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VIOLATION OF  $CP$  INVARIANCE  
FOR NEUTRAL  $K^0$ ,  $D^0$ ,  $B_d^0$ ,  $B_s^0$  MESONS  
AND QUARKS IN WEAK INTERACTIONS

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Нарушение  $CP$ -инвариантности для кварков и нейтральных  $K^0$ -,  $D^0$ -,  $B_d^0$ -,  $B_s^0$ -мезонов в слабых взаимодействиях

Работа посвящена рассмотрению возможных схем введения  $CP$ -нарушения для нейтральных мезонов и кварков в слабых взаимодействиях. Отмечено, что в общем случае введение  $CP$ -фазы только для первого и третьего семейств является некорректным. Такие фазы нужно вводить и для остальных семейств, и при этом не обязательно, чтобы эти фазы были одинаковыми для всех семейств. Кроме того, рассмотрены нарушения  $CP$ -инвариантности для  $K^0$ -,  $D^0$ -,  $B_d^0$ -,  $B_s^0$ -мезонов, где кроме  $CP$ -фаз появляются углы смешивания  $\beta_1'$ ,  $\beta_c$ ,  $\beta_d$ ,  $\beta_s$ . Получены выражения для вероятностей переходов при  $CP$ -нарушении для этих мезонов. В заключение обсуждается схема  $CP$ -нарушения для  $d$ -,  $s$ -,  $b$ -кварков, где появляются углы их смешивания и фазы.

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Violation of  $CP$  Invariance for Neutral  $K^0$ ,  $D^0$ ,  $B_d^0$ ,  $B_s^0$  Mesons and Quarks in Weak Interactions

$CP$  violation in the Kobayashi–Maskawa matrix was introduced by using phase  $\delta$  which is the same for the three families of quarks. However, analysis of  $CP$  violation of mesons has shown that new small-angle mixings appear besides of  $CP$  phases. This work is devoted to the consideration of possible schemes for introducing  $CP$  violation. It is noted that in general case it is not correct to use  $CP$  phase only for the first and third quark families as it is usually introduced.  $CP$  phase has to be presented for all quark families, and moreover these phases cannot be the same for all families. Besides, a common case of  $CP$  violation was considered for  $K^0$ ,  $D^0$ ,  $B_d^0$ ,  $B_s^0$  mesons, where mixing angles and phases are present at  $CP$  violation. Expressions for transition probabilities for these processes are given. In conclusion, mixing of  $d$ ,  $s$ ,  $b$  quarks at  $CP$  violation was considered with taking into account their angle mixings and phases.

The investigation has been performed at the Veksler and Baldin Laboratory of High Energy Physics, JINR.

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## 1. INTRODUCTION

Previously it was supposed that  $P$  parity is a well number, however, after theoretical [1] and experimental [2] works it has become clear that in weak interactions  $P$  parity is violated. Then in work [3], there has been an advanced supposition that  $CP$  parity, but not  $P$  parity, is conserved in weak interactions. Work [4] has reported that there is two  $\pi$ -decay modes in  $K_L$  decays with a probability of about 0.2%, which is a detection of  $CP$ -parity violation.

It has been detected that strangeness  $S$  also is violated in weak interactions [5] (see also references in [6]). In order to solve this problem, N. Cabibbo [6] proposes to introduce matrix mixing of  $d$ ,  $s$  quarks. Then we can connect the decay modes of mesons (for example,  $\pi$  and  $K$  mesons) or giperons. For this aim, it is necessary to use charged weak interactions current  $j_F^\mu$  of  $d$ ,  $s$  quarks (of two quark families) in the following form:

$$j_F^\mu = (\bar{u}\bar{c})_L \gamma^\mu V \begin{pmatrix} d \\ s \end{pmatrix}_L, \quad V = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix}, \quad (1)$$

where  $V$  characterizes the mixing of  $d$  and  $s$  quarks, and  $\theta$  is the angle mixing of  $d, s$  quarks

$$\begin{pmatrix} d' \\ s' \end{pmatrix}_L = V \begin{pmatrix} d \\ s \end{pmatrix}_L. \quad (2)$$

