, including hydro evolution and hadronic cascade (full), the calculation without hadronic cascade (no casc), and the calculation without hydro and without cascade (base). Concerning particle spectra, we refer to [2], where we compare the corresponding calculations with experimental data, for pp scattering at 900 GeV.

The space-time evolution of the «full» hydrodynamic approach will be completely different compared to the «base» approach, where particles are directly produced from breaking strings, as can be seen from Fig. 1, where we plot the distribution of formation points of π^+ as a function of the radial distance $r = \sqrt{x^2 + y^2}$ (in the pp center-of-mass system (cms)) for the three scenarios. Only particles with space-time rapidities around zero are considered. All calculations in this paper refer to high-multiplicity events in pp scattering at 900 GeV, with a mean $dn/d\eta(0)$ equal to 12.9. The «base calculation» (dotted line) gives as expected a steeply falling distribution as a function of r . In the two cases involving a hydrodynamic evolution, particle production is significantly delayed, even more in the case of the full calculation, with hadronic cascade. The bump in the two latter scenarios is due to particles being produced from the fluid, the small p_t contribution is due to corona particles.

This particular space-time behavior of the hydrodynamic expansions should clearly affect Bose–Einstein correlations — what we are going to investigate in the following. There is a long history of so-called femtoscopic methods [4], where the study of two-particle correlations provides information about the source function $S(\mathbf{P}, \mathbf{r}')$, being the probability of emitting a pair with total momentum \mathbf{P} and relative distance \mathbf{r}' . Under certain assumptions, the source function is related to the measurable two-particle correlation function $CF(\mathbf{P}, \mathbf{q})$ as

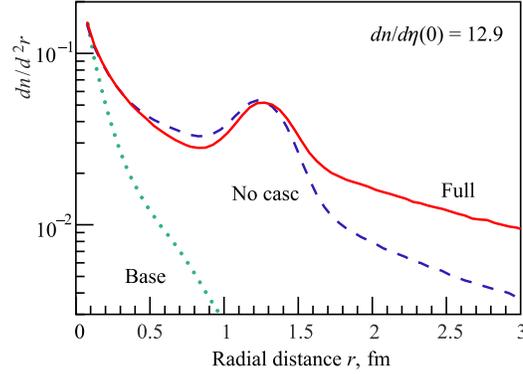


Fig. 1. (Color online) The distribution of formation points of π^+ as a function of the radial distance in a high-multiplicity event from pp scattering at 900 GeV, for the following scenarios: the full calculation (solid line), a calculation without hadronic cascade (dashed), and a calculation without hydro and without cascade (dotted)

$CF(\mathbf{P}, \mathbf{q}) = \int d^3r' S(\mathbf{P}, \mathbf{r}') |\Psi(\mathbf{q}', \mathbf{r}')|^2$, with \mathbf{q} being the relative momentum, and where Ψ is the outgoing two-particle wave function, with \mathbf{q}' and \mathbf{r}' being relative momentum and distance in the pair center-of-mass system. The source function S can be obtained from our simulations, concerning the pair wave function, we follow [5], some details are given in [1].

Here, we investigate $\pi^+\pi^+$ correlations. We calculate the correlation function with Bose-Einstein (BE) quantum statistics included, but no Coulomb corrections. Weak decays are not carried out. We compute correlation functions for different k_T interval defined as (in MeV): $KT1 = [100, 250]$, $KT3 = [400, 550]$, $KT5 = [700, 1000]$, where k_T of the pair is defined as $k_T = (|\mathbf{p}_t(\text{pion } 1) + \mathbf{p}_t(\text{pion } 2)|)/2$. In Fig. 2, *a*, we show the results for $KT1$. We compare the three different scenarios: «full calculation» (solid line), «calculation without hadronic cascade» (dashed), and «calculation without hydro and without cascade» (dotted), and data from ALICE [6]. The data are actually not Coulomb corrected, because the effect is estimated to be small compared to the statistical errors. We consider here the high-multiplicity class, with $dn/d\eta(0) = 11.2$, close to the value of 12.9 from our simulated high-multiplicity events. We compare with the real data (not polluted with simulations), normalized via

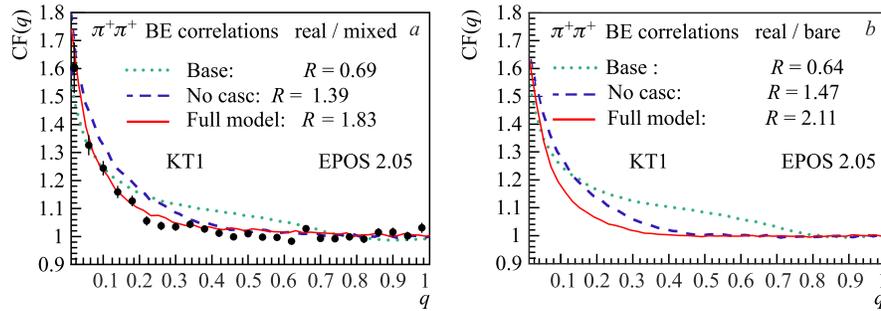


Fig. 2. (Color online) The correlation functions CF for $\pi^+\pi^+$ pairs as obtained from our simulations, for the three different scenarios, for k_T bin $KT1$, compared to data (points). *a*) Normalization via mixed events; *b*) normalization via a simulation without BE correlation («bare»)

mixed events, and we do the same with our simulations. Despite the limited statistics, in particular at large k_T , we see very clearly that the «full» scenario, including hydro evolution and hadronic cascade, seems to fit the data much better than the two other ones. Usually people like to extract radii from these distributions, so when we make a fit of the form $CF - 1 = \lambda \exp(-R|q|)$, in the $|q|$ range from 0.05 to 0.70. We obtain the radii given in the figure. So the radii are very different, varying from 0.69 fm (base approach) to 1.80 fm (full model), which is understandable from Fig. 1. We prefer an exponential fit rather than a Gaussian, simply because the former one works, the latter one does not. We do not want to give a precise meaning to R , it simply characterizes the distribution.