This approach was then extended for the case of three quark families by Kobayashi and Maskawa in [7]. In the case of three quark families, there appears a parameter violating  $CP$  parity, while in the case of two quark families this parameter is absent. For introduction of the three quark mixings, we will use again charged vector current  $J^\mu$ , which has the following form:

$$J^\mu = (\bar{u}\bar{c}\bar{t})_L \gamma^\mu V \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L, \quad (3)$$

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}, \quad \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_L = V \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L, \quad (4)$$

It is more suitable to choose parameterization of  $V$  in the following form, which was proposed by Maiani [8]:

$$V = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_\gamma & s_\gamma \\ 0 & -s_\gamma & c_\gamma \end{pmatrix} \begin{pmatrix} c_\beta & 0 & s_\beta \exp(-i\delta) \\ 0 & 1 & 0 \\ -s_\beta \exp(i\delta) & 0 & c_\beta \end{pmatrix} \begin{pmatrix} c_\theta & s_\theta & 0 \\ -s_\theta & c_\theta & 0 \\ 0 & 0 & 1 \end{pmatrix},$$

$$c_\theta = \cos \theta, \quad s_\theta = \sin \theta, \quad c_\beta = \cos \beta, \quad c_\gamma = \cos \gamma, \quad \exp(i\delta) = \cos \delta + i \sin \delta, \quad (5)$$

where  $\theta, \beta, \gamma$  are mixing angles of three quarks and  $\delta$  is the parameter of  $CP$  violation. It is important to remark that the parameter of  $CP$  violation is the same for all three quark families, i.e., it is a global parameter.

## 2. $CP$ VIOLATION IN MESON SECTOR

Before considering  $CP$  violation, let us consider the case of Kobayashi–Maskawa matrix  $V'$  when the parameter of  $CP$  violation is zero ( $\delta = 0$ )

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix},$$

$$V' = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_\gamma & s_\gamma \\ 0 & -s_\gamma & c_\gamma \end{pmatrix} \begin{pmatrix} c_\beta & 0 & s_\beta \\ 0 & 1 & 0 \\ -s_\beta & 0 & c_\beta \end{pmatrix} \begin{pmatrix} c_\theta & s_\theta & 0 \\ -s_\theta & c_\theta & 0 \\ 0 & 0 & 1 \end{pmatrix}. \quad (6)$$

Values of 9 parameters  $V_{a,b}, a = 1-3, b = 1-3$  are established [9] by now. The values of  $\theta, \beta, \gamma$ , are established also, but value of  $\delta$  has not been established with high precision. Besides, the expression for  $V$  in (5) can have another form. For example, it can be in the form

$$V_2 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_\gamma & s_\gamma \\ 0 & -s_\gamma & c_\gamma \end{pmatrix} \begin{pmatrix} c_\beta & 0 & s_\beta \\ 0 & 1 & 0 \\ -s_\beta & 0 & c_\beta \end{pmatrix} \begin{pmatrix} c_\theta & s_\theta \exp(-i\delta) & 0 \\ -s_\theta \exp(i\delta) & c_\theta & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad (7)$$

or in the form

$$V_3 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_\gamma & s_\gamma \exp(-i\delta) \\ 0 & -s_\gamma \exp(i\delta) & c_\gamma \end{pmatrix} \begin{pmatrix} c_\beta & 0 & s_\beta \\ 0 & 1 & 0 \\ -s_\beta & 0 & c_\beta \end{pmatrix} \begin{pmatrix} c_\theta & s_\theta & 0 \\ -s_\theta & c_\theta & 0 \\ 0 & 0 & 1 \end{pmatrix}. \quad (8)$$

It is not obligatory that the parameter  $\delta$  in  $V, V_2, V_3$  must be the same. It can be different:  $\delta, \delta_2, \delta_3$ .

Let us consider more realistic case, but first consider  $CP$  violation for neutral  $K^0, D^0, B^0$  mesons.

**2.1. The Case of  $K^0, \bar{K}^0$  Mesons.** At strangeness violation,  $K^0, \bar{K}^0$  mesons are transformed into superposition states of  $K_1^0, K_2^0$  mesons

$$K^0 = \frac{K_1^0 + K_2^0}{\sqrt{2}}, \quad \bar{K}^0 = \frac{K_1^0 - K_2^0}{\sqrt{2}}, \quad (9)$$

and it leads to  $K^0, \bar{K}^0$  meson oscillations via  $K_1^0, K_2^0$ , which dominate in the time range  $t \simeq 0.0 \div 8\tau_{K_1^0}$  ( $\tau_{K_1^0}$  is the lifetime of  $K_1^0$  and  $\tau_{K_1^0} \cong \tau_{K_S}$  mesons).

$CP$  violation in the system of  $K^0$  mesons was widely investigated experimentally [1,4,9,10] and theoretically [11,12]. At  $CP$  violation in the system of  $K^0$  mesons, oscillations are absent and there is realized the interference between  $K_S, K_L$  states, which appear at  $CP$  violation

$$\begin{aligned} K_1^0(t) &= \cos \beta_1 K_S(t) + \sin \beta_1 e^{i\delta_1} K_L(t), \\ K_2^0(t) &= -\sin \beta_1 e^{-i\delta_1} K_S(t) + \cos \beta_1 K_L(t), \end{aligned} \quad (10)$$

where  $\beta_1$  is the angle mixing at  $CP$  violation, and  $\delta_1$  is the  $CP$  phase.

There can be the case [11], when

$$\begin{aligned} K_1^0(t) &= \cos \beta_1 K_S(t) + \sin \beta_1 e^{i\delta_1} K_L(t), \\ K_2^0(t) &= -\sin \beta_1 e^{i\delta_1} K_S(t) + \cos \beta_1 K_L(t). \end{aligned} \quad (10')$$

If we separate (factorize) time dependence of  $K_S(t), K_L(t)$ , then

$$K_S(t) = e^{-iE_S t - \frac{\Gamma_S t}{2}} K_S(0), \quad K_L(t) = e^{-iE_L t - \frac{\Gamma_L t}{2}} K_L(0), \quad (10'')$$

where  $E_k^2 = (p^2 + m_k^2)$ ,  $k = S, L$  and  $\Gamma_S, \Gamma_L$  are decay widths of  $K_S, K_L$  meson states.

Then the probability  $P(K^0, K_1^0 \rightarrow K_1^0, t)$  of the  $K_1^0(t)$  meson state presence in dependence on time  $t$  for primary  $K^0$  meson is given by the following expression [12]:

$$\begin{aligned} P(K^0, K_1^0 \rightarrow K_1^0, t) &= |K_1^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_S t) + \right. \\ &\left. + \varepsilon^2 \exp(-\Gamma_L t) + 2\varepsilon \exp\left(\frac{1}{2}(\Gamma_S + \Gamma_L)t\right) \cos((E_L - E_S) - \delta_1)t \right], \end{aligned} \quad (11)$$

and the probability  $P(\bar{K}^0, K_1^0 \rightarrow K_1^0, t)$  of the  $K_1^0(t)$  meson state presence in dependence on time  $t$  for primary  $\bar{K}^0$  meson is given by the following expression:

$$\begin{aligned} P(\bar{K}^0, K_1^0 \rightarrow K_1^0, t) &= |K_1^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_S t) + \right. \\ &\left. + \varepsilon^2 \exp(-\Gamma_L t) - 2\varepsilon \exp\left(\frac{1}{2}(\Gamma_S + \Gamma_L)t\right) \cos((E_L - E_S) - \delta_1)t \right], \end{aligned} \quad (12)$$

where  $\varepsilon = \sin \beta_1$  is the parameter of mixing at  $CP$  violation [12].