Normalizing by mixed events is something one can easily do experimentally (this is why we compare with these data), but it is clear that one has still unwanted correlations, like those due to energy-momentum conservation, which is not an issue in mixed events. Doing simulations, life is easier. We can take simulations without Bose–Einstein correlations as base line, rather than mixed events. This is referred to as «real/bare» normalization (to be distinguished from the «real/mixed» case discussed earlier). The corresponding results are shown in Fig. 2, *b*, the solid line (full calculation) is now completely horizontal away from the peak region, the radius from the exponential fit is 2.11 fm instead of 1.83 fm for the «mixed» normalization. For the other k_T regions, the situation is similar, the final results for all the three k_T regions for the full calculation are shown in Fig. 3, *a*, together with the radii from the exponential fit: they are almost identical, around 2 fm.

We get to the same conclusion as outlined in [6]: the radii are k_T -independent, contrary to what has been observed in AuAu scattering. How can it be that our hydrodynamic scenario gives a strong k_T dependence in AuAu, but not in pp ? To answer this question, we compute the «true» correlation function (real/bare normalization) for the calculation without hydro and without cascade (just string decay). The results are shown in Fig. 3, *b*. Surprisingly, here we get a strong k_T dependence of the radii, but the «wrong» way: we have 0.64 for KT1 and 1.63 fm for KT5! Actually such behavior is quite normal: the distribution is broader for high- p_t particles, because high- p_t resonances live longer and can move further out before decaying. This effect is in principle also present in AuAu scattering, but it is much more visible for the small pp system. So in pp we have two competing effects:

- radii increase with k_T , due to the bigger size of the source of the high- p_t particles compared to the low- p_t ones,

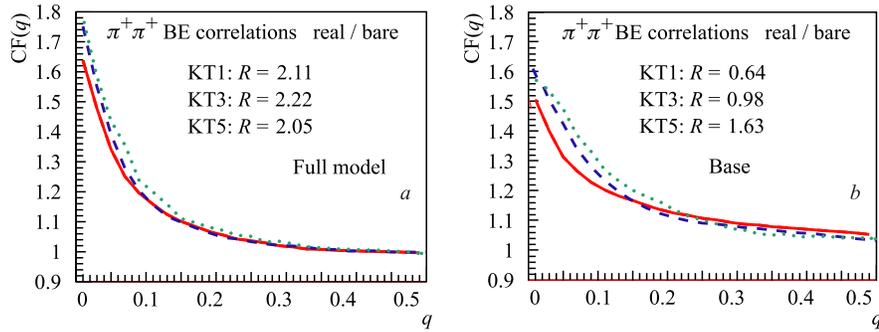


Fig. 3. (Color online) Correlation function, normalized by using a simulation without BE correlation («bare»), for three k_T intervals. *a*) Full model; *b*) calculation without hydro and without cascade

- radii decrease with k_T , as in AuAu (see [1]), in case of collective flow, due to the p - x correlation.

This p - x correlation exists indeed for the case of hydrodynamic evolutions, and is much smaller in the basic scenario. So in the hydro scenarios, the two competing effects roughly cancel, the radii are k_T -independent.

To summarize: we employ a hydrodynamic approach to pp scattering at 900 GeV. A very interesting application is Bose–Einstein correlations. We have shown that, as in heavy-ion scattering, the hydrodynamic expansion leads to momentum–space correlations, which clearly affect the correlation functions. To see the signal is nontrivial due to the fact that in addition to the x - p correlations (which leads to decreasing radii with k_T), there is a second effect which works the other way round: the single particle source size is p_t -dependent, which is an important effect in pp , not so in heavy-ion scattering. In this sense we can interpret the k_T independence of the radii as a real flow effect. Our simulation does not only reproduce the k_T independence, but also the whole correlation functions, which is not at all reproduced from the «base scenario» without hydro and without cascade. So the correlation data provide a very strong evidence for a collective hydrodynamic expansion in pp scattering at the LHC.

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REFERENCES

1. *Werner K. et al.* arXiv:1004.0805; Phys. Rev. C. 2010. V. 82. P. 044904.
2. *Werner K. et al.* arXiv:1010.0400; Phys. Rev. C (submitted).
3. *Bleicher M. et al.* // J. Phys. G. 1999. V. 25. P. 1859;
Petersen H. et al. // Phys. Rev. C. 2008. V. 78. P. 044901.
4. *Kopylov G. I., Podgoretsky M. I.* // Sov. J. Nucl. Phys. 1972. V. 15. P. 219; 1974. V. 18. P. 336;
Pratt S. // Phys. Rev. Lett. 1984. V. 53. P. 1219;
Lisa M. A. et al. // Ann. Rev. Nucl. Part. Sci. 2005. V. 55. P. 357–402;
Kisiel A., Florkowski W., Broniowski W. // Phys. Rev. C. 2006. V. 73. P. 064902.
5. *Lednicky R.* // Part. Nucl. 2009. V. 40. P. 307.
6. *ALICE Collab.* arXiv:1007.0516.

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