Value for  $\sin \beta_1 \simeq 2.23 \cdot 10^{-3}$ ,  $\delta_1 \simeq 43^\circ$  (see [1, 4, 9, 10]). The  $K_S, K_L$  meson interference dominates at  $t > 8\tau_{K_S}$ . It is important not to mix it up with  $K^0, \bar{K}^0$  meson oscillations, which dominate at  $t < 8\tau_{K_S}$ !

**2.2. The Case of  $D^0, \bar{D}^0$  Mesons.** The case of  $D^0, \bar{D}^0$  mesons fundamentally differs from the  $K^0, \bar{K}^0$  meson case, since they consist of  $c, u$  quarks  $D^0 = c\bar{u}$  and  $\bar{D}^0 = \bar{c}u$ . It is supposed that  $u, c, t$  quark states are not mixed in weak interactions, while  $d, s, b$  quarks are in mixed states (see Eq. (4)). Therefore the quark block diagram for  $D^0, \bar{D}^0$  meson oscillations will strongly differ from the  $K^0, \bar{K}^0$  meson oscillations case. We will not come to detailed consideration of  $D^0, \bar{D}^0$  meson oscillations, since we are interested in  $CP$  violation. However, it is necessary to remark that observation of  $D^0, \bar{D}^0$  meson oscillations is a very difficult problem. The task to detect  $CP$  violation in this case is also a very hard problem.

At violation of  $d, s, b$  number in weak interactions,  $D^0, \bar{D}^0$  mesons are transformed into superpositions of  $D_{1c}^0, D_{2c}^0$  mesons

$$D^0 = \frac{D_{1c}^0 + D_{2c}^0}{\sqrt{2}}, \quad \bar{D}^0 = \frac{D_{1c}^0 - D_{2c}^0}{\sqrt{2}}, \quad (13)$$

and it leads to  $D^0, \bar{D}^0$  meson oscillations via  $D_{1c}^0, D_{2c}^0$ .

At  $CP$  violation in the system of  $D^0, \bar{D}^0$  mesons, oscillations have to be absent and there is realized the interference between  $D_{Sc}(t), D_{Lc}(t)$  states, which appear at  $CP$  violation

$$\begin{aligned} D_{1c}^0(t) &= \cos \beta_c D_{Sc}(t) + \sin \beta_c e^{i\delta_c} D_{Lc}(t), \\ D_{2c}^0(t) &= -\sin \beta_c e^{-i\delta_c} D_{Sc}(t) + \cos \beta_c D_{Lc}(t), \end{aligned} \quad (14)$$

where  $\beta_c$  is the angle mixing at  $CP$  violation and  $\delta_d$  is the  $CP$  phase.

There can be the case [11] when

$$\begin{aligned} D_{1c}^0(t) &= \cos \beta_c D_{Sc}(t) + \sin \beta_c e^{i\delta_c} D_{Lc}(t), \\ D_{2c}^0(t) &= -\sin \beta_c e^{i\delta_c} D_{Sc}(t) + \cos \beta_c D_{Lc}(t). \end{aligned} \quad (14')$$

If to use the procedure which was done in (11), then the expression for probability  $P(D^0, D_{1c}^0 \rightarrow D_{1c}^0, t)$  of the  $D_{1c}^0(t)$  meson state presence in dependence on time  $t$  for primary  $D_d^0$  meson gets the following form:

$$\begin{aligned} P(D^0, D_{1c}^0 \rightarrow D_{1c}^0, t) &= |D_{1c}^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_{Sc}t) + \varepsilon_c^2 \exp(-\Gamma_{Lc}t) + \right. \\ &\quad \left. + 2\varepsilon_c \exp\left(\frac{1}{2}(\Gamma_{Sc} + \Gamma_{Lc})t\right) \cos((E_{Lc} - E_{Sc}) - \delta_c)t \right], \end{aligned} \quad (15)$$

and the probability of the presence of  $D_{1c}^0(t)$  meson state in time  $t$  dependence for primary  $\bar{D}_d^0$  meson is given by the following expression:

$$P(\bar{D}^0, D_{1c}^0 \rightarrow D_{1c}^0, t) = |D_{1c}^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_{Sc}t) + \varepsilon_c^2 \exp(-\Gamma_{Lc}t) - 2\varepsilon_c \exp\left(\frac{1}{2}(\Gamma_{Sc} + \Gamma_{Lc})t\right) \cos((E_{Lc} - E_{Sc}) - \delta_d)t \right], \quad (16)$$

where  $\varepsilon_d = \sin \beta_c$ ,  $\Gamma_{Sc}$ ,  $\Gamma_{Lc}$  are the decay widths of  $D_{Sc}$ ,  $D_{Lc}$  meson states [12].

Until now, an indication of a strong presence of  $CP$  violation in experiments with  $D^0$ ,  $\bar{D}^0$  mesons [13] has not been found.

**2.3. The Case of  $B^0, \bar{B}^0$  Mesons.** In this case,  $B^0, \bar{B}^0$  mesons consist of quarks, which are in mixed states in the framework of weak interactions. In contrast to the  $K^0$  meson case, here there will be two states  $B_d^0 = b\bar{d}$  and  $B_s^0 = b\bar{s}$ . The quark block diagram for  $B^0, \bar{B}^0$  mesons will work in analogy with the  $K^0, \bar{K}^0$  meson case (i.e., oscillations will take place there). Now we will consider some  $CP$  violation. As in the case of  $K^0$  mesons, at  $CP$  violation there has to arise interference between  $CP = \pm 1$  states. But observation of this interference term in experiments is a very hard task, since  $B_d^0, B_s^0$  have big masses and, hence, very many decay canals. Unfortunately, an indication of the strong presence of  $CP$  violation has not been found until now in experiments [14] with  $B_d^0, \bar{B}_d^0$  and  $B_s^0, \bar{B}_s^0$  mesons. Nevertheless, we can introduce, in analogy with  $K^0$  meson parameters, mixing angles and phase  $\delta_{ds}$  of  $CP$  violation.

At violation of  $b$ -number in weak interactions,  $B_d^0, \bar{B}_d^0$  mesons are transformed into superpositions of  $B_{1d}^0, B_{2d}^0$  bosons

$$B_d^0 = \frac{B_{1d}^0 + B_{2d}^0}{\sqrt{2}}, \quad \bar{B}_d^0 = \frac{B_{1d}^0 - B_{2d}^0}{\sqrt{2}}, \quad (17)$$

and it leads to  $B_d^0, \bar{B}_d^0$  meson oscillations via  $B_{1d}^0, B_{2d}^0$ .

At  $CP$  violation in the system of  $B^0, \bar{B}^0$  mesons, oscillations have to be absent and there is realized the interference between  $B_{Sd}, B_{Ld}$  states, which appear at  $CP$  violation

$$\begin{aligned} B_{1d}^0(t) &= \cos \beta_d B_{Sd}(t) + \sin \beta_d e^{i\delta_d} B_{Ld}(t), \\ B_{2d}^0(t) &= -\sin \beta_d e^{-i\delta_d} B_{Sd}(t) + \cos \beta_d B_{Ld}(t), \end{aligned} \quad (18)$$

where  $\beta_d$  is the angle mixing at  $CP$  violation, and  $\delta_d$  is the  $CP$  phase.

There can be the case [11] when

$$\begin{aligned} B_{1d}^0(t) &= \cos \beta_d B_{Sd}(t) + \sin \beta_d e^{i\delta_d} B_{Ld}(t), \\ B_{2d}^0(t) &= -\sin \beta_d e^{i\delta_d} B_{Sd}(t) + \cos \beta_d B_{Ld}(t). \end{aligned} \quad (18')$$

If to use the procedure which was done in (11), then the expression for probability  $P(B_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t)$  of the  $B_{1d}^0(t)$  meson state presence in dependence on time  $t$  for primary  $B_d^0$  meson gets the following form:

$$P(B_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t) = |B_{1d}^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_{Sd}t) + \varepsilon_d^2 \exp(-\Gamma_{Ld}t) + 2\varepsilon_d \exp\left(\frac{1}{2}(\Gamma_{Sd} + \Gamma_{Ld})t\right) \cos((E_{Ld} - E_{Sd}) - \delta_d)t \right], \quad (19)$$

and the probability  $P(\bar{B}_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t)$  of the presence of  $B_{1d}^0(t)$  meson state in time  $t$  dependence for primary  $\bar{B}_d^0$  meson is given by the following expression:

$$P(\bar{B}_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t) = |B_{1d}^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_{Sd}t) + \varepsilon_d^2 \exp(-\Gamma_{Ld}t) - 2\varepsilon_d \exp\left(\frac{1}{2}(\Gamma_{Sd} + \Gamma_{Ld})t\right) \cos((E_{Ld} - E_{Sd}) - \delta_d)t \right], \quad (20)$$

where  $\varepsilon_d = \sin \beta_d$ ,  $\Gamma_{Sd}$ ,  $\Gamma_{Ld}$  are decay widths of  $B_{Sd}$ ,  $B_{Ld}$  meson states [12].

At violation of  $b$  number in weak interactions,  $B_s^0$ ,  $\bar{B}_s^0$  mesons are transformed into superpositions of  $B_{1s}^0$ ,  $B_{2s}^0$  bosons

$$B_s^0 = \frac{B_{1s}^0 + B_{2s}^0}{\sqrt{2}}, \quad \bar{B}_s^0 = \frac{B_{1s}^0 - B_{2s}^0}{\sqrt{2}}, \quad (21)$$

and it leads to  $B_s^0$ -,  $\bar{B}_s^0$ -meson oscillations via  $B_{1s}^0$ ,  $B_{2s}^0$ .

In the case of  $B_s^0$ ,  $\bar{B}_s^0$  mesons, we have  $B_{Ss}$ ,  $B_{Ls}$  states, which appear at  $CP$  violation

$$\begin{aligned} B_{1s}^0(t) &= \cos \beta_s B_{Ss}(t) + \sin \beta_s e^{i\delta_s} B_{Ls}(t), \\ B_{2s}^0(t) &= -\sin \beta_s e^{-i\delta_s} B_{Ss}(t) + \cos \beta_s B_{Ls}(t), \end{aligned} \quad (22)$$

where  $\beta_s$  is the angle mixing at  $CP$  violation, and  $\delta_s$  is the  $CP$  phase.

There also can be the case [11] when

$$\begin{aligned} B_{1s}^0(t) &= \cos \beta_s B_{Ss}(t) + \sin \beta_s e^{i\delta_s} B_{Ls}(t), \\ B_{2s}^0(t) &= -\sin \beta_s e^{i\delta_s} B_{Ss}(t) + \cos \beta_s B_{Ls}(t). \end{aligned} \quad (22')$$

If to use the procedure which was done in (11), then the expression for probability  $P(B_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t)$  of the presence of  $B_{1s}^0(t)$  meson state in dependence on time  $t$  for primary  $B_s^0$  meson gets the following form:

$$P(B_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t) = |B_{1s}^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_{Ss}t) + \varepsilon_s^2 \exp(-\Gamma_{Ls}t) + 2\varepsilon_s \exp\left(\frac{1}{2}(\Gamma_{Ss} + \Gamma_{Ls})t\right) \cos((E_{Ls} - E_{Ss}) - \delta_s)t \right], \quad (23)$$

and the probability  $P(\bar{B}_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t)$  of the presence of  $B_{1s}^0(t)$  meson state in time  $t$  dependence for primary  $\bar{B}_s^0$  meson is given by the following expression:

$$P(\bar{B}_d^0, B_{1d}^0 \rightarrow B_{1d}^0, t) = |B_{1s}^0(t)|^2 \simeq \frac{1}{2} \left[ \exp(-\Gamma_{S_s} t) + \varepsilon_s^2 \exp(-\Gamma_{L_s} t) - 2\varepsilon_s \exp\left(\frac{1}{2}(\Gamma_{S_s} + \Gamma_{L_s}) t\right) \cos((E_{L_s} - E_{S_s}) - \delta_s) t \right], \quad (24)$$

where  $\varepsilon = \sin \beta_s$ ,  $\Gamma_{S_s}$ ,  $\Gamma_{L_s}$  are decay widths of  $B_{S_s}$ ,  $B_{L_s}$  meson states [12].

### 3. CP VIOLATION IN THE QUARK SECTOR

Now let us return to  $CP$  violation for quarks, but with another approach than it was done in [7]. There  $CP$  violation becomes apparent by using  $CP$  phase  $\delta$ . But at consideration of  $CP$  violation in the case of  $K^0$ ,  $\bar{K}^0$ , mesons we see that there appears a new angle mixing  $\beta_1$  and the phase  $\delta_1$ , while the angle mixing  $\beta_1$  in [7] is absent. For simplification we will consider  $CP$  violation in quark sector using pairs of quarks. For the first pair we have

$$\begin{pmatrix} d'' \\ s'' \end{pmatrix}_L = \begin{pmatrix} \cos \beta'_1 & \sin \beta'_1 e^{i\delta'_1} \\ -\sin \beta'_1 e^{i\delta'_1} & \cos \beta'_1 \end{pmatrix} \begin{pmatrix} d' \\ s' \end{pmatrix}_L. \quad (25)$$

It is obvious that  $\beta'_1 \neq \beta_1$  and  $\delta'_1 \neq \delta_1$ .

For the second pair of quarks we have

$$\begin{pmatrix} d'' \\ b'' \end{pmatrix}_L = \begin{pmatrix} \cos \theta'_1 & \sin \theta'_1 e^{i\delta'_2} \\ -\sin \theta'_1 e^{i\delta'_2} & \cos \theta'_1 \end{pmatrix} \begin{pmatrix} d' \\ b' \end{pmatrix}_L. \quad (26)$$

For the third pair of quarks we have

$$\begin{pmatrix} s'' \\ b'' \end{pmatrix}_L = \begin{pmatrix} \cos \gamma'_1 & \sin \gamma'_1 e^{i\delta'_3} \\ -\sin \gamma'_1 e^{i\delta'_3} & \cos \gamma'_1 \end{pmatrix} \begin{pmatrix} s' \\ b' \end{pmatrix}_L. \quad (27)$$

Probably origin of all the above parameters  $\beta'_1$ ,  $\theta'_1$ ,  $\gamma'_1$ ,  $\delta'_1$ ,  $\delta'_2$ ,  $\delta'_3$  has a dynamic character and, therefore, for computation of values of these parameters, it is necessary to know the precise dynamic nature of  $CP$  violation.

### CONCLUSION

$CP$  violation in Kobayashi–Maskawa matrix has been introduced by using phase  $\delta$ , which is the same for the three families of quarks. However, analysis of  $CP$  violation of mesons has shown that new small angle mixings appear besides

of  $CP$  phases. This work is devoted to the consideration of possible schemes for introducing  $CP$  violation. It is noted that in general case it is not correct to use  $CP$  phase only for the first and third quark families as it is usually introduced.  $CP$  phase has to be presented for all quark families and, moreover, these phases for all families cannot be the same. Besides, the common case of  $CP$  violation has been considered for  $K^0, D^0, B_d^0, B_s^0$  mesons, where mixing angles and phases are presented at  $CP$  violation.  $CP$  violation for  $K^0$  mesons is determined by the angle mixing  $\beta_1'$  and phase  $\delta_1'$ ; for  $B_d^0$  meson, by the angle mixing  $\beta_d$  and phase  $\delta_d$ ; and for  $B_s^0$  meson, by the mixing  $\beta_s$  and phase  $\delta_s$ . Also are given expressions for transition probabilities for these processes. And in conclusion mixing of  $d, s, b$  quarks at  $CP$  violation has been considered with taking into account their angle mixings and phases (i.e., there  $CP$  angle mixings appear besides of  $CP$  phases).

